

Identifying and accounting for the Coriolis effect in NO₂ observations and emission estimates

Daniel A. Potts ¹

Roger Timmis ²

Emma J. S. Ferranti ³

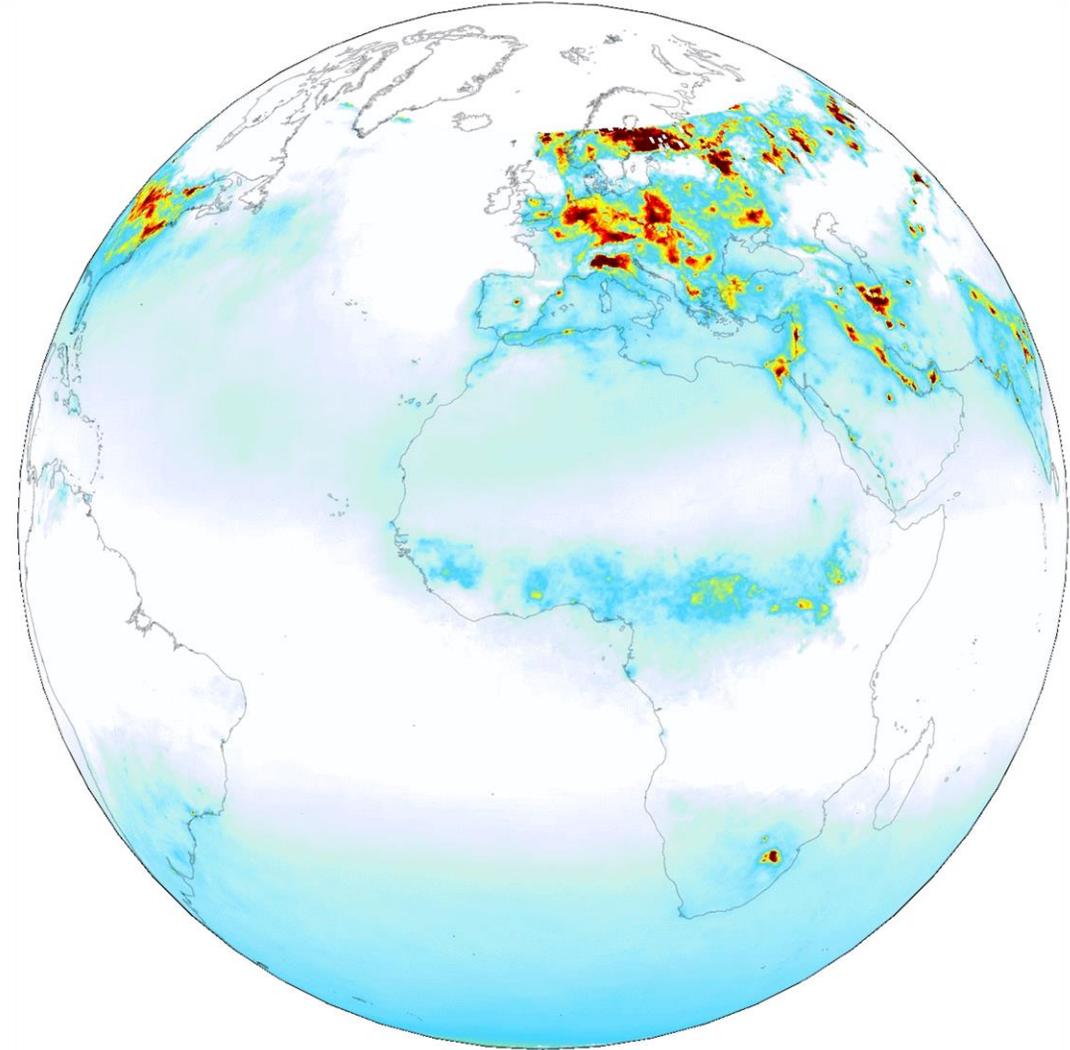
Joshua D. Vande Hey ^{1,4}

¹ School of Physics and Astronomy, University of Leicester, Leicester, UK

² Environment Agency, c/o Lancaster University, Lancaster, UK

³ School of Engineering, University of Birmingham, Edgbaston, UK

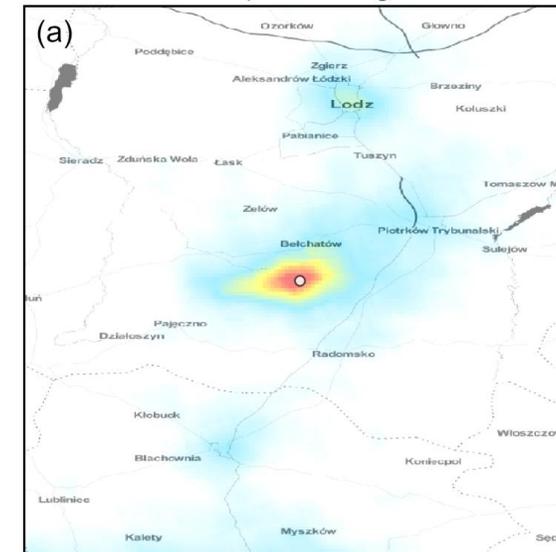
⁴ Centre for Environmental Health and Sustainability, University of Leicester, Leicester, UK



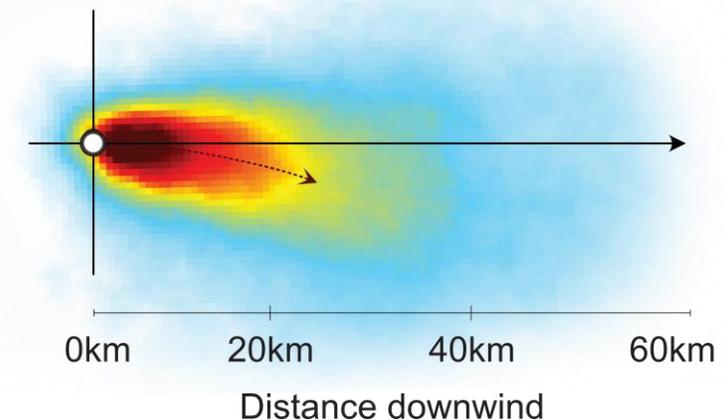
How this study came about

- PhD titled “smarter analysis of satellite data for air quality regulators”
- Testing out methods to quantify emissions from satellite observations
- Noticed a slight curvature in the wind rotated average from Belchatow power station in Poland
- Could this be due in part to the influence of the Coriolis Effect?

Temporal Average



Wind rotated average

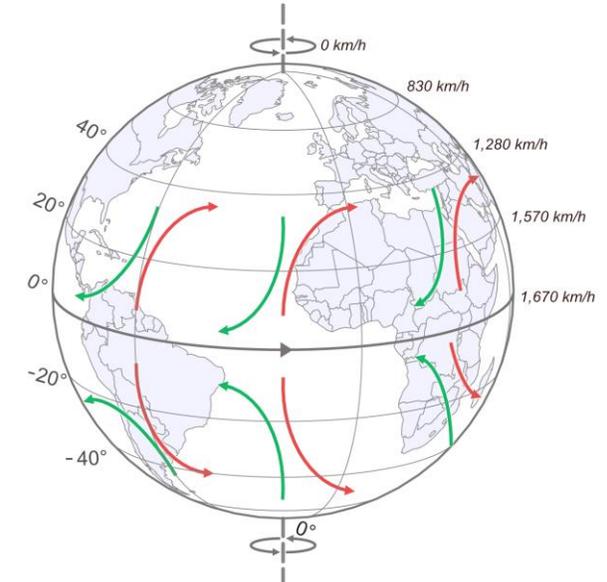


Coriolis effect

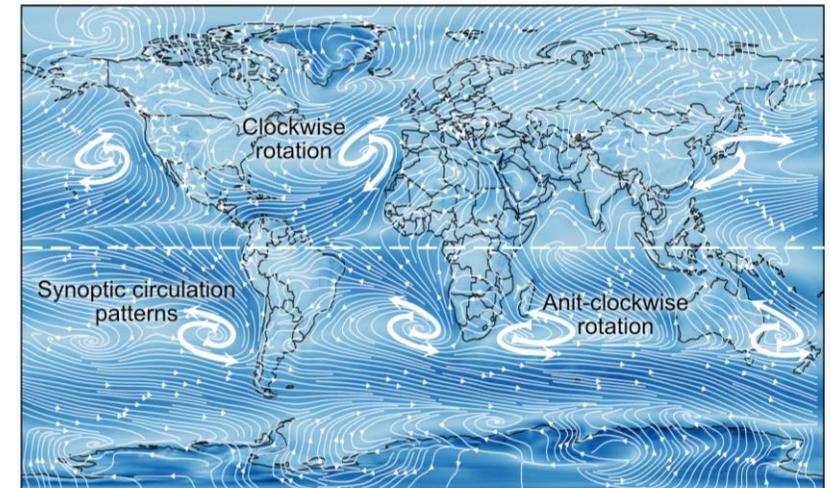
What is it?

- Inertial force that acts on an object that moves within a rotating coordinate system
- Deflects clockwise in Northern Hemisphere
- Deflects anti-clockwise in Southern Hemisphere
- Effect greatest at the poles
- Negligible at the equator
- $F_c = -2m(\Omega \times v)$
- Influences the movement of the atmosphere
 - Greater deflection for higher wind speeds

Atmospheric Coriolis Effect



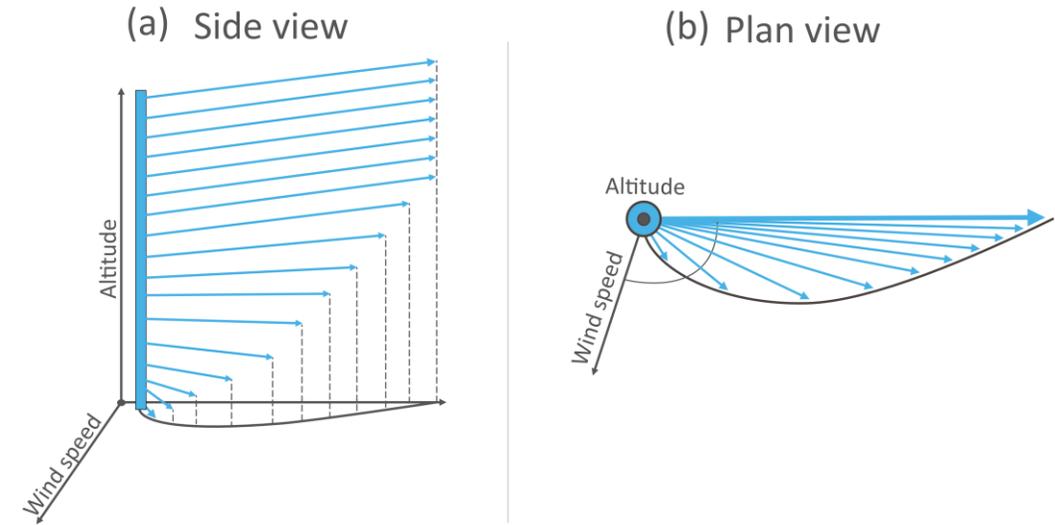
Average 100m winds (2019)



Coriolis effect

- Secondary impact of the Coriolis effect on emission plumes
- Plumes from power stations are
 - Thermally buoyant
 - Ejected at heights of +250 m
- Wind speeds increase with increasing altitude
- Coriolis force is a function of velocity $F_c = -2m(\Omega \times v)$
- When conditions allow for the plume to ascend,
 - Plume rises into faster moving wind field
 - Wind field above is orientated at an angle to the field below
- Known as the Ekman spiral

Atmospheric Ekman Spiral



Belchatow power station, Poland



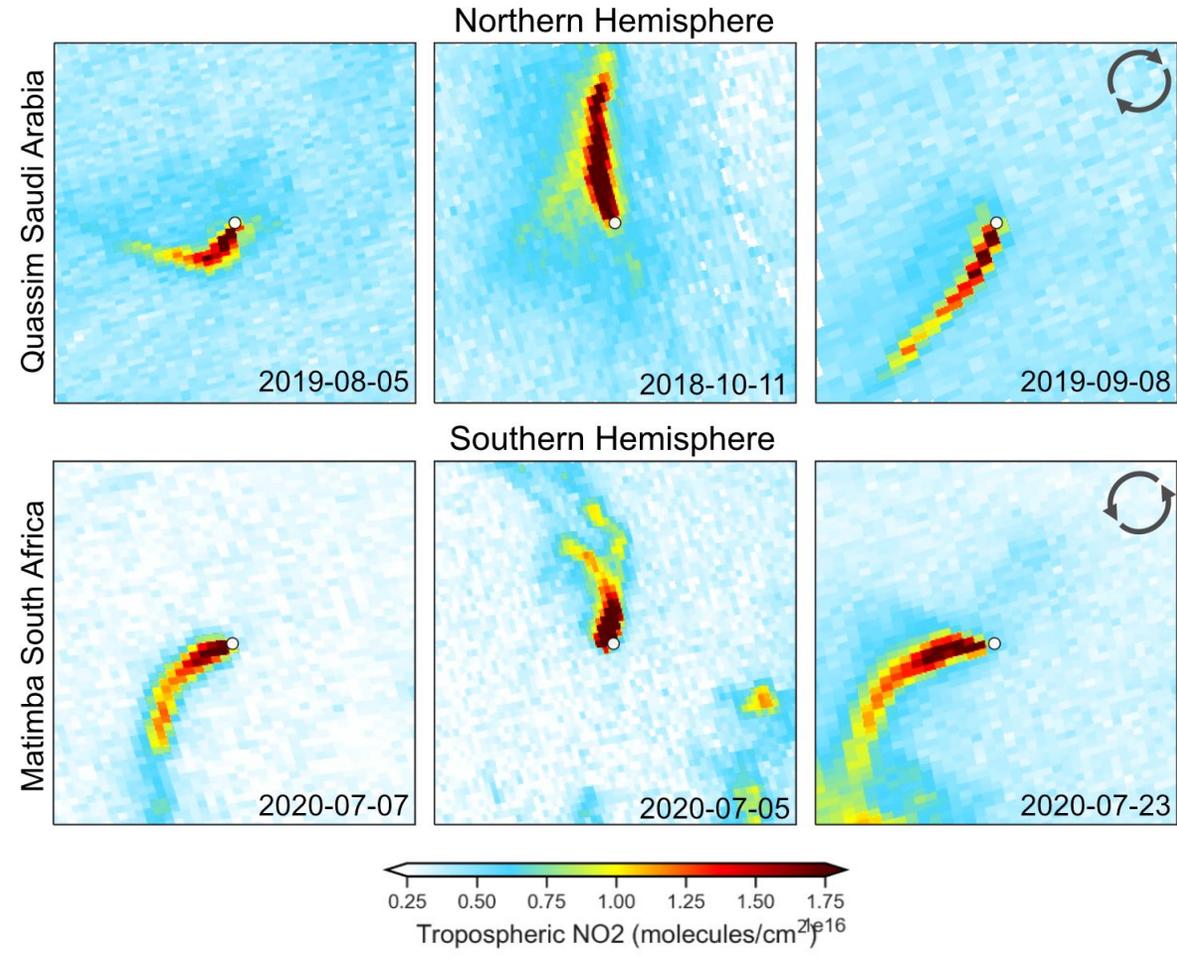
Impact on emission plumes

Emission plumes observed by TROPOMI can exhibit strong curvature

- Often (but not always) following the direction of the Coriolis force
- Local, smaller scale effect can dominate on daily timescales

Study question:

- For temporal averages, could Coriolis-induced curvature introduce a spatial bias?
- Does this effect emission quantification



Study design

16 large industrial point sources

- Mostly coal power stations
- Northern and southern hemisphere
- Range of continents
- Produce wind rotated aggregates for each site
- Identify presence/lack of curvature

n	Site name	Country	Type of site	Long	Lat	Stack height (m)	Capacity (MW)	Average surface pressure (hPa)
Northern Hemisphere								
1	Colstrip	USA	Coal power station	-106.61	45.8835	215	1480	900
2	Janschwalde	Germany	Coal power station	14.458	51.8344	300	3000	1006
3	Belchatow	Poland	Coal power station	19.327	51.267	300	5102	992
4	Quassim	Saudi Arabia	Oil power station	44.013	26.205	NA	915	939
5	Mae Moh	Thailand	Coal power station	99.751	18.296	200	2455	968
6	Vinh Tân	Vietnam	Coal power station	108.803	11.317	210	6225	992
7	Neyveli	India	Coal power station	79.441	11.558	275	3390	1002
8	Raichur	India	Coal power station	77.343	16.355	220	1720	965
Southern Hemisphere								
9	Chuquicamata	Chile	Copper smelter	-68.890	-22.314	NA	NA	736
10	Matimba	South Africa	Coal power station	27.613	-23.669	250	3690	914
11	Muja	Australia	Coal power station	116.305	-33.445	151	1094	985
12	Tarong	Australia	Coal power station	151.915	-26.784	210	1400	962
13	Tanjung	Indonesia	Coal power station	110.745	-6.445	240	2640	996
14	Hwange	Zimbabwe	Coal power station	26.470	-18.383	180	920	921
15	Jorge Lacerda	Brazil	Coal power station	-48.969	-28.452	200	857	1008
16	Millmerran	Australia	Coal power station	151.279	-27.962	141	850	967



Wind rotation & EMG

- Common approach to derive emissions from satellite observations

- Pommier et al, 2013

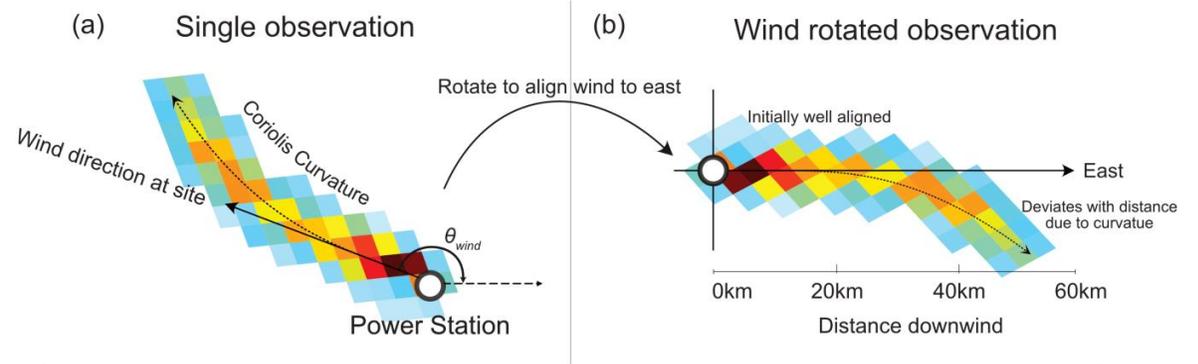
- Used for emissions from:

- Cities (Goldberg et al, 2019)
 - Power stations (Fioletov et al, 2015 & Hakkarainen et al, 2021),
 - Fertiliser plants (Clarisse et al, 2019 & Dammers et al, 2019)

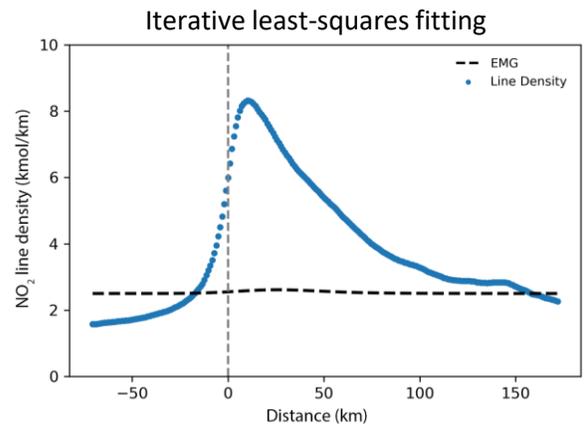
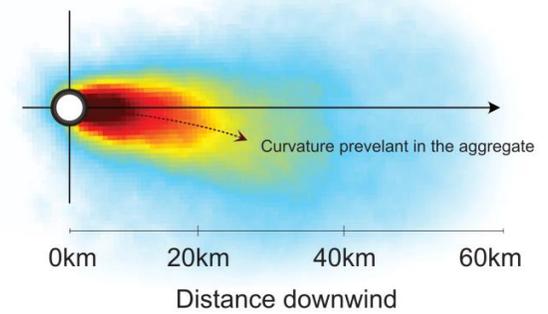
- Rotate all quality observations to a common axis in respect to that observations wind direction

- Fit an Exponentially Modified Gaussian (EMG)

- Extract emissions from fit parameters



(c) Rotate and aggregate multiple observations



$$NO_2 \text{ line density} = \alpha \left[\frac{1}{x_o} \exp\left(\frac{\mu}{x_o} + \frac{\sigma^2}{2x_o^2} - \frac{x}{x_o}\right) \Phi\left(\frac{x - \mu}{\sigma} - \frac{\sigma}{x_o}\right) \right] + \beta$$

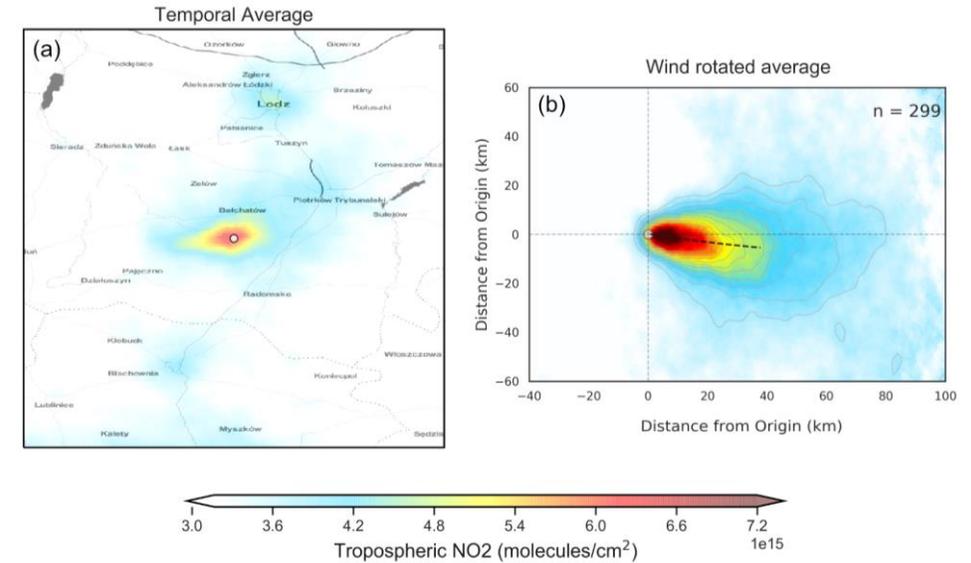
$$NO_x \text{ emissions} = 1.33 \left(\frac{\alpha}{\tau_{eff}} \right), \quad \text{where } \tau_{eff} = \frac{x_o}{\omega}$$

Examples of curvature

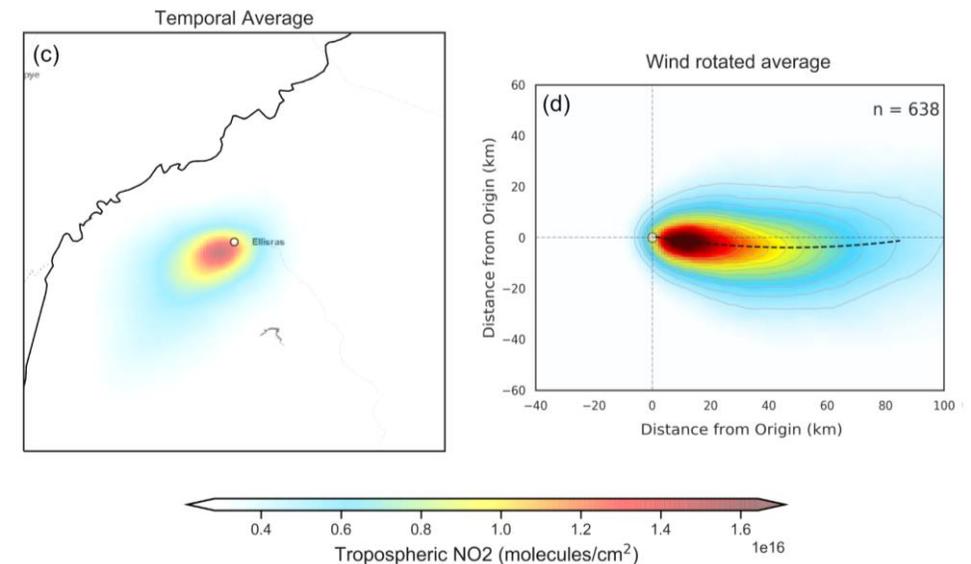
- Of the 16 sites:
 - 9 showed identifiable curvature
 - In expected direction
 - 5 showed no/negligible curvature
 - 2 showed opposing curvature
 - Discussed next slide

- Clear deflection of aggregate plume from the “common” axis

Belchatow, Poland



Matimba, South Africa

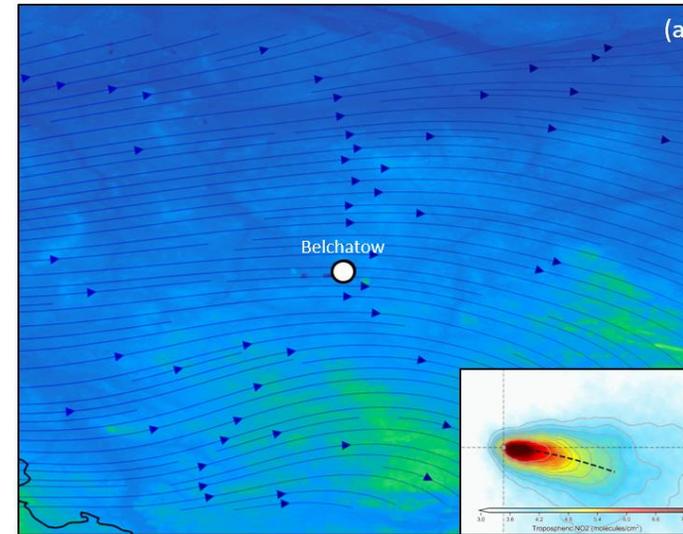


Opposing curvature cases

- Jorge Lacerda, Brazil
- Chuquicamata, Chile

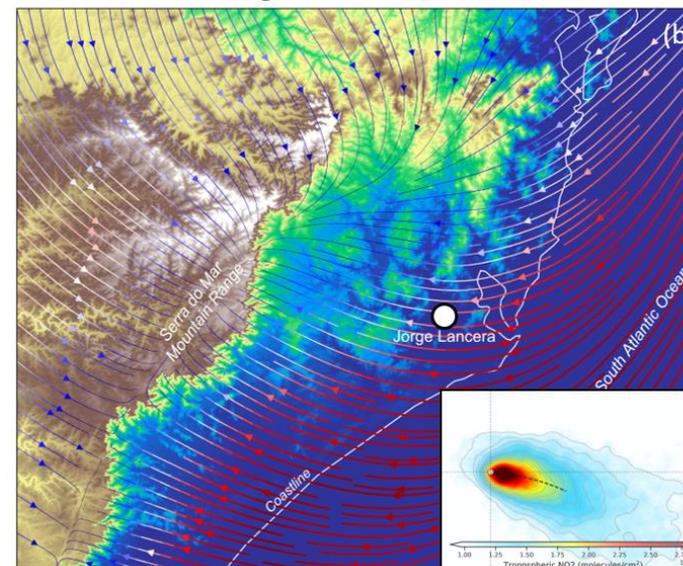
- Both in highly variable topographic regions
- Small scale local affects dominate over larger scale Coriolis influence
- In contrast to Belchatow with low speed, uniform wind fields

Belchatow, Poland



Correct curvature
Weak local affects
Coriolis prevalent

Jorge Lacerda, Brazil

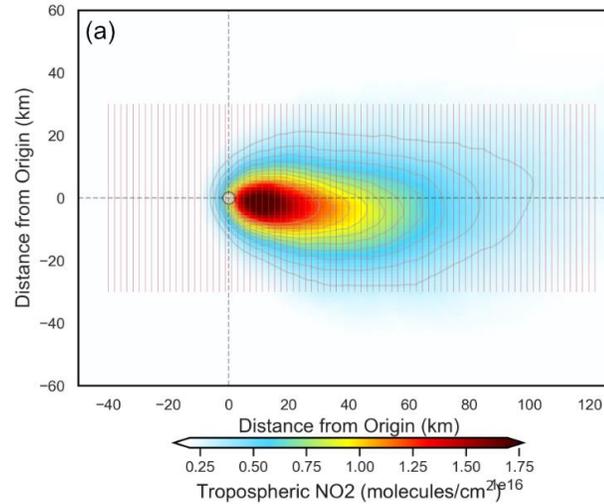


Opposing curvature
Strong local affects
Coriolis not visible

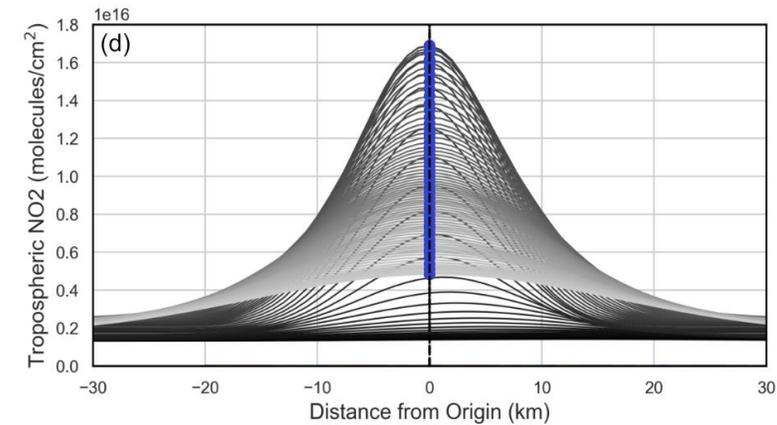
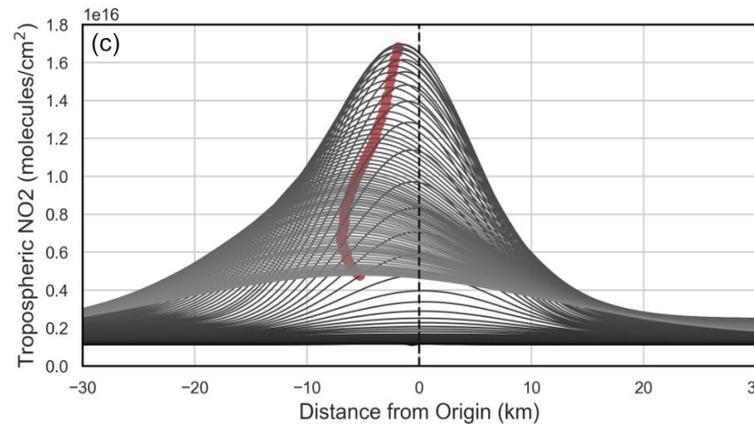
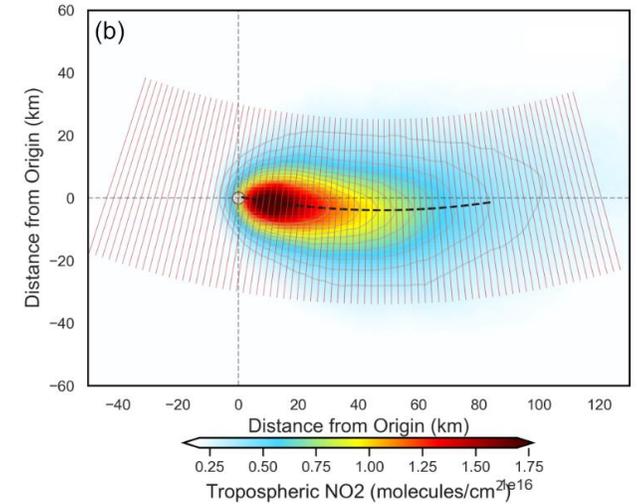
Impact on emission estimates

- Two approaches
 - a) Perpendicular to axis
 - b) Perpendicular to plume spine
- By taking transects perpendicular to the plume spine, transect peaks are realigned to the origin
- More representative path of dispersion

Scenario (a)
Perpendicular to the x-axis

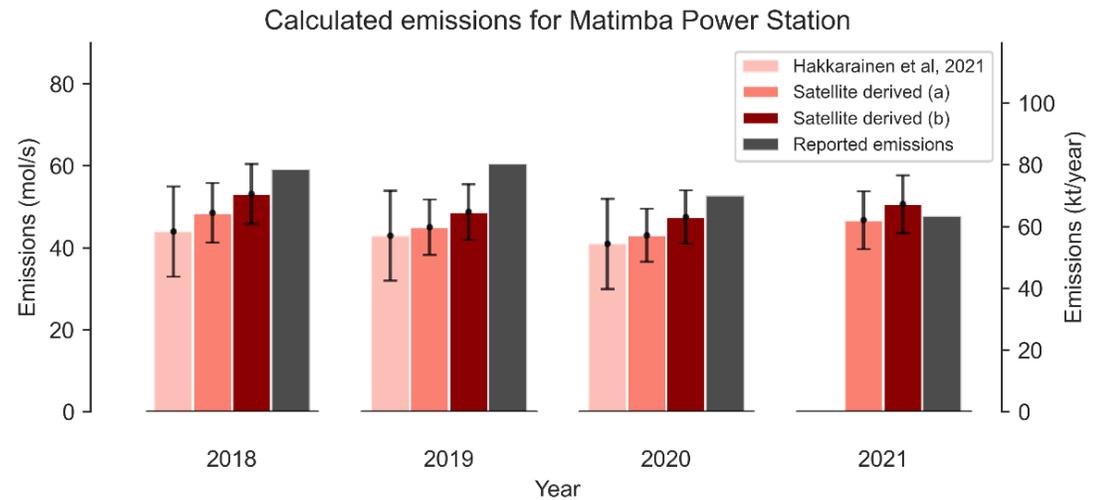
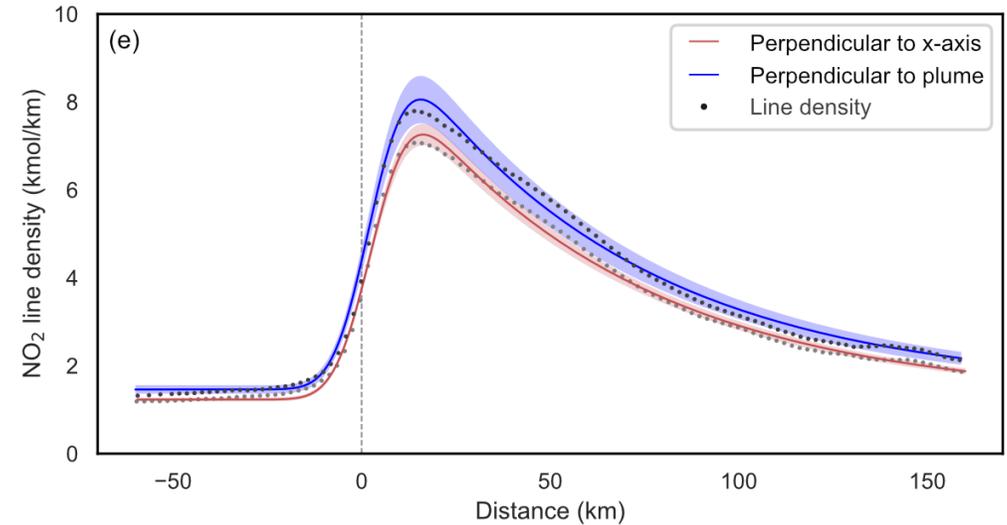


Scenario (b)
Perpendicular to the plume spine



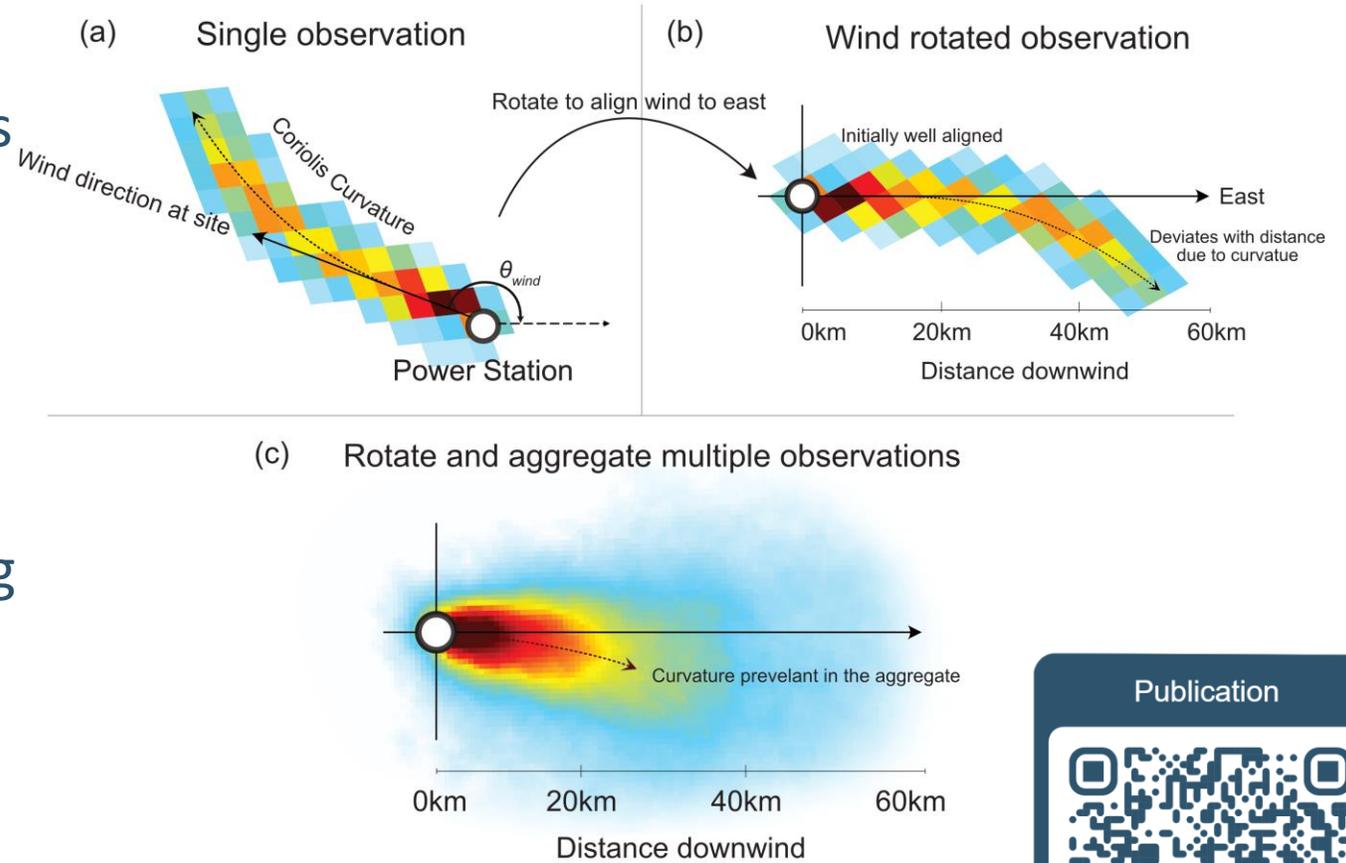
Impact on emission estimates

- Approach (b) yields a higher maximum in line density curve
- Approach (b) yielded an emission rate more comparable to reported emissions
- **9%** difference in emission estimates between (a) and (b)



Take away points

- Coriolis induced curvature can be observed in observed emission plumes
- In certain locations with simple meteorology
 - Curvature can be high
 - Can impact emission estimates (~9%)
- Care should be taken when performing wind rotation to ensure correct alignment to common axis
- If not aligned, the curvature should be accounted for



Potts, D. A., Timmis, R., Ferranti, E. J., & Vande Hey, J. D. (2023). *Identifying and accounting for the Coriolis effect in satellite NO₂ observations and emission estimates*. Atmospheric Chemistry and Physics.