

1 **Objections to some conventions in non-parametric analyzes of regional agricultural**  
2 **production.**

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4 **Abstract**

5 Nonparametric analyzes of regional agricultural production is frequently motivated by sustainability  
6 goals. In theory, an efficient allocation of production inputs and increased production outputs induced  
7 by innovations and technical progress could allow to save on scarce natural resources while  
8 simultaneously expanding the provision of food and fiber. Policy recommendations derived from two-  
9 stage analyzes thus confidently advise policy makers and farmers to modernize, specialize or scale up  
10 to counteract technical inefficiency. In this paper two major objections are presented to these  
11 conventions within the agricultural economics literature. First, we show that when spatially differing  
12 climatic conditions are sufficiently considered in two-stage analyzes, conventional policy  
13 recommendations are not valid anymore. Second, we argue that from a production-theoretic point of  
14 view, the traditionally employed technical efficiency model fails in providing information on  
15 sustainability of agricultural production. We thus suggest to conceptually decompose technical  
16 efficiency into an operational and a physical efficiency measure. For the period 2004 to 2018, we find a  
17 stagnating trend in physical productivity in the agricultural sectors of 122 European regions. In  
18 conjunction with the subordinate role of contextual to environmental determinants of inefficiency we  
19 propose to neither motivate studies with sustainability goals by default nor derive policy  
20 recommendations whenever the impact of environmental factors is not sufficiently considered.

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22 **Keywords:** technical efficiency, regional analysis, DEA, Malmquist-productivity index, environmental  
23 factors, nonparametric analysis, Tobit regression, panel data, sustainability

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25 **JEL-Codes:** D24, Q15, R15

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26 **1 Introduction**

27 Just recently, Hansson, Manevska-Tasevka and Asmild (2020) have raised an important question  
28 regarding the interpretation of inefficiency obtained in non-parametric analyzes. What if the decision-  
29 makers chose to conduct their farming business (at least to some degree) inefficiently? What if they  
30 acted rationally and based their decisions on considerations remote to the agricultural economist such  
31 as a preference for high animal welfare or other extensive practices? The authors convincingly argue  
32 that the contribution of studies that provide policy recommendations in order to nudge inefficient  
33 farmers to catch-up with sample peers is limited whenever the rational choice of the decision-maker is  
34 not sufficiently considered.

35 In this paper we would like to build on the authors' rationale by posing a different question. What if the  
36 decision-maker is not capable of choosing between conducting his farming business more or less  
37 productive? What if the varying degrees of inefficiency found in non-parametric analyzes are  
38 determined by spatially differing factors outside of the sphere of influence of both policy and decision-  
39 makers? In such cases, policy recommendations would not only miss out on acknowledging rational  
40 production decisions but potentially even harm farmers by erroneously urging them to invest in what  
41 is referred to in the literature as better allocation of production inputs (Toma et al. 2017) by means of  
42 specialization (Galluzzo 2022), technological modernization (Nowak, Kijek and Domańska 2015), or  
43 operating on optimal scale (Galluzzo 2013).

44 One might object that studies have hardly ever discussed factors that are determinate in the sense of  
45 being neither controlled by policy- and decision makers as explanatory factors of inefficiency. Indeed,  
46 the majority of studies in the literature is dedicated towards examining the effect of regionally differing  
47 sectoral characteristics such as size, specialization, or subsidies, which are of course subject to and  
48 manipulated by farmers or agricultural policies. Given the growing importance of studies on  
49 environmental efficiency or motivating efficiency analyses with sustainability goals, the neglect of  
50 determinate i.e., climate related factors, as a potential driver of (in-)efficiency comes as a surprise.  
51 Apart from some notable exceptions (, which will be addressed in the upcoming literature review  
52 section) few authors acknowledge the role environmental features play in explaining inefficiency  
53 variation and the consequences this might bear for studies' policy implications.

54 Following this line of thought, we'd further like to critically discuss the idea perpetuated in the  
55 literature that non-parametric efficiency and productivity analyzes are suitable tools in assessing the  
56 sustainability of (regional) agricultural production. A considerable amount of studies motivate  
57 conducting technical efficiency analysis with sustainability goals, e.g., pointing at 'the potential for  
58 increasing agricultural production in the EU, balancing environmental resource savings with economic  
59 return. (Toma et al. 2017: 140)' or the need for 'growth in agricultural productivity and a more efficient  
60 way of utilizing limited inputs [...] [if] output is to keep up with the increasing demand for food and  
61 raw materials (von Hobe, Michels and Musshoff 2021: 2)'. In theory, rising productivity figures should  
62 reflect an improved feasibility in expansion of production possibilities, either induced by advanced  
63 technology or skills. The latter in turn are supposed to enable producers to increase (or maintain)

64 agricultural produce output, utilizing constant (or less) resource input quantities. Arguably though,  
65 findings of most productivity analyses may allow to support this motivation only to a very limited  
66 extent, because the technical efficiency model conventionally employed, contains only limited  
67 information on actual physical produce and resources. We thus suggest decomposing the latter into an  
68 efficiency model based on physical production factors and an efficiency model built on an operational  
69 input-output set.

70 Empirical results for crop and mixed farms of 122 EU regions in the period 2004 to 2018 show that  
71 climatic conditions i.e., radiation, temperature and precipitation levels are statistically and  
72 economically significant in explaining efficiency variation. Given all other model parameters remain  
73 constant, we find that an increase in mean regional temperature of one degree Celsius already accounts  
74 for 1.5 % of (input-oriented technical) inefficiency variation. The results for the 'operational' and  
75 'physical' model efficiency affirm the claim that agricultural production efficiency substantially  
76 depends on neglected determinate factors. For the former, environmental and usually considered  
77 sectorial features e.g., economic size or intensity of practices, are found to determine a decision-makers  
78 degree of inefficiency. For the latter in turn, regional sectoral characteristics seem to play a subordinate  
79 role and inefficiency variation can mostly be attributed to spatially differing climatic conditions. In case,  
80 the latter are not sufficiently accounted for in efficiency analyses, inefficiency might be wrongfully  
81 attributed to decision-makers and policy recommendations misleading.

82 Findings of the productivity analysis reveal that the claim of future increases in (technical) productivity,  
83 contributing towards a harmonization of saving on natural resources while expanding provision of food  
84 and fiber, is questionable at least. Although our findings do suggest an increase in technical  
85 productivity, productivity for our physical efficiency measure is stagnating, suggesting that further  
86 expansion of agricultural produce in accordance with environmentally sound production conditions,  
87 might be overestimated. As a consequence, motivating technical efficiency and productivity analyses  
88 with sustainability goals by default seems inadmissible.

89 The remainder of the paper is organized as follows. The literature review in section 2 provides proof  
90 that the conventions lined out above exist and discusses why they are problematic above all in the  
91 context of regional agricultural production. In section 3, the theoretical framework for the empirical  
92 application case and the conceptual decomposition of technical efficiency and is introduced. In section  
93 4, results of the efficiency, (Malmquist-) productivity and second stage random effects Tobit panel  
94 regression analysis are discussed. The paper closes with concluding remarks in section 5.

95

96 **2 Literature Review**

97 Of course, not all studies on agricultural production efficiency and productivity employing  
98 nonparametric methods are affected by the issue outlined above. Whether or not the neglect of  
99 environmental factors leads to deterred policy implications depends on a variety of factors, above all  
100 the scope of the analysis and how its results are interpreted.

101 In the agricultural economics literature, the scope of studies varies significantly. Roughly, they may be  
102 divided in analyzes of efficiency (mostly) using cross-sectional data on the one hand and analyzes of  
103 productivity based on panel data on the other. Some works focus on specific farm types, e.g., dairy, crop  
104 or mixed farms and are conducted either on farm-level, regional, country or even global scale. Clearly,  
105 not all frameworks are equally vulnerable to the influence of determinate factors such as climatic  
106 conditions. In farm-level analyses of dairy farms for example, ecological features are expected to have  
107 a less pronounced effect on inefficiency variation when compared to productivity estimates of arable  
108 farms in a global scale setting. The criticism outlined in the introduction thus concerns studies to a  
109 different degree and above all applies to analyzes conducted at least on a regional level.<sup>1</sup>

110 And even in studies examining efficiency on regional or even broader scope, the issue does not  
111 necessarily have to arise. An example for a concise and sound country-level analysis is provided by  
112 Coelli and Rao (2005), in which agricultural total factor productivity of 93 countries is examined by  
113 employing the (nonparametric) Malmquist Productivity Index. The authors argue that their findings  
114 are mainly of interest because they show a reversal in the productivity trend reported by previous  
115 studies. They further argue that future research should consider land quality, irrigation, and rainfall  
116 levels to allow for a more meaningful interpretation of the differences that exist between the countries'  
117 efficiency numbers. The conclusions drawn by the authors are thus exclusively based on a relative  
118 comparison with other studies, make no judgments on why decision-makers might be inefficient and  
119 neither provide policy recommendations on how to enhance productivity levels.

120 The latter is of course legitimate whenever environmental factors are explicitly and sufficiently  
121 accounted for within the methodological framework. Chambers, Hailu and Quiggin (2011) proposed a  
122 methodology to account for event-specific uncertainty in agricultural production. They showed how  
123 Data Envelopment Analysis (DEA) can be adapted to consider stochastic elements in a state-contingent  
124 setting. Their findings suggest that different quantities of rainfall influence agricultural efficiency  
125 estimates. A similar approach was pursued by Gadanakis and Areal (2020), who derived the efficiency  
126 scores based on sub-vector DEA to ensure that only farms with homogenous environmental conditions  
127 were compared. In another article, Chambers, Pieralli and Sheng (2020) incorporated climatic variates  
128 directly into the productivity accounting framework and decomposed the productivity growth  
129 measured (among others) into a technological change and a weather-related change component. Their

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<sup>1</sup> One should note though, that an impact of environmental variables on efficiency cannot be ruled out completely in agricultural production contexts. Schmitt et al. (2022) showed that extreme weather events caused significant crop yield losses at farm level, which suggests that environmental factors might even affect inefficiency distributions in farm-level analysis.

130 results suggest that the observed slowdown in Australian agricultural productivity growth is not  
131 attributable to a slowdown in technological change but much rather induced by weather-related events.  
132 Chambers and Pieralli (2020) confirm the importance of climatic features by applying the method to  
133 the case of US agricultural production.

134 Given that some studies are not affected due to a specific scope or a careful interpretation of the results  
135 and other analyzes explicitly account for the effect of environmental factors, one might question the  
136 relevance of the issue outlined in the introduction section. Even though the cases introduced here exist,  
137 they are by no means the norm. Let's move from the exception to the rule.

138 Instead of applying a methodology as described above, the two-stage analysis is the most popular  
139 approach to determine efficiency of decision-makers and explanatory factors of inefficiency. The two-  
140 stage approach comprises calculating DEA estimates in a first step, before regressing on the yielded  
141 efficiency estimates in a censored or truncated regression model in the second stage. In the latter, the  
142 effect of contextual variables (within the sphere of influence of the decision-maker) is considered. In  
143 context of agricultural production these variables include but are not limited to e.g., size, specialization,  
144 and subsidies. A direct incorporation of climatic variates into the efficiency framework (of the first  
145 stage) as in the example of Chambers, Pieralli and Sheng (2020) is not intended. Interestingly, the issue  
146 equally arises in eco- or environmental efficiency analyses (e.g., Baležentis et al. 2020; Grassauer et al.  
147 2021; Yang, Wang and Bin 2022), which consider not climatic conditions but environmentally  
148 undesirable outputs, e.g., nutrient surpluses, within their efficiency model. When efficiency estimates  
149 reflect results on the latter, they are presumably even more sensitive to the impact of the climatic  
150 conditions with which they interact.

151 While a few studies employing the two-stage approach consider environmental factors in the second  
152 stage of the analysis, there is no discussion of the consequences this might bear for policy implications  
153 (e.g., Heidenreich et al. 2022). In fact, in one particular case, soil quality is found to have a significant  
154 impact on inefficiency (, whereas the effect of other considered covariates is unclear), yet authors  
155 formulate mantra-like calls for investments in modernization to enable technological progress (Nowak,  
156 Kijek and Domańska 2015). In addition, there are plenty of examples, where studies ignore potential  
157 impact of environmental factors, yet suggest more or less concrete policy measures, such as enhancing  
158 farmers' knowledge and managerial skills (Todorović et al. 2020), correction of scale and improvement  
159 of technology (Błażejczyk-Majka, Kala and Maciejewski 2012), learning processes and imitation of  
160 technologies (Baráth and Fertő 2017), removing misallocation of resources by investing in agricultural  
161 extension systems (Bagchi, Rahman and Shunbo 2019), agricultural innovation (He, Li and Cui 2021).

162 In some of the above cases (e.g., Galluzzo 2013, Galluzzo 2022; Nowak, Kijek and Domańska 2015) these  
163 recommendations are not based on statistical and economic significance of sectoral characteristics.  
164 Much rather it seems to be an accepted convention to provide some general economic advice on how  
165 to enhance productivity. We do not mean to propose that none of the inefficiency found in these  
166 analyses cannot reasonably be targeted by such measures. Also, one might be tempted to say that  
167 modernizing farm equipment, acquiring new skills or adopting best practices should not be harmful

168 either way. Nonetheless, we would argue that this is not well thought out. The above-mentioned policy  
169 recommendations require for substantial investments in either machinery, skills or time. But spendings  
170 on machinery for example, will limit decision- and policymakers' future scope of action and might be  
171 unjustified whenever inefficiency is due to climatic conditions outside of the sphere of influence or due  
172 to farmers' conscious production choices (Hansson, Manevska-Tasevka and Asmild 2020).

173 Even though the effect of differing climatic conditions on the efficiency estimates is largely ignored,  
174 'environment' and 'sustainability' are popular keywords to motivate nonparametric technical efficiency  
175 analysis. This is not limited to studies dedicated to eco- or environmental efficiency (e.g., He, Li and Cui  
176 2021), but just as much includes traditional technical efficiency analyzes (e.g., Toma et al. 2017; von  
177 Hobe, Michels and Musshoff 2021). The latter are motivated by the prospect of learning about the  
178 harmonization of saving on scarce natural resources (inputs) on the one hand and satisfying the  
179 growing demand for food and fiber (outputs) on the other. From a conceptual point of view though, this  
180 rationale makes sense only if the technical efficiency estimate contains information on scarce natural  
181 resources and the provision of food and fiber. In the majority of the studies discussed above though,  
182 the technical efficiency model has been calculated employing land, labor, capital and often intermediate  
183 consumption as inputs, while farm gross output or another form of operational output serves as output.  
184 While in the input-oriented case, technical efficiency estimates might thus indeed to some extent reveal  
185 potential in savings on quantities of land, fertilizer, pesticides or energy, in the output-oriented case,  
186 they may above all reflect farms' or sectors' economic returns.

187 Partly, this convention could be explained by agricultural economists' interest in good comparability of  
188 studies in different empirical application cases or with previous analyses. Also, when analyses are  
189 conducted for cases that might only be of interest to a small, specialized part of the scientific  
190 community, agricultural economists might be interested in aligning their conceptual and  
191 methodological approach with acknowledged and frequently employed approaches. This seems likely  
192 given that the profound methodological advances in nonparametric analysis are in context of  
193 agricultural production only scarcely adopted thus far.<sup>2</sup> Regardless of the causes of the conventions  
194 lined out in this section, inadequate policy recommendations or erroneously motivating nonparametric  
195 analysis with sustainability goals should in any case be avoided. In this paper, we would like to  
196 contribute towards this goal by comparing the effect of regionally differing, determinate climatic  
197 conditions to conventionally employed contextual variables and proposing a conceptual alternative to  
198 the traditionally employed technical efficiency model with the approach introduced in the upcoming  
199 section.

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<sup>2</sup> Substantial methodological advances have been made in the nonparametric methodology. Bădin et al. (2014) for example introduced a nonparametric conditional methodology, where a flexible location scale model is employed to regress the ratio of conditional to unconditional measure on external factors. Even though the methodology allows for the calculation of a pure managerial efficiency measure ( $\theta$ , the residual of efficiency variation not attributable to external factors) thus far only two studies adopted the methodology in an agricultural production context. The study of Minviel and De Witte (2017) is the only analysis employing the methodology to agricultural efficiency in particular. (They did not consider environmental factors though, which is reasonable given their farm level scope.)

### 201 **3 Methodology**

#### 202 *3.1 Conceptual Model Decomposition and Hypotheses*

203 Building on the remarks made in the literature review, the traditional technical efficiency model might  
204 in the input-oriented case indeed contain relevant information on the potential of resource savings. In  
205 the output-oriented case though, information on expansion of physical produce might be quite limited,  
206 given that conventionally an operational measure like farm gross results are employed as output  
207 variable. Further, a lot of the policy recommendations drawn by agricultural economists are directed  
208 at evaluating and enhancing efficiency caused by rather operational choices of decision-makers. We  
209 therefore suggest to conceptually decompose the technical efficiency model into two components. First,  
210 an (input-oriented) operational model containing all relevant cost variables linked to production  
211 inputs, which allows to make a judgment on the efficiency of input allocation. Building on an operational  
212 efficiency measure, policy recommendations like modernization and specialization might be justified  
213 and more targeted. Second, an (output-oriented) physical efficiency model, where the farm gross  
214 results are substituted by actual produce that contains all the information necessary for a making the  
215 judgment on harmonization of resource conservation and provision of food and fiber.

216 Since our criticism concerns the neglect of the impact of climatic conditions on efficiency estimates  
217 of the traditionally employed technical efficiency, the two introduced models will be compared to input-  
218 and output oriented (conventional) technical efficiency estimates. In a second step, we imitate the most  
219 frequently performed approach in the literature and incorporate a set of covariates representing  
220 sectoral characteristics into a second stage regression analysis. Of course, in our case we will also  
221 consider a set of environmental variables associated with crop yield variability, which we presume  
222 might translate to technical and physical efficiency of decision-makers. In case, we obtain a  
223 straightforward impact of environmental factors on technical efficiency estimates, the assumption H1a  
224 many studies implicitly build on will be rejected.

225 H1a): Environmental factors do not have a statistically or economically significant impact on  
226 technical efficiency estimates.

227 Since our criticism included the prospect that a neglect of environmental factors could also lead to  
228 seriously misleading policy recommendations by wrongly attributing inefficiency to inefficient input-  
229 allocation, sectoral characteristics usually considered in the literature should play an economically  
230 subordinate role to environmental variables when explaining technical inefficiency. In this case, H1b  
231 needs to be rejected:

232 H1b): Robustness of the statistical and economic significance of sectoral characteristics is not  
233 diminished by the inclusion of environmental variables as explanatory factors.

234 Second, in order to test whether technical efficiency and productivity measures reveal future potential  
235 for a harmonization of resource conservation and provision of produce, the physical productivity  
236 measure needs to actually increase over the considered period and coincide with the technical  
237 productivity index results. In order to support our claim that this is not the case, H2 needs to be rejected.

238 H2): Physical productivity has increased over the considered period and follows a similar trend  
239 as technical productivity.

240

### 241 3.2 Two-stage approach

#### 242 Data Envelopment Analysis

243 In order to test hypotheses H1a and H1b, a two-stage approach is employed, which connects a radial  
244 Data Envelopment Analysis (DEA) model in the first step and a (censored) Tobit panel data regression  
245 model employing the yielded efficiency scores as dependent variable in the second step. Again, we are  
246 aware of e.g., the lack of a clear theory on the underlying data generating process when Tobit regression  
247 procedures are applied or that efficiency scores are not naturally independent observations but much  
248 rather serially correlated (Simar and Wilson 2007). Choosing a modified approach, building on an e.g.,  
249 order-m or order-alpha frontier analysis adopting the nonparametric conditional methodology would  
250 solve those issues.

251 Yet, the credibility of our line of thought depends on guaranteeing for a good comparability of our  
252 empirical results with the results yielded based on the conventions we criticized in the previous section.  
253 Adopting a modified and less frequently employed methodology might reasonably cast doubt on the  
254 transferability of our findings to the findings of other studies. Further, we would also like to encourage  
255 the replication of our approach in order to allow for future considerations of environmental factors that  
256 is easy to implement. Given that authors, like Bădin et al. (2014) or Chambers, Pieralli and Sheng  
257 (2020), already explored the path of modified methodologies, we choose to adopt the conventionally  
258 used two-stage framework.

259 Based on the pioneering work of Farrell (1957) on production efficiency assessment, Charnes, Cooper  
260 and Rhodes (1978) were the first to introduce a linear programming technique, which allows to  
261 calculate relative efficiency scores of decision-making units considering multiple inputs and outputs.  
262 The mathematical formulations below reflect a reduced version of the DEA under variable returns to  
263 scale assumption, as first introduced by Banker, Charnes and Cooper (1984). Here the output-based  
264 radial efficiency scores are calculated as Debreu-Farrell measure of efficiency (Debreu, 1951; Farrell,  
265 1957). Equation (1) denotes the production possibility set that describes the feasible technology T:

$$P(x) \equiv \{y : (x, y) \in T\} \tag{1}$$

266 of a specific production context in which all outputs  $y$  are producible by the inputs  $x$ . The upper  
267 boundary of the set defines the efficiency frontier, a convex hull that envelopes the empirically  
268 observed input-output ratios and is interpreted as the best-practice frontier of the sample. The distance  
269 of an individual DMU's output to the efficiency frontier (or its required proportional enlargement of  
270 output) determine a DMU's degree of technical inefficiency. The linear programming problem of the  
271 output-oriented DEA model corresponds to (Banker, Charnes and Cooper 1984):

$$\max \phi \tag{2}$$



$$s. t. \sum_{j=1}^n x_{ij} \lambda_j \leq x_{io} \quad i = 1, 2, \dots, m;$$

$$\sum_{j=1}^n y_{rj} \lambda_j \geq \phi y_{ro} \quad r = 1, 2, \dots, s;$$

$$\sum_{j=1}^n \lambda_j = 1$$

$$\lambda_j \geq 0$$

272 where the considered DMU<sub>o</sub> is one of n decision making units in the sample, for which the efficiency  
 273 in transforming a set of m inputs into s outputs is evaluated. The empirically observed input and output  
 274 quantities of DMU<sub>o</sub> are expressed by the vectors  $x_{io}$  and  $y_{ro}$  respectively.  $\lambda$  denotes the DMU's weight  
 275 and  $\phi$  its efficiency score. The linear program for the output-oriented case under constant returns to  
 276 scale assumption coincides with equation (2) if the convexity constraint  $\sum_{j=1}^n \lambda_j = 1$ . is relaxed. The  
 277 relationship of efficiency measured under constant returns to scale with efficiency measured under  
 278 variable returns to scale reveals information on whether a decision-maker operates scale inefficient in  
 279 the sense of operating on a scale section where the feasible technology is more restricted and only  
 280 permits a lower level of productivity. The corresponding scale efficiency index can be calculated as  
 281  $SE(o) = \phi_{CRS}(o)/\phi_{VRS}(o)$  (Arru et al. 2019).

282

### 283 *Panel Tobit Regression Model*

284 In the second stage, the determinants of the yielded efficiency estimates are assessed conducting a  
 285 random effects panel data Tobit regression analysis. The yielded efficiency scores range in the interval  
 286 [0,1] (with 1 = efficient, < 1 inefficient) for the input-oriented case and 1 (efficient) and > 1 (inefficient)  
 287 for the output-oriented case. Employing a Tobit regression model to determine the relationship  
 288 between inefficiency variation, contextual and environmental variables is believed to partly account for  
 289 the input (output) -oriented efficiency measure being right (left) censored at 1, where the scores of the  
 290 efficient DMUs are concentrated. Acknowledging the more fundamental methodological critique  
 291 associated with two-stage analysis, this variant is expected to at least produce more meaningful results  
 292 as e.g., an OLS based regression. A reduced version of the random effects panel data Tobit model is  
 293 denoted by (Radovanov et al. 2020):

$$\phi_{it}^* = x'_{it} \beta + \varepsilon_{it}$$

$$\phi_{it} = 0 \text{ if } \phi_{it}^* \leq 0 \tag{3}$$

$$\phi_{it} = \phi_{it}^* \text{ if } \phi_{it}^* \geq 0$$

294 where  $y_{it}$  is the dependent variable measured by  $y_{it}^*$  it as the latent dependent variable of the efficiency  
 295 estimate according to efficiency model for positive values, otherwise censored, corresponding to region

296 i and period t. The vector of independent covariates is denoted as  $x'_{it}$  with  $\beta$  being the coefficient vector  
 297 and  $\epsilon_{it}$  the error term, which is expected to be independently and normally distributed.

298

### 299 3.3 *Malmquist-productivity index*

300 Ideally, the validity of the conceptual decomposition of the efficiency model could be proven by  
 301 employing the Malmquist-productivity index. In case, the technical productivity trend can be  
 302 interpreted as product of the operational and physical productivity trend, future analyzes could simply  
 303 incorporate the two proposed model set-ups to validate the implications of the technical efficiency  
 304 model within their framework. This would allow for more refined policy implications allowing for a  
 305 precise targeting of operational inefficiencies and productivity losses with some of the above criticized  
 306 policy recommendations.

307 The Malmquist-productivity index (MPI) introduced by Caves et al. (1982) is an acknowledged method  
 308 to account for trends in productivity when non-parametric methods are employed. The index values  
 309 are calculated analogously to the DEA method based on distance functions, yet the decision-makers  
 310 input-output combinations are not simply projected against the frontier of one period, but also against  
 311 the production possibility frontier of a different base period. The Malmquist-Productivity Index thus  
 312 accounts for the distance of inefficient decision-makers' input-output set to the production possibility  
 313 frontier of a certain period t+1, relates this to the mean distance of DMUs to the production possibility  
 314 frontier of a previous period t as well as relating the level of the production possibility frontier in t+1  
 315 to the one in t.

316 Based on an input vector  $x^t = \{x_1^t, x_2^t, \dots, x_m^t\}$ , and an output vector  $y^t = \{y_1^t, y_2^t, \dots, y_n^t\}$ , given the  
 317 production possibility set  $P^t = \{x^t, y^t\}$ , the geometric mean of the Malmquist-Productivity Index for t  
 318 and t+1 corresponds to (Grifell-Tatjé and Lovell, 1994):

$$MP_t^{t+1} = \left[ \frac{D_0^t(x^{t+1}, y^{t+1})D_0^{t+1}(x^{t+1}, y^{t+1})}{D_0^t(x^t, y^t)D_0^{t+1}(x^t, y^t)} \right]^{\frac{1}{2}} \quad (4)$$

319 The index equals 1, if productivity remains constant. Values larger (smaller) than one indicate  
 320 increasing (decreasing) overall productivity. Färe et al. (1994) further proposed to decompose the MPI  
 321 into the technological and efficiency change component. The technological change measures the  
 322 'frontier-shift' and thus reveals differences in maximum feasible productivity over the considered time  
 323 period. Values above one are believed to reflect positive technological development. For period t and  
 324 t+1 it is defined as:

$$MPTECH_t^{t+1} = \left[ \frac{D_0^t(x^{t+1}, y^{t+1})D_0^t(x^t, y^t)}{D_0^{t+1}(x^{t+1}, y^{t+1})D_0^{t+1}(x^t, y^t)} \right]^{\frac{1}{2}} \quad (5)$$

325 The efficiency change component in turn reflects how on average the distance of inefficient DMUs to  
 326 the frontier develops. Values above one thus reveal the degree to which decision-makers are able to  
 327 'catch-up' to the most productive observations in the sample. For period t and t+1 it is denoted as:

$$MPEFFCH_t^{t+1} = \left[ \frac{D_0^t(x^{t+1}, y^{t+1})}{D_0^t(x^t, y^t)} \right]^{\frac{1}{2}} \quad (6)$$

328 For further details on the methodology of the Malmquist-Productivity Index see Caves et al. (1982),  
329 Färe et al. (1994) and Grifell-Tatjé and Lovell (1994).

330

## 331 **4. Data**

### 332 *4.1. Efficiency model data*

#### 333 *Technical efficiency*

334 For the outlined approach, availability of data is crucial. For one, the conceptual decomposition of the  
335 traditional technical efficiency measure is only possible if data not only on conventionally employed  
336 inputs and outputs is available, but also data on input costs and explanatory factors. Further, the  
337 empirical application case should equally permit the integration of environmental data. In conjunction  
338 with the broad interest of agricultural economists in production efficiency, productivity and its  
339 determinants in the European Union, the EU's farming sector seems suitable as empirical application  
340 case.

341 Agricultural production data stems from the farm accountancy data network (FADN) database (2022)  
342 of the years 2004 to 2018. Farming sectors' representation of 122 regions (according to the FADN  
343 classification) classified as fieldcrops and mixed production farms are used. As outlined in the literature  
344 review, vulnerability of livestock specialists to climatic conditions might be limited and consequently  
345 they have not been taken up into the sample.

346 Technical efficiency (for both the input- and output-oriented case) will be computed with the  
347 (conventionally used) inputs land represented by the total utilized agricultural area (UAA) in hectare  
348 (SE025<sup>3</sup>), labor given as total labor input expressed in full time person working equivalents (SE010),  
349 capital as [€] value of the closing evaluation of total assets (SE436) and finally the intermediate  
350 consumption [in €] accounting for production specific costs such as seeds and seedlings, fertilizers,  
351 feed, other crop protection as well as overheads (SE275). The total output [€] (SE131), which denotes  
352 the monetary value of output of crops and crop products, livestock, and livestock products and of other  
353 input, including other gainful activities (OGA) of the farms, serves as the output of the technical  
354 efficiency model.

355

#### 356 *Operational efficiency*

357 In order to decompose the traditional technical efficiency measure, the (input-oriented) operational  
358 efficiency will also be calculated with the total output as output and the intermediate consumption,  
359 which represents direct costs of production. The remaining inputs of the operational efficiency measure

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<sup>3</sup> Reference number in FADN database. Detailed information on standard variables in the FADN database may be found here: <https://agridata.ec.europa.eu/extensions/FADNPublicDatabase/FADNPublicDatabase.html>.

360 are included as the production costs tied to the classical inputs of technical efficiency.<sup>4</sup> The total labor  
361 input is thus substituted by the sum of wages paid (SE370) and spendings on contract (SE350) and  
362 contractual work (SE720). This includes wages, security charges (and insurance) of wage earners, as  
363 well as costs linked to work carried out by contractors. As equivalent to the land input serves the  
364 monetary value linked to maintaining and improving agricultural land (e.g., fencing, drainage and fixed  
365 irrigation equipment) (SE447). Finally, the capital input is substituted by capital costs, which we  
366 calculated as the sum of depreciation (SE360), balance of interest paid and received (SE381), balance  
367 of subsidies and taxes on investment (SE405) and net investment on fixed assets (SE521). We carefully  
368 considered dependencies of all variables to rule out potential redundancies.

369 Note that for a variety of regions, subsidies and interest received, result in negative aggregate capital  
370 costs, forcing us to exclude a considerable amount of observations from the sample (, since  
371 nonparametric analyzes do only allow for a consideration of positive integer numbers). The integration  
372 of the capital costs thus led to a reduction of sample size from 1,997 to 1,646 observations. This could  
373 potentially cause operational efficiency estimates to be biased, either positively because regions  
374 receiving high absolute amounts of subsidies could conduct business less intensive or inefficient, or  
375 negatively because higher amounts of interests received could signal a high long-term operational  
376 efficiency or simply benefits due to profitable investments in the past.

377

### 378 *Physical efficiency*

379 The second measure we are proposing as a supplement to the traditional technical efficiency model, is  
380 the physical efficiency model. In contrast to the operational efficiency measure, here in the (output-  
381 oriented case) the inputs of the technical efficiency model are taken over, while the total output will be  
382 substituted by physical outputs that contain the information that may allow to evaluate if actual  
383 produce is indeed expanded. Overall, three different physical outputs, wheat (SE110\*SE025), maize  
384 (SE115\*SE025) and milk (SE125\*SE085) produce, which can be seen as proxy outputs for the  
385 production technologies of the crop specialists and mixed farming sectors in the EU, are considered. All  
386 three variables are given in absolute amounts in kilogram. Given the already high number of four inputs,  
387 limiting the output variables to three seems rational, to keep the share of efficient DMUs following an  
388 enlarged production set moderate.

389 Analogously to the operational efficiency model, the number of observations is considerably lower than  
390 for its technical efficiency counterpart, since data availability for actual produce is not available for all  
391 regions or at any point in time. In total, for the efficiency measure, sample size drops from 1,997 to  
392 1,195 observations. Since availability of produce data also differed for individual regions within the  
393 time frame considered, the calculation of the Malmquist-Productivity index (, which requires data to be

---

<sup>4</sup> Note that in data envelopment analysis, the technical efficiency measure may also be decomposed methodologically into a cost and allocative efficiency measure if input quantities and prices are fully available. This approach is not adopted here since i.e., the total output considered is not simply calculated as output quantities multiplied by their price. Also, quantity data is not available for all inputs (e.g., intermediate consumption).

394 available for each region of all inputs, outputs and years) is based on a panel of 876 observations, thus  
 395 posing the smallest sample size for any model within this paper. Similar to the operational efficiency  
 396 model, the physical efficiency measure could thus be (, supposedly positively) biased since actual  
 397 produce has been least consistently reported by eastern EU member countries. The latter have been  
 398 found to be rather technically inefficient when compared to western member states (e.g., Błażejczyk-  
 399 Majka, Kala and Maciejewski 2012; Kaiser and Schaffer 2022), which could cause structural differences  
 400 in between the model samples.

401 Note that a comparison of mean efficiency estimates between the different models calculated with  
 402 different data would in any case bear only very limited implications due to, e.g., differences in sample  
 403 size, the enlarged size of the production set and thus differing shares of efficient DMUs (Bravo-Ureta et  
 404 al. 2007; Minviel and Latruffe 2017). In line with our research issue, discussion of results will thus focus  
 405 on model differences regarding the individual productivity trends and the explanatory power of the  
 406 sectoral characteristics and environmental variables considered.

407 The presumed production dependency for the proposed models is supported by all inputs correlating  
 408 significantly and strongly positive with the respective outputs (see Appendix S1 and S2 for a table  
 409 showing correlations and significance levels). Descriptive statistics of the model inputs and outputs are  
 410 given in table 1.

411

Variable	Obs.	Mean	Std. dev.	Min	Max
UAA [ha]	1,812	83.40	113.22	1.78	790.61
Labor [TLU]	1,812	1.98	1.86	0.40	20.99
Intermediate Consumption [€]	1,812	82,154.80	120,890.70	2,412.00	964,507.00
Total assets [€]	1,812	512,376.30	591,530.70	15,860.00	3,401,421.00
Costs UAA [€]	1,812	245,032.00	391,472.30	1,604.00	2,828,859.00
Costs labor [€]	1,812	26,006.82	50,074.67	200.08	401,567.30
Capital costs [€]	1,812	22,626.35	34,381.33	-79.944.00	293,590.00
Gross Output [€]	1,812	127,844.70	175,541.10	5,689.00	1,498,796.00
Wheat yield [kg]	1,696	5,466.845	7,978.05	31.72	53,631.51
Maize yield [kg]	1,474	7,436.677	10,904.55	106.05	141,200.50
Milk produce [kg]	1,514	44,001.65	101,145.30	0.00	858,638.40

412 **Table 1.** Descriptive statistics of model inputs and outputs.

413

#### 414 4.1. Regression covariates data

##### 415 Sectoral characteristics

416 In the literature, most contextual variables either refer to size, specialization, diversification, intensity  
 417 or extensivity of practices and of course subsidization. A variety of authors assumes size to be beneficial  
 418 for farms' efficiency due to increasing returns to scale (Forleo et al. 2021). Galluzzo (2016) argues for  
 419 example, employing FADN data of Italian farms, that especially small-sized family farms' technical  
 420 efficiency is low and largely dependent of subsidization. In order to incorporate the effect of size into  
 421 the second stage of the analysis, we consider the economic size of a holding expressed in 1,000 Euro of  
 422 standard output (SE005).

423 In our sample, crop specialized, and mixed production farm types are considered. Especially in context  
424 of the physical efficiency model, specialization could be decisive for the relationship of the partial  
425 productivities of crop yields and milk produce. Nonetheless, given that only the two farm types with  
426 migrating production technologies are considered, it might be useful to consider a continuous variable  
427 that accounts for the degree of specialization rather than considering the two farm types as  
428 dichotomous covariate. The number of dairy cows, expressed in livestock units (SE085), comprising all  
429 female bovine animals (including female buffaloes), which are held principally for milk production, thus  
430 serve us as specialization covariate.

431 Forleo et al. (2021) convincingly argued that apart from being an important factor in securing profitable  
432 incomes of family farms, diversification also influences farmers' technical efficiency. In line with  
433 previous studies (e.g., Arru et al. 2019), we therefore include other gainful activities (OGA) in form of  
434 total OGA output (SE700), related to the holding created i.e., from processing of farm products, receipts  
435 from contract work, agritourism, production of renewable energy or forestry.

436 To account for the intensity or extensivity of practices respectively, fertilizer quantities and agricultural  
437 area out of production are considered. The amount of purchased fertilizers and soil improvers  
438 (excluding those used for forests) (SE295) are considered as a proxy for rather intensive farming,  
439 whereas more agricultural area withdrawn from production (SE074), due to compulsory agricultural  
440 policy measures and permanent grassland and meadows no longer used but maintained in good  
441 environmental condition, are expected to reflect rather extensive farming practices.

442 Finally, in line with the majority of technical efficiency analyzes in agricultural production contexts (e.g.,  
443 Minviel and De Witte 2017, Minviel and Latruffe 2017, Todorović et al. 2020), we consider the total  
444 subsidies on current operations linked to production (SE605), including subsidies on crops and  
445 livestock, total support for rural development, decoupled payments, as well as subsidies on  
446 intermediate consumption and external factors.

447

#### 448 *Environmental factors*

449 Although only scarcely addressed in agricultural efficiency analyses, the dependence of European crop  
450 yield variability from climatic conditions is well documented (Supit et al. 2010). In our framework four  
451 environmental factors, namely radiation, temperature, precipitation and wind speed are accounted for.  
452 Note that the effect of climatic conditions on actual crop yield variability is much more complex that  
453 may be considered here on an aggregate annual and regional level. In crop yield variability studies,  
454 climatic conditions are frequently modelled non-linearly for different crop types individually and  
455 according to seasonal and spatial variations (Palosuo et al. 2011). For all of the considered variables  
456 there is an optimal corridor of values, which is beneficial to crop growth. Nonetheless, for the context  
457 of European crops, some assumptions regarding the potential aggregate effects of the environmental  
458 factors on technical efficiency can be made based on crop yield variability studies.

459 In context of European crop production, Peltonen-Sainio et al. (2010) find a negative effect of high  
460 temperature and precipitation levels on crop yield productivity. Heavy rainfall for example, can cause

461 root rot or drowning of the crops. Hot and dry periods, especially in form of high maximum  
 462 temperatures in summer, cause reduction of the growth of shoots, root growth and are also associated  
 463 with lower wheat and maize yield productivity in European regions (Pirttioja et al. 2015; Zscheischler,  
 464 Orth and Seneviratne 2017). We thus expect precipitation (given as annual mean of rainfall [mm]) and  
 465 climate (represented by the mean annual temperature of each region [°C]) as unfavorable determinants  
 466 of inefficiency.

467 High values of global solar radiation are known to enhance photosynthesis, which is responsible for  
 468 sufficient accumulation of assimilates. Low levels of solar radiation lead to shortened grain filling  
 469 periods and an increased risk of lodging. Mean total global radiation (in KJ/m<sup>2</sup>) is thus expected to be  
 470 a positive determinant of a region's efficiency. (Guo et al. 2022)

471 While moderate wind speed alters the balance of hormones in crops and contributes to making carbon  
 472 dioxide available to plants, wind erosion can be quite harmful, causing loss of plant nutrients, organic  
 473 matter and changes in soil texture, which results in lower yield productivity. Mean wind speed [m/s] is  
 474 thus included as fourth (supposedly unfavorable) environmental variable in the analysis (Lyles 1975;  
 475 Fryrear 1985).

476 The four climatic variables are available as high-resolution point data derived from the Agri4Cast  
 477 Resources Portal (European Commission 2022) and were extracted using a shape layer with the FADN  
 478 classification of European regions. Finally, continuous annual means were calculated for all regions.<sup>5</sup>  
 479 Extraction, cutting, and field statistics were performed using QGIS 3.14.

480 Descriptive statistics of sectoral characteristics and environmental regression covariates are given in  
 481 table 2.

482

Variable	Obs.	Mean	Std. dev.	Min	Max
Global radiation [KJ/m <sup>2</sup> ]	1,812	12,772.13	2,676.96	7,130.48	21,764.89
Temperature [°C]	1,812	11.87	3.40	-0.44	20.70
Wind speed [m/s]	1,812	3.04	0.83	1.32	5.71
Precipitation [mm]	1,812	1.85	0.58	0.11	4.27
Total production subsidies [€]	1,812	27,678.51	39,264.17	14.00	290,500.00
Economic size [€]	1,812	115.59	163.50	5.20	1,369.00
Area out of production [ha]	1,812	3.72	5.86	0.00	67.40
OGA output [€]	1,812	4,147.23	15,624.19	0.00	199,317.00
Fertilizers purchased [€]	1,812	11,451.09	16,350.24	122.00	125,666.00
Nr. of dairy cows [LU]	1,812	4.81	11.34	0.00	103.52

483 **Table 2.** Descriptive statistics of regression covariates.

484

---

<sup>5</sup> Please note that the climatic conditions thus refer to the total area of each region and are not agricultural area specific. Hence, weather events occurring on non-agricultural areas also partly constitute the environmental variables.

485 **4 Empirical Results**

486 *4.1 Two-stage approach*

487 Descriptive statistics of the efficiency estimates for the different models are provided in table 3.

488

Variable	Orient.	Eff. model	Obs.	Mean	Std. dev.	Min	Max
<i>in_te_vrs</i>	input	technical	1,812	0.87	0.11	0.42	1
<i>in_te_se</i>				0.86	0.16	0.21	
<i>in_ope_vrs</i>		operational	1,646	0.86	0.17	0.22	1
<i>in_ope_se</i>				0.81	0.20	0.17	
<i>oo_te_vrs</i>	output	technical	1,812	1.28	0.37	1	4.67
<i>oo_te_se</i>				1.13	0.29		4.83
<i>oo_phy_vrs</i>		physical	1,195	1.12	0.20	1	2.49
<i>oo_phy_se</i>				1.11	0.23		3.15

489

490 **Table 3.** Descriptive statistics of input- and output-oriented technical, operational and physical efficiency model  
 491 estimates under variable returns to scale assumption (vrs), as well as scale efficiency estimates (se).

492 Looking at the input-oriented models, operational (scale) efficiency is found to be lower than technical  
 493 efficiency. Analogously, for the output-oriented models, the EU farming sectors are less physically  
 494 (scale) than technically (scale) efficient. For the different models, estimates of the Tobit regression  
 495 analysis are given in table 4. First of all, we find the environmental factors radiation, temperature and  
 496 precipitation to have a statistically and economically significant impact on the physical, the input-  
 497 oriented and output-oriented technical efficiency models. Signs of covariates are consistent over all  
 498 three models<sup>6</sup> and correspond to the expected effect based on the literature. Only exception is the  
 499 variable wind, which reveals inconsistent results, suggesting a positive effect on both technical  
 500 efficiency models, yet a negative impact on operational efficiency.

501 Also, wind speed is found to be statistically insignificant for the physical efficiency model. From a  
 502 conceptual point of view this does not seem plausible since physical efficiency should be most  
 503 vulnerable to all environmental factors. This suggests that the variable is quite sensitive to the model  
 504 set-up and leads us to the conclusion that its results should be interpreted carefully.

505 The latter means that as expected there is no or only a quite moderate effect of environmental variables  
 506 on operational efficiency. Indeed, our results suggest that operational efficiency largely depends on  
 507 contextual variables regularly considered in the literature. Apart from the agricultural area excluded  
 508 from production, all covariates are statistically significant. A higher number of dairy cows is found to  
 509 be beneficial for profitability (in our sample of crop specialists and mixed farms), while engaging in  
 510 other gainful activities and receiving more subsidization might signal that farmers either willingly  
 511 conduct their business more extensively or are inadvertently less input allocation efficient. Quite  
 512 surprisingly though, larger economic size and quantities of fertilizers have a negative impact on  
 513 operational efficiency.

---

<sup>6</sup> Please note that for all output-oriented models the sign of the effect has to be the opposite as for the input-oriented models since in the output-oriented case >1 denotes inefficiency, while in the input-oriented case 0 to < 1 denotes inefficiency.



**Table 4.** Panel Tobit regression analysis results for input- and output-oriented technical efficiency, input-oriented operational efficiency and output-oriented physical efficiency model under variable returns to scale assumption.

$\phi_{it}^{vrs}$	input-oriented		output-oriented	
	technical	operational	technical	physical
	(1)	(2)	(3)	(4)
Global radiation	2.18e-05*** (5.03e-06)	-1.36e-06 (6.28e-06)	-5.79e-05*** (1.78e-05)	-3.20e-05* (1.70e-05)
Temperature	-0.015*** (0.004)	0.005 (0.004)	0.041*** (0.013)	0.048*** (0.013)
Wind speed	0.035*** (0.009)	-0.034*** (0.011)	-0.115*** (0.032)	0.116 (0.032)
Precipitation	-0.020*** (0.007)	-0.004 (0.010)	0.058** (0.028)	0.070*** (0.025)
Economic size	9.32e-05 (7.08e-05)	-1.01e-04** (8.85e-05)	-8.64e-04*** (2.67e-04)	1.31e-04 (2.20e-04)
Area out of production	-0.004*** (0.001)	-7.72e-05 (0.001)	0.010*** (0.003)	0.001 (0.003)
Fertilizers purchased	-1.07e-06 (6.53e-07)	-1.92e-06*** (7.35e-07)	9.08e-07 (2.46e-06)	9.79e-08 (2.52e-06)
Nr. of dairy cows	0.003** (0.001)	0.006*** (0.001)	-0.003 (0.004)	-0.008** (0.004)
Total production subsidies	1.65e-07 (3.82e-07)	-1.53e-06*** (4.86e-07)	-1.70e-07 (1.42e-06)	-1.80e-06 (1.30e-06)
OGA output	2.73e-07 (2.49e-07)	-4.54e-07* (2.36e-07)	-9.33e-07 (9.73e-07)	7.74e-07 (8.43e-07)
constant	0.727*** (0.068)	1.011*** (0.078)	1.756*** (0.000)	0.707*** (0.237)
Log likelihood	947.93	708.80	-814.90	-267.58

514 Note: \*\*\*, \*\* and \* denote significance at 1%, 5% and 10% level.

515 Partly, this could be due to the calculation under variable returns to scale, which to some extent offsets  
516 size-related differences. Thus, the negative effect of fertilizers could be interpreted as such, that  
517 operational efficiency is lower for farms of relatively comparable size (, occupying the same scale  
518 section), when they use larger quantities of fertilizers. Potentially, the peers constituting the different  
519 scale sections are regions characterized by farms of comparably smaller economic size, which spend  
520 less on input quantities. Yet, the effect of economic size is found to be statistically significant in the  
521 operational and output-oriented technical efficiency model exclusively. Assuming its effect to be  
522 meaningful, it is limited to the models that are neither associated with the harmonization of resource  
523 savings nor provision of food and fiber.

524 Comparing the results of the operational with the input-oriented technical efficiency model, a few  
525 things should be noted. First of all, apart from the number of dairy cows and the share of land excluded  
526 from production, no variable representing sectoral characteristics is found to have a statistically  
527 significant effect on input-oriented technical efficiency when environmental factors are considered.  
528 The negative effect of land excluded from production seems plausible given that the efficiency measure  
529 is partly based on total utilized agricultural area. The higher the share of UAA excluded from  
530 production, the lower the partial productivity of the land employed. In accordance with the findings for  
531 operational efficiency, mixed productions farms' efficiency might benefit from a higher share of  
532 livestock. An effect of size, fertilization or subsidization on the other hand cannot be found.

533 For the output-oriented models we find similar results for the sectoral characteristics. While in the  
534 technical efficiency model economic size and agricultural land excluded from production have a  
535 statistically significant negative effect on efficiency, in the physical efficiency model the only non-  
536 environmental factor that is statistically significant is the number of dairy cows, which is supposed to  
537 contribute to milk produce productivity. Thus, the results of the physical efficiency model suggest that  
538 physical produce substantially depend on environmental factors outside of the sphere of influence of  
539 the decision-maker. Nonetheless, it should be critically noted that we would have expected agricultural  
540 area out of production to have a profound effect on physical efficiency. Especially since it was found to  
541 have a statistically significant effect in the other output-oriented model.

542 It stands out that the interpretation of the conventional covariates is not always straightforward due to  
543 their statistical significance and signs of effects changing across the considered models. On the contrary  
544 (except for the variable wind speed), the interpretation of the environmental variables' effects is quite  
545 straightforward. Indeed, their varying economic significance according to efficiency model is also  
546 reasonable. As expected, we find higher coefficients for environmental variables in the physical  
547 efficiency model than in the output-oriented technical efficiency model. In conjunction with the higher  
548 standard deviation and maximum value (0.37 and 4.67 compared to 0.20 and 2.49) we conclude that  
549 the economic significance of environmental factors is more pronounced for the physical than the  
550 technical efficiency measure.

551 Given the Farrell-Debreu measure of efficiency, the interpretation of the coefficients might be most  
552 graphic for the input-oriented technical efficiency. Given all other model parameters stay constant, a

553 change of one degree in mean temperature or one mm of precipitation could account for 1.5 or 2  
 554 percent of the efficiency estimate respectively. A change of global radiation of 1,000 KJ/m<sup>2</sup> would in  
 555 turn explain 2.2 percent of inefficiency. Given a mean efficiency of 0.87 and taking into account that in  
 556 the sample temperature ranges from 0.44 to 21 degrees Celsius (3.40 std. deviation), precipitation from  
 557 0.11 to 4.27 mm (0.58 std. deviation) and radiation from 7,130 to 21,764 (2,677 std. deviation), the  
 558 results suggest that environmental factors do not only have a statistically significant but also  
 559 economically significant effect on agricultural production efficiency.

560

561 *4.1 Malmquist productivity results*

562 Descriptive statistics for the Malmquist-productivity index results are provided in table 5.

563

Variable	Prod. model	Obs.	Mean	Std. dev.	Min	Max
<i>MP_te</i>	technical	1,456	1.10	0.21	0.50	2.39
<i>TECH_te</i>			1.07	0.17	0.67	1.88
<i>EFFCH_te</i>			1.03	0.17	0.41	1.92
<i>MP_ope</i>	operational	1,091	0.98	0.21	0.36	2.39
<i>TECH_ope</i>			0.93	0.17	0.47	2.44
<i>EFFCH_ope</i>			1.06	0.21	0.51	1.98
<i>MP_phy</i>	physical	742	0.92	0.14	0.52	1.95
<i>TECH_phy</i>			0.91	0.12	0.61	1.42
<i>EFFCH_phy</i>			1.01	0.11	0.58	1.90

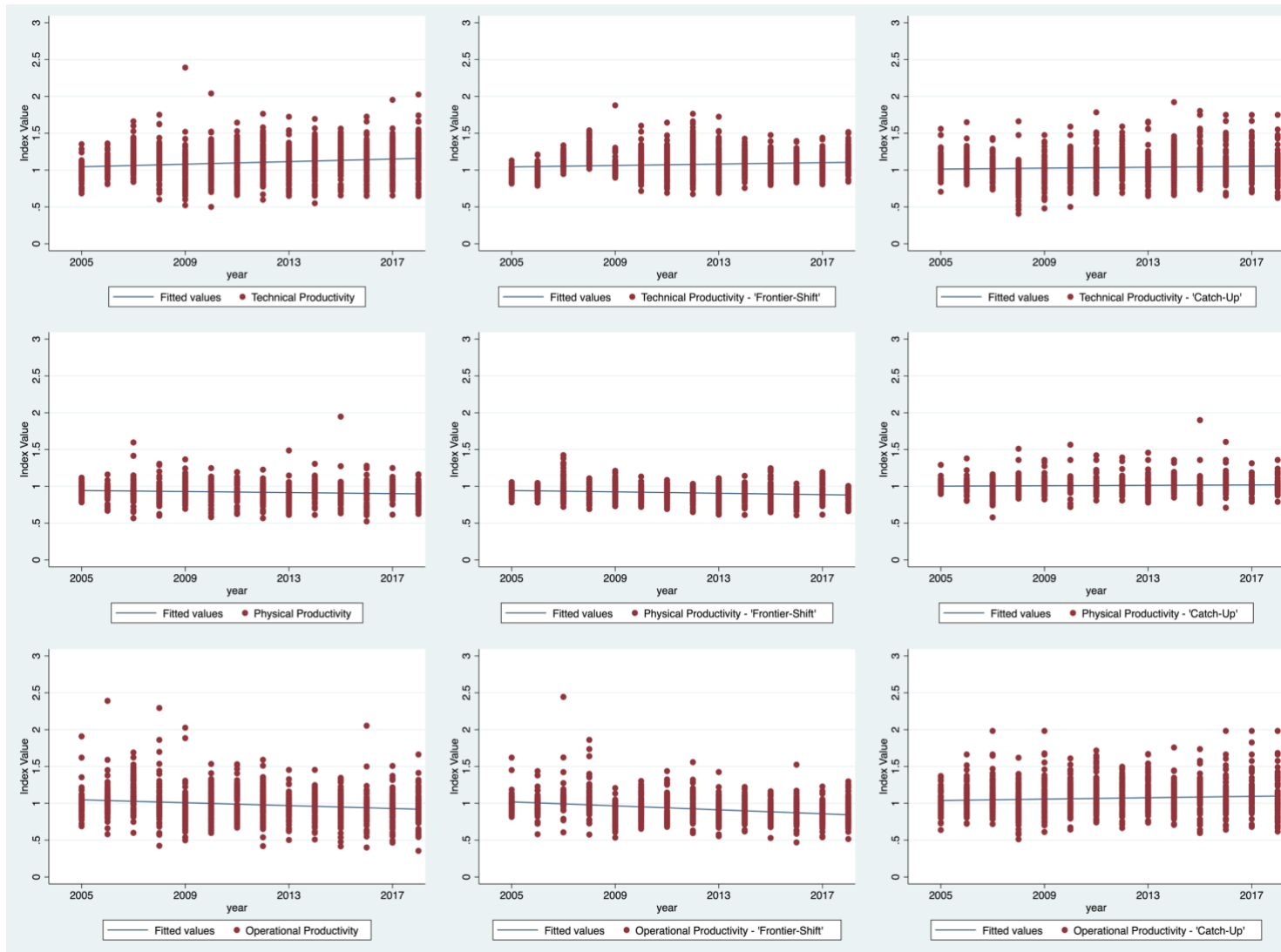
564 **Table 5.** Average Malmquist-productivity index (MP), technological (TECH) and efficiency change (EFFCH)  
 565 component value for technical, operational and physical productivity of the period 2005-2018 (base year =  
 566 2004).  
 567

568 The results of the Malmquist-productivity index support the findings of the efficiency analysis. Looking  
 569 at figure 1, we can obtain that the distribution of operational and technical productivity figures is quite  
 570 wide whereas the variation of physical productivity estimates is rather narrow.

571 This suggests that for operational productivity the potential for productivity gains is in principle high.  
 572 Nonetheless, over the considered period it has rather stagnated and on average sample peers have even  
 573 become about 7 percent less productive (negative technological change). The stagnating overall trend  
 574 in operational productivity thus stems from a substantial positive efficiency change effect, meaning that  
 575 less productive decision-makers have ‘caught up’ to the frontier, indicating a more efficient allocation  
 576 of production inputs.

577 In accordance with the findings for physical efficiency estimates, the range of physical productivity  
 578 values is narrow when compared to the other models. The decline in mean technological change to  
 579 about 0.91 suggests that substantial physical productivity gains due to induced technological change  
 580 are rather unlikely. Overall, physical productivity has on average decreased of about eight percent,  
 581 meaning that less productive regions have at least moderately caught up to sample peers.

582 **Figure 1.** Fitted and index values according to years for the Malmquist-productivity index, technological and efficiency change component



584 For our sample, technical productivity is the only model in which we obtain mean productivity gains of  
585 about 10 percent, driven by a significant frontier-shift of 7 percent and a moderate catch-up of 3  
586 percent. Interestingly, the results indicate that the idea of viewing the operational and physical  
587 productivity measure as decomposed parts of traditional technical productivity must be rejected. This  
588 could be due to the above-mentioned lower comparability of the indices caused by the substantially  
589 reduced sample size and thus potential biases.

590 In any case, the results clearly show that physical productivity has decreased and only reveals a low  
591 potential for future productivity gains. For the considerably reduced samples, we find that the trends  
592 in physical and operational productivity are negative over the considered period and counteract the  
593 productivity gains measured with the traditional technical efficiency model.

#### 594 4.2 Discussion

595 Our results only partly confirm the findings of previous studies assessing determinants of technical  
596 efficiency. While in the output-oriented case, economic size has a positive effect on efficiency, this  
597 cannot be confirmed for the input-oriented case. We find that our covariate representing extensivity is  
598 found to have a negative impact on efficiency. Indeed, and in contrast to findings of previous studies  
599 (e.g., Galluzzo 2018; Newman and Mathews 2007), we even find a negative effect of specialization (on  
600 crop farming) at least for the input-oriented case. Furthermore, the effect of covariates employed to  
601 account for diversification, intensive practices, and subsidies on the traditional technical efficiency  
602 model is unclear.

603 On the contrary, all four environmental variables employed have a statistically and economically  
604 significant effect on technical efficiency. Since the variable wind speed seems to be rather sensitive  
605 given the results of the decomposed efficiency models, we conclude that global solar radiation,  
606 temperature and precipitation are important determinants of technical efficiency. As a consequence,  
607 we argue that H1a and H1b can be rejected.

608 Regarding the implications of efficiency models for the harmonization of resource savings and  
609 expansions of food and fiber, the findings of the productivity analysis reveal a mixed picture. It could  
610 be shown that environmental factors have the most pronounced effect on the physical efficiency  
611 measure, while being least important for explaining operational efficiency. Yet, we could not provide  
612 evidence that the technical productivity measure can simply be decomposed into an operational and  
613 physical model of productivity. Indeed, the product of trends in operational and physical productivity  
614 do not coincide with the trend in technical productivity. Even though the comparability of the models  
615 might thus be limited, the physical productivity trend is actually decreasing for the EU's regional  
616 agricultural production and period of 2004 to 2018. The latter clearly suggests that future enlargement  
617 of produce while simultaneously reducing resource input might be overestimated and in any case needs  
618 to be accounted for explicitly, whenever studies motivate technical efficiency or productivity analyses  
619 by sustainability goals. Hypothesis H2 can thus also be rejected.

620 As already pointed out, one major drawback of our analysis might be the differing data sets according  
621 to each model, which followed from excluding observations that were neither available for a specific  
622 region, inconsistently over time or in case of operational productivity incompatible with the Malmquist-  
623 productivity index method. The resulting trade-off, to either further limit sample size in the  
624 productivity analysis for all three models or to lessen comparability of the results should be critically  
625 noted and might partially explain why the productivity analysis does not support the idea of the  
626 conceptual decomposition. Another drawback that was mentioned above is the choice of the  
627 methodology, for which a variety of limitations are well-documented (see 2.). While we are confident  
628 that environmental factors indeed play a vital role in explaining inefficiency variation and that they are  
629 not subordinate to previously considered contextual variables, the validity of our remarks on the  
630 economic significance (and its precise extent) of individual covariates might indeed be impaired by the  
631 method's limitations.

632

## 633 **5 Concluding remarks**

634 Based on conventions within nonparametric regional agricultural production efficiency and  
635 productivity analyses, two research issues were examined. First, we questioned the validity of regularly  
636 formulated (, rather operational) policy recommendations such as e.g., modernization, specialization  
637 and acquiring managerial skills, to reduce inefficiency whenever environmental factors are not  
638 properly accounted for in the analysis. Our findings clearly indicate that in analyses with a regional  
639 scope, environmental factors are decisive in explaining inefficiency variation. This could be shown for  
640 the frequently assessed case of EU agricultural production, employing the most popular nonparametric  
641 framework. In addition, our results suggest that the effect of regularly considered contextual covariates  
642 used to motivate the above-mentioned policy recommendations is subordinate to the effect of  
643 regionally differing determinate factors. Whenever determinate factors, such as environmental  
644 conditions might be relevant due to a regional, inter-country or even global scope, but are not  
645 accounted for, regularly proposed policy recommendations could be arbitrary and their value for  
646 decision- or policy makers thus unclear.

647 This paper further tried to contribute to the literature by proposing a decomposition of the traditional  
648 technical efficiency model. We presumed that a careful choice of inputs and outputs could differentiate  
649 the information the technical efficiency model contains on operational and physical productivity. The  
650 results of the efficiency analysis support this line of thought, showing a lower (higher) sensitivity of the  
651 operational (physical) efficiency model to environmental variables when compared to traditional  
652 technical efficiency. Even though a conceptual decomposition of technical efficiency could not be  
653 validated by the results of the productivity analysis, basing policy implications on the findings of the  
654 operational efficiency model, might nonetheless allow to make justified claims about decision-makers'  
655 input allocation efficiency and help find best practices for future productivity increases.

656 Interestingly, while the trend of technical productivity was found to be moderately positive for the  
657 considered period, physical productivity decreased, hence casting serious doubts on the idea of an

658 ongoing harmonization of resource savings and provision of food and fiber. In conjunction with the  
659 technical efficiency model containing only limited information on actual produce, we conclude that the  
660 second issue raised, whether conventional technical efficiency and productivity analysis should be  
661 motivated by sustainability goals, should be objected to.

662 Finally, we would like to encourage future analyzes employing any nonparametric approach to assess  
663 determinants of efficiency to include environmental variables into their framework. Accounting for the  
664 stochastic nature of agricultural production methodologically might be useful, yet not always fully get  
665 a grasp on the structural impact spatially varying climatic features have on technical efficiency. By  
666 avoiding these conventions of nonparametric efficiency and productivity analyzes, future studies could  
667 help decision-makers to indeed improve their input allocation efficiency with targeted policy  
668 implications, while avoiding to wrongfully attribute inefficiency due to climatic factors outside of their  
669 sphere of influence or their conscious and rational choices.

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**Appendix.**

S1. Pairwise correlation coefficients and corresponding significance levels for operational model inputs and outputs.

	Costs land	Costs labor	Intermediate Consumption	Capital costs	Gross output
Costs land	1				
Costs labor	0.33***	1			
Intermediate Consumption	0.37***	0.97***	1		
Capital costs	0.40***	0.87***	0.93***	1	
Gross output	0.38***	0.96***	0.99***	0.93***	1

Note: \*\*\*, \*\* and \* denote significance at 1%, 5% and 10% level.

S2. Pairwise correlation coefficients and corresponding significance levels for physical model inputs and outputs.

	UAA	Labor	Intermediate Consumption	Total assets	Yield wheat	Yield maize	Milk produce
UAA	1						
Labor	0.85***	1					
Intermediate Consumption	0.94***	0.80***	1				
Total assets	0.64***	0.47***	0.74***	1			
Yield wheat	0.97***	0.77***	0.95***	0.71***	1		
Yield maize	0.92***	0.75***	0.90***	0.71***	0.92***	1	
Milk produce	0.88***	0.81***	0.92***	0.88***	0.88***	0.84***	1

Note: \*\*\*, \*\* and \* denote significance at 1%, 5% and 10% level.