

# Modeling toroidal currents in the ionospheric electrojet regions

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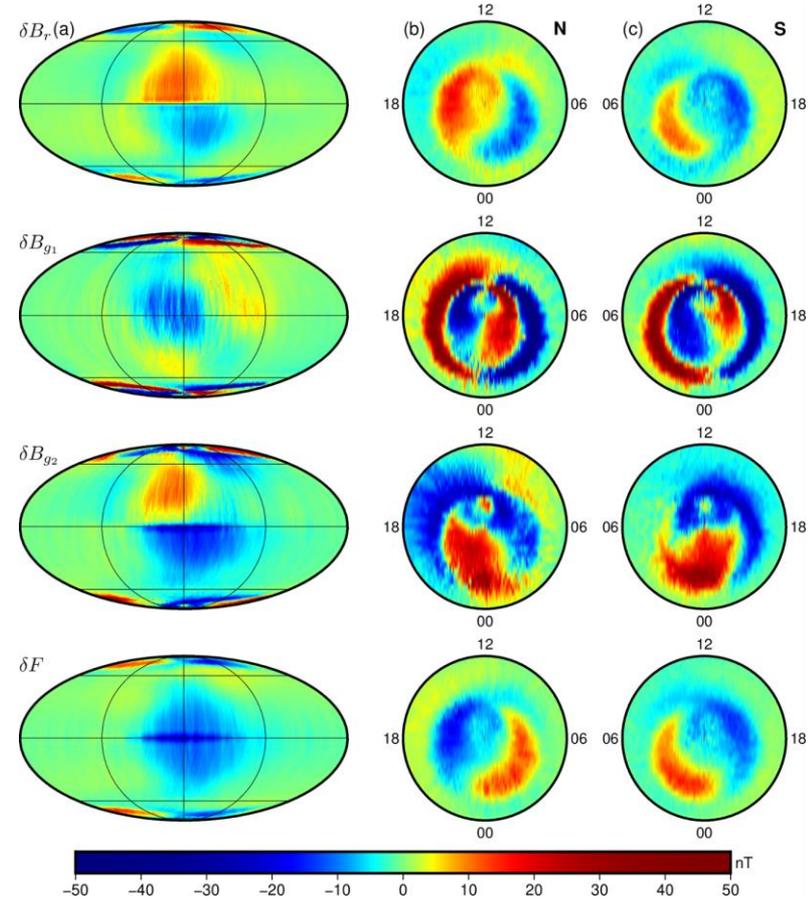
# Outline

- Electrojet observations and modeling history
- Methodology
- Rotated current loops in QD coordinates
- SH representation
- Covariance between current loops
- PCA and resulting basis functions
- Application: long-period electrojet signals seen in Swarm data



# Swarm observations of electrojets

- Swarm A mean ionospheric signal over six years
- January 1, 2017 to December 31, 2022
- Data binned with respect to QD Latitude and MLT

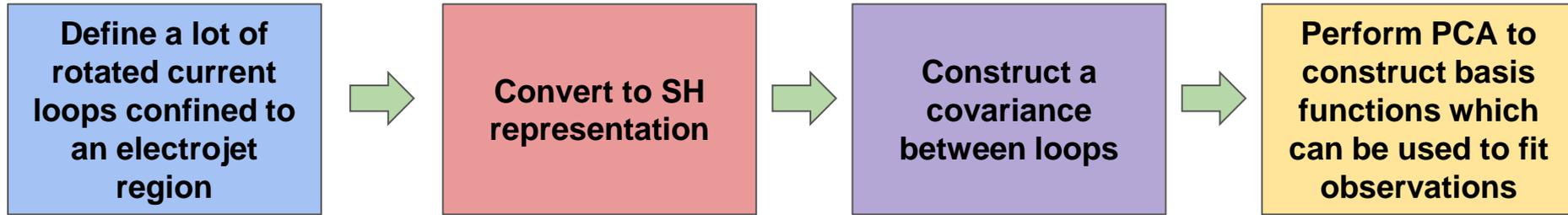


# Empirical electrojet modeling methods and history

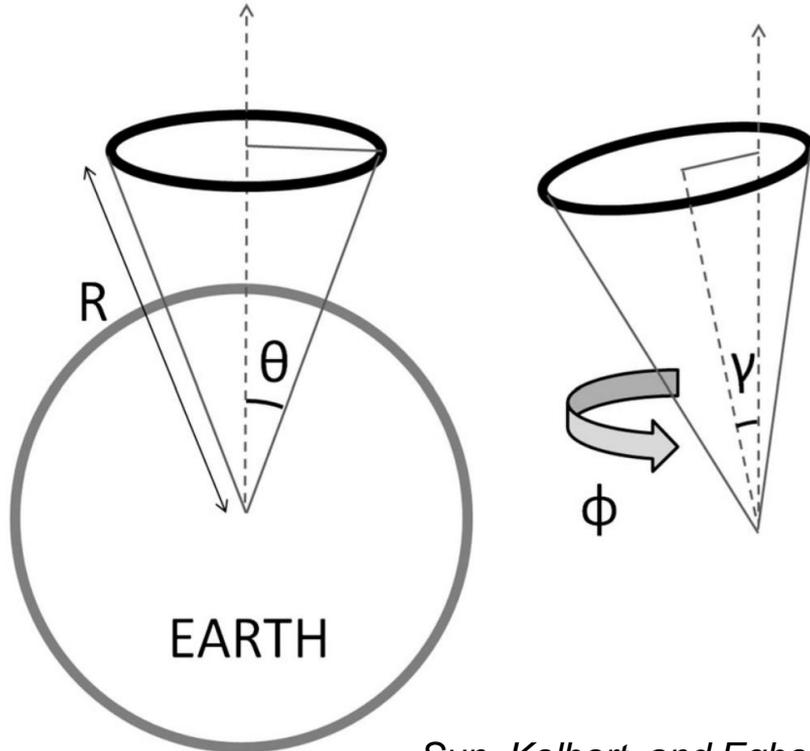
1D	2D	3D
<b>Line Currents</b> Olsen 1996 Ritter et al, 2003 Lühr et al, 2004 Alken et al, 2013, 2015 Aakjaer et al, 2016	<b>Spherical Harmonics</b> Haines, 1985 Sabaka et al, 2002 Torta et al, 2020	
<b>1DSECS</b> Vanhämäki et al, 2003 Juusola et al, 2006 Vanhämäki et al, 2020	<b>2DSECS</b> Amm 1997 Amm and Viljanen, 1999 Pulkkinen et al, 2003	
	<b>PCA of current loops</b> Sun, Kelbert and Egbert, 2015 This study	<b>Stay tuned...</b>



# Methodology



# Rotated current loops

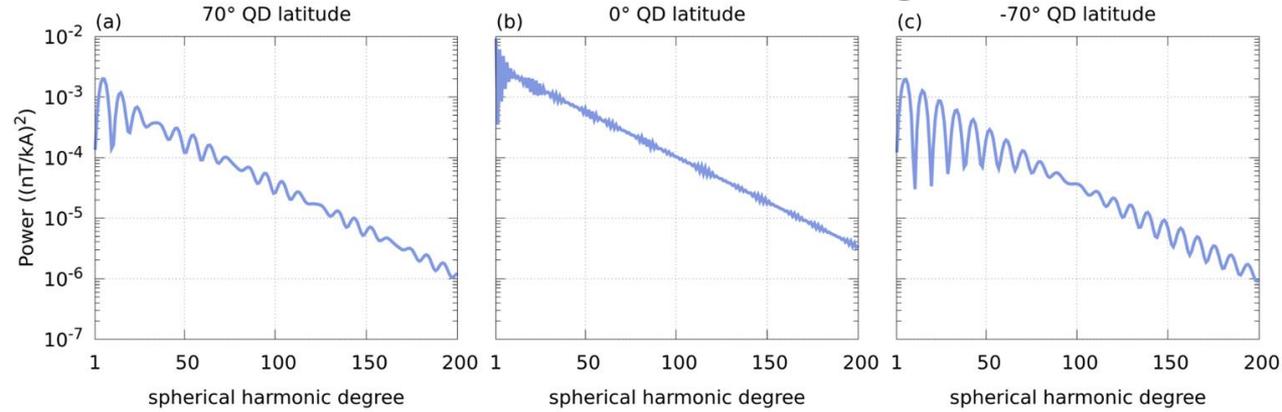


- Perform a large number of rotations to allow current flow in many different directions, with a preference for QD zonal flow

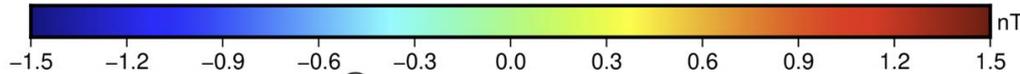
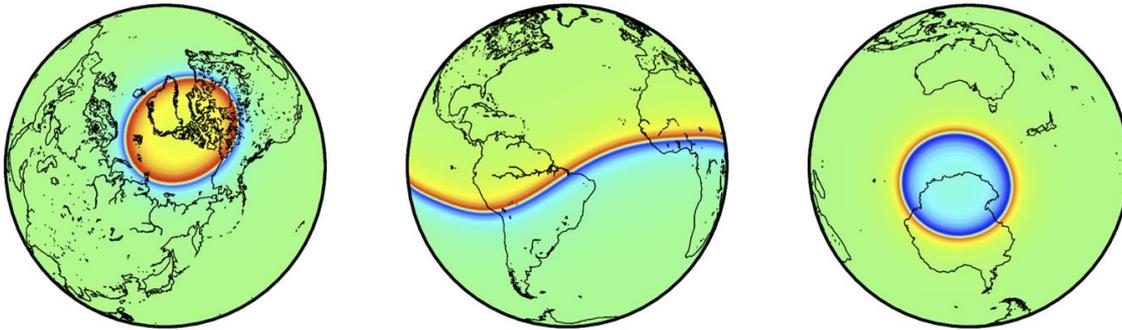
$$L_{final} = R_z(\eta)R_y(\psi)L_0$$

- $\eta, \psi$  are rotation angles for the loops in QD coordinates

# SH Representation of a single loop

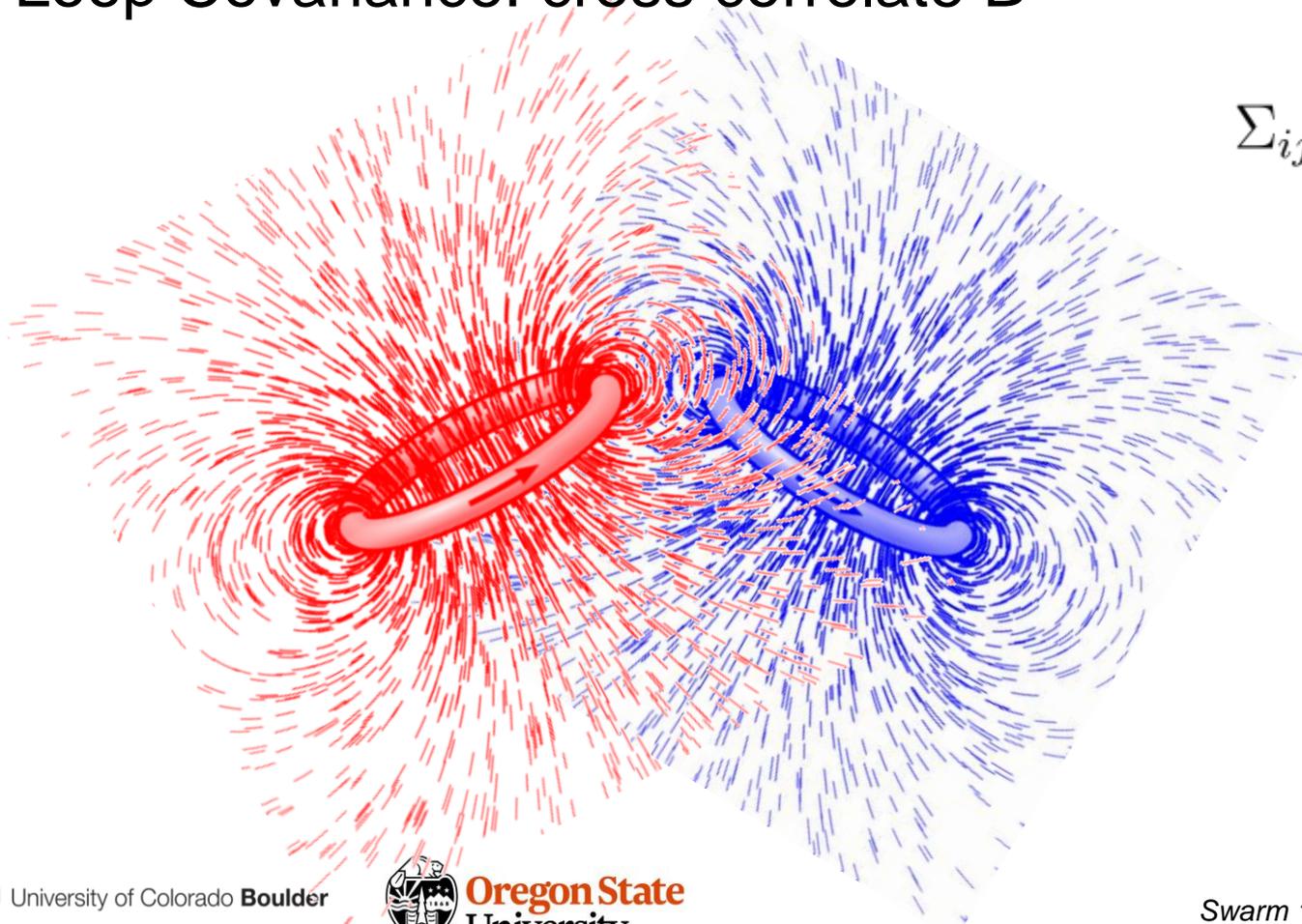


SH degree/order 90 for Swarm altitude



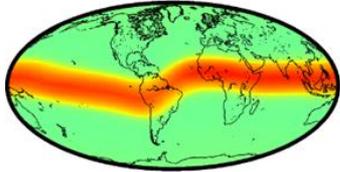
# Loop Covariance: cross correlate B

$$\Sigma_{ij} = \int \mathbf{B}_i \cdot \mathbf{B}_j d^3r$$

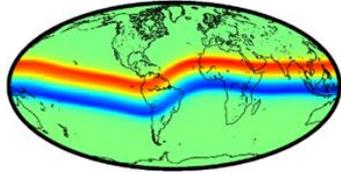


# Equatorial modes (surface Bx component)

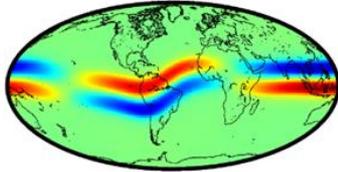
Mode 1



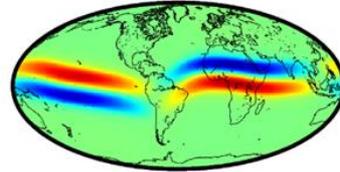
Mode 2



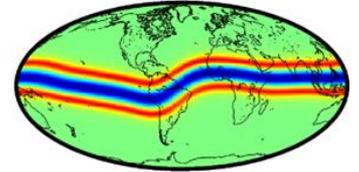
Mode 3



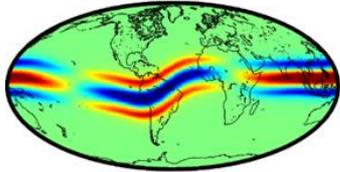
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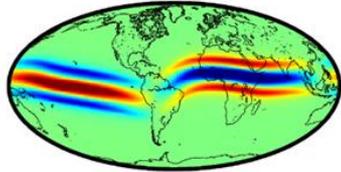
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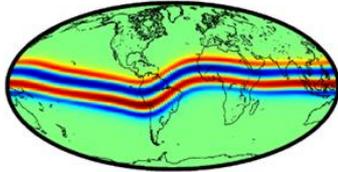
Mode 6



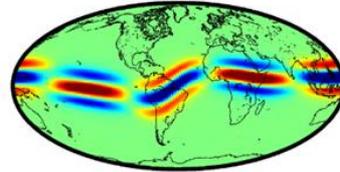
Mode 7



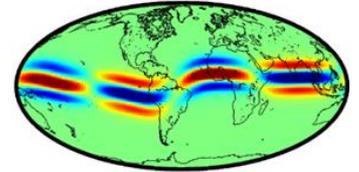
Mode 8



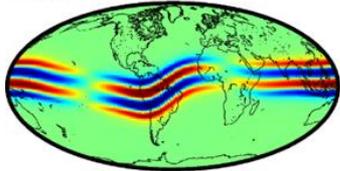
Mode 9



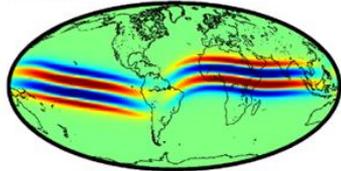
Mode 10



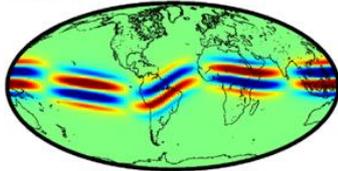
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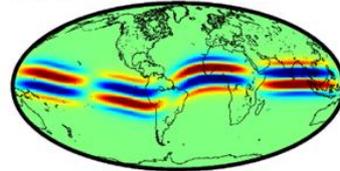
Mode 12



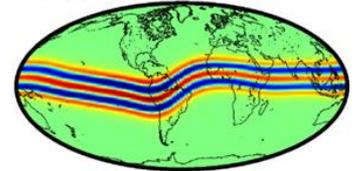
Mode 13



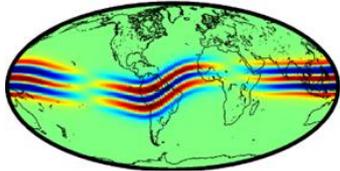
Mode 14



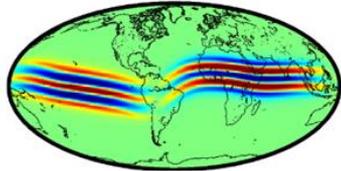
Mode 15



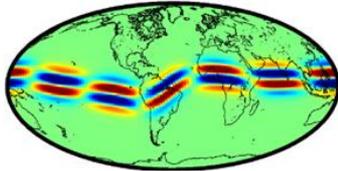
Mode 16



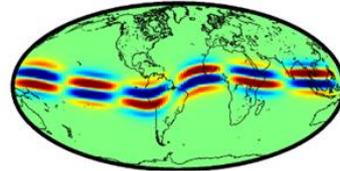
Mode 17



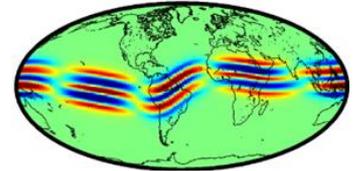
Mode 18



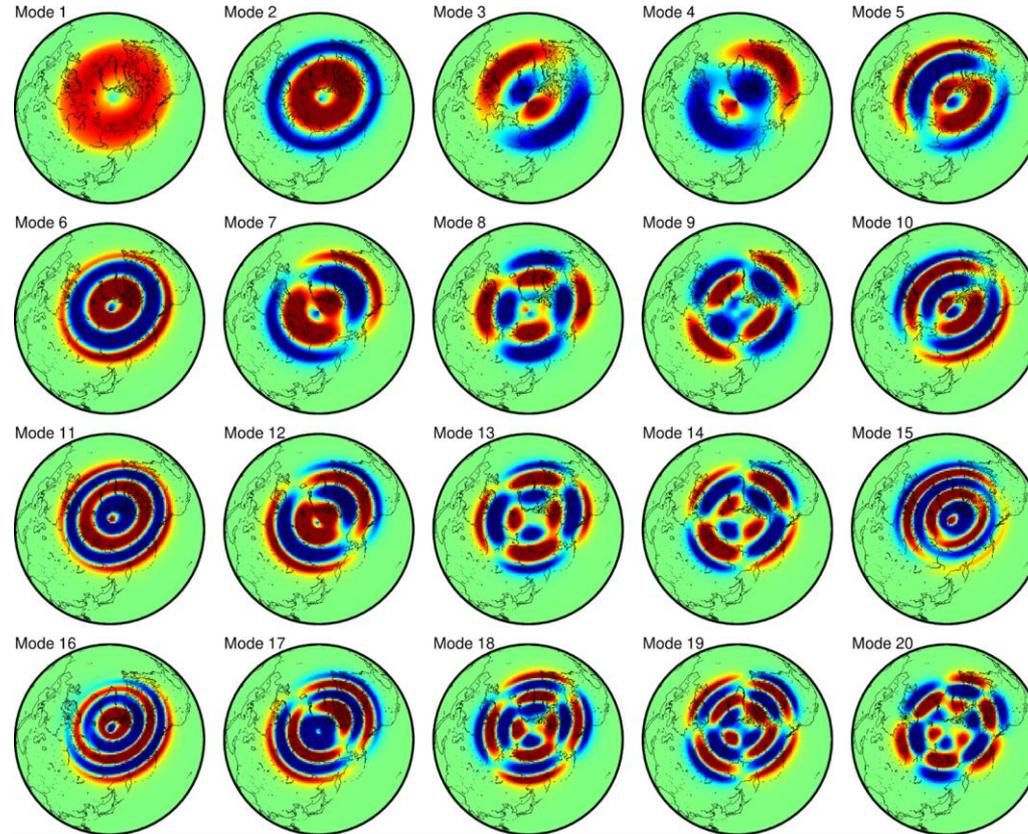
Mode 19



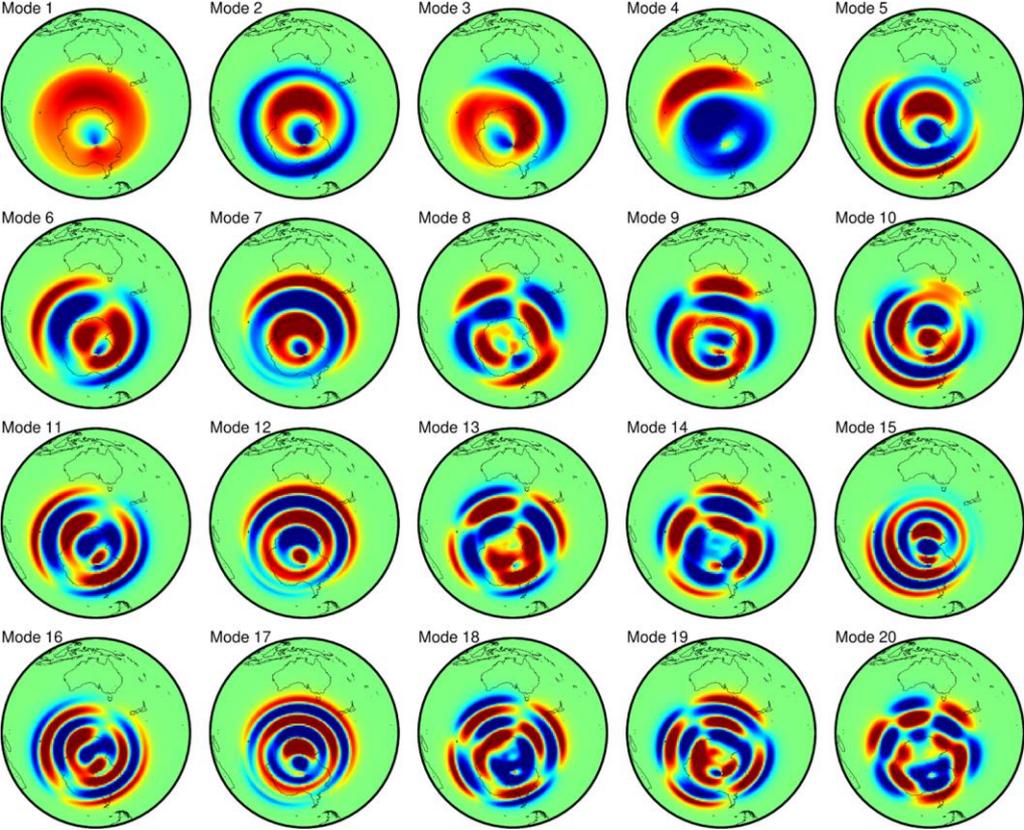
Mode 20



# Northern modes (surface Bx component)

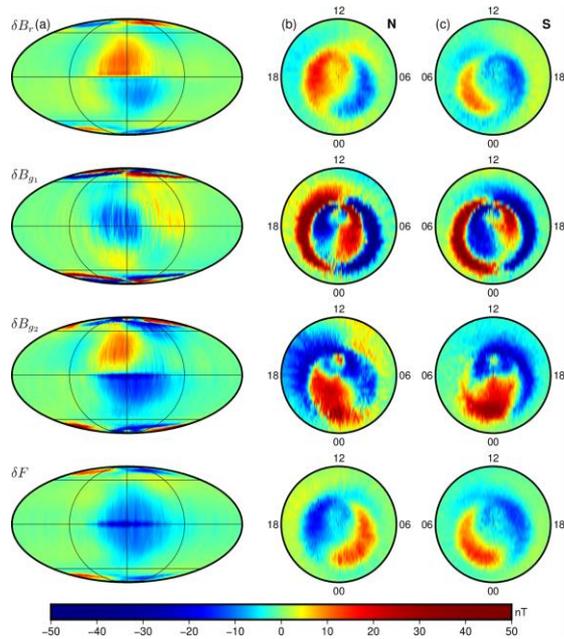


# Southern modes (surface Bx component)



# Application: fitting long-period electrojet signals

$$\mathbf{B}^{source}(\mathbf{r}, t) = \sum_{i=1}^W \alpha_i \Xi_i(\mathbf{r})$$

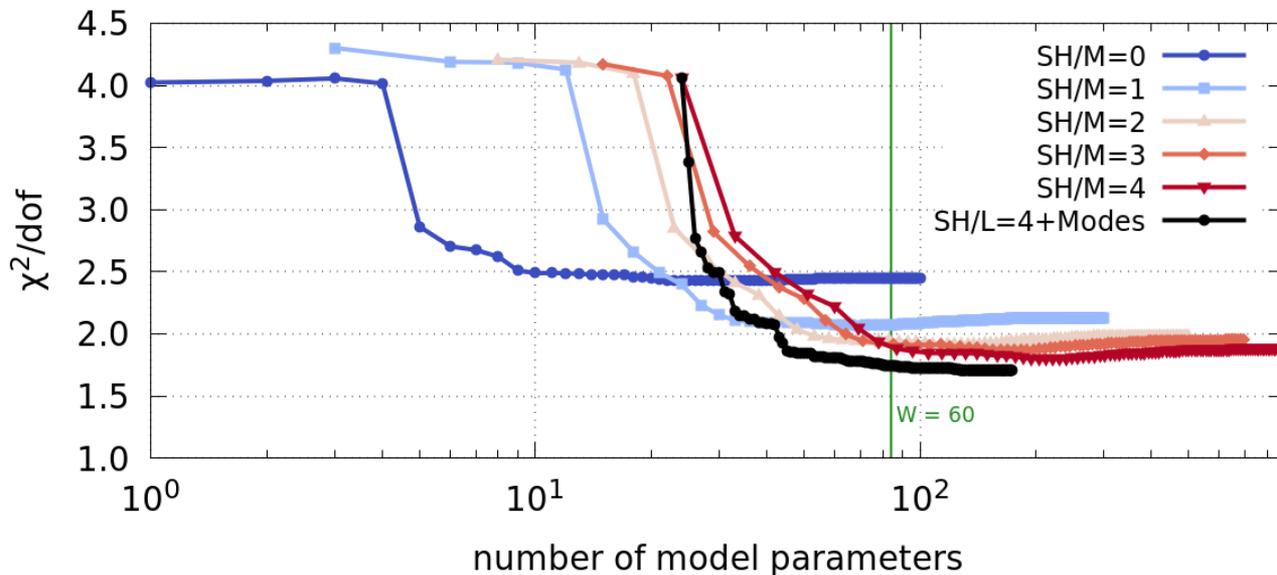


- Fit the mean ionospheric signal seen by Swarm over six years
- First term fits our new electrojet basis functions
- Second term is a low degree/order (L,M=4) SH model to capture mid-latitude Sq signals
- Model is regularized using the loop covariance matrix



# Application: goodness of fit analysis

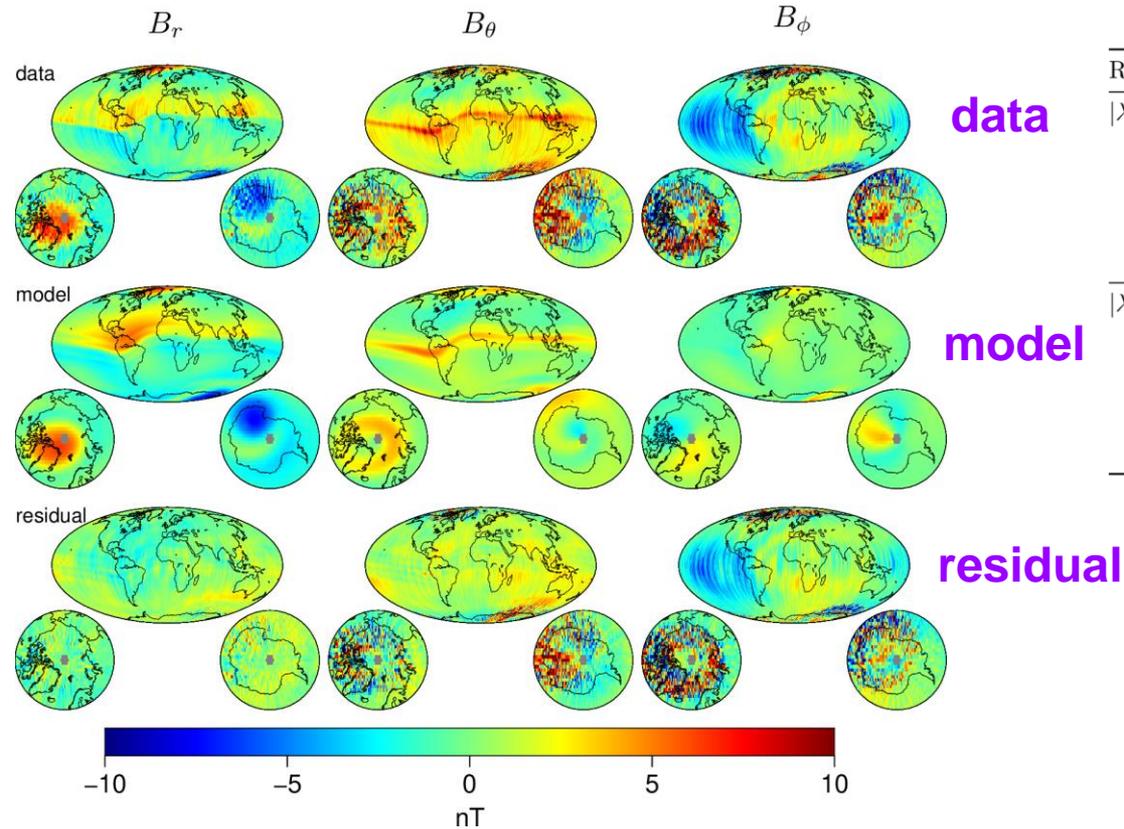
Goodness of fit



- Full model: L,M=4, W=60, **84** total model parameters
- SH only model: L=25,M=4, **213** model parameters

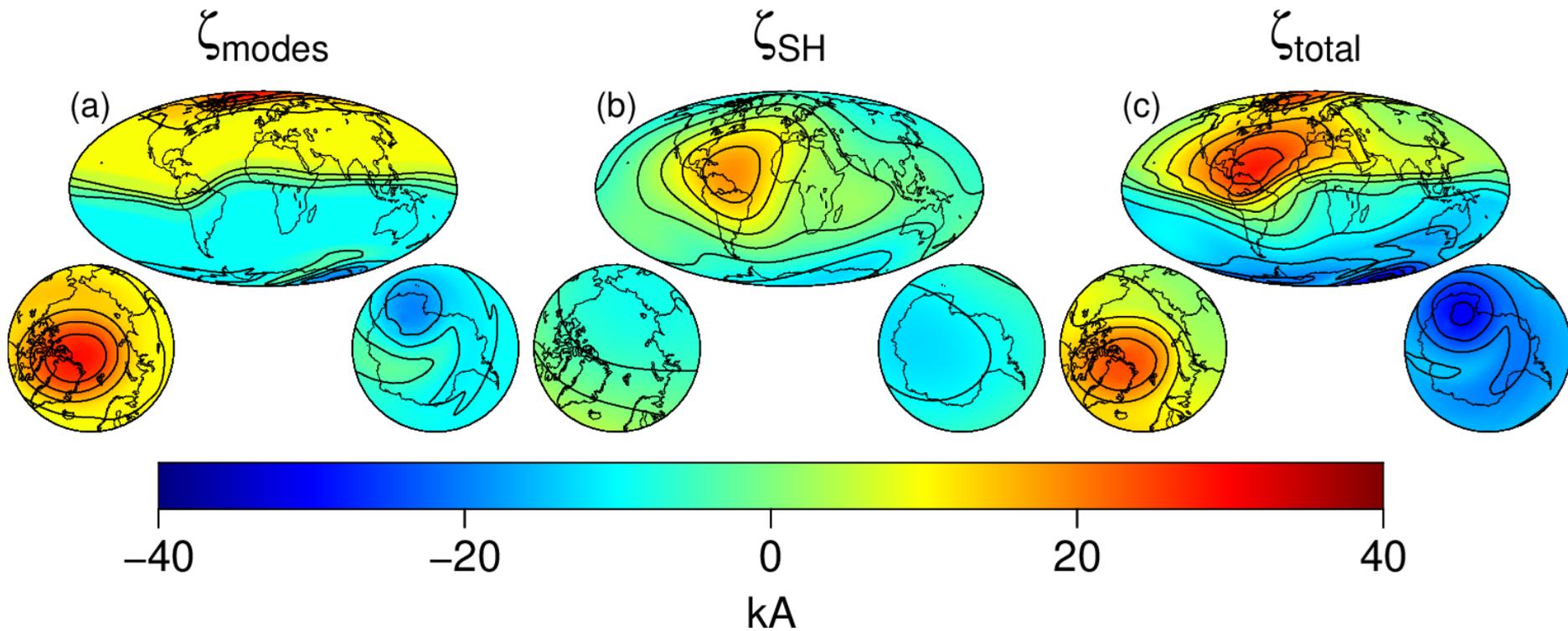


# Data, fitted model, and residuals



Region	Satellite	Component	$N$	$\mu$ (nT)	$\sigma$ (nT)	rms (nT)
$ \lambda_q  \leq 55^\circ$	Swarm A	$B_r$	39639	0.08	1.12	1.12
		$B_\theta$	39639	1.28	0.92	1.57
		$B_\phi$	39639	-0.57	1.92	2.00
	Swarm B	$B_r$	39631	-0.06	1.08	1.08
		$B_\theta$	39631	1.23	0.90	1.52
		$B_\phi$	39631	-0.45	1.90	1.95
$ \lambda_q  > 55^\circ$	Swarm A	$B_r$	23001	0.28	1.64	1.67
		$B_\theta$	23001	0.65	4.44	4.49
		$B_\phi$	23001	0.32	5.43	5.44
	Swarm B	$B_r$	23729	0.18	1.57	1.58
		$B_\theta$	23729	0.42	4.48	4.50
		$B_\phi$	23729	0.40	5.48	5.50

# Application: equivalent current stream function at 110km



# Summary

- We have developed a novel method of constructing basis functions to fit toroidal currents in the electrojet regions
- Our basis functions are fully 2D, and are based on PCA of a large number of rotated current loops
- We have applied these new functions to fit long-period signals in all 3 electrojet regions simultaneously

## Next Steps

- Fit shorter period electrojet signals
  - Orbit-by-orbit fits to Swarm A/C pair
- Simulations with Nanomagsat to see if we can recover longitudinal gradients in the electrojet currents

