

PROPAGATION OF IMPACT-INDUCED SEISMIC WAVES INTO THE INTERIOR OF A RUBBLE-PILE ASTEROID

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MOTIVATION

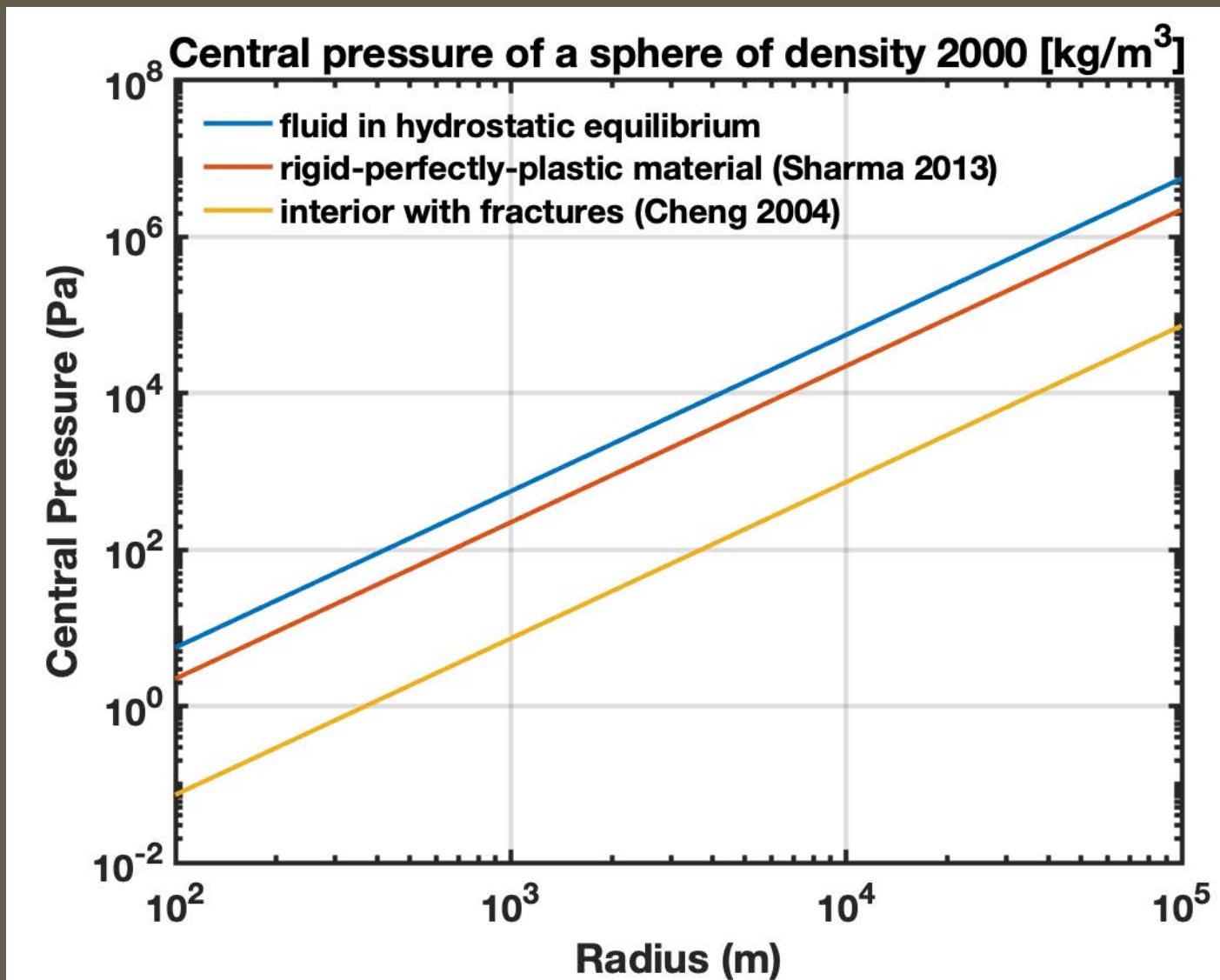
- Effects of impact induced seismic waves into the interior of a selfgravity body
- Dependence of wavespeed with the increasing pressure in the interior
- Effects on the relocation of the material in the interior
- Visible effects on the surface far from the impact point



PRESSURE IN THE INTERIOR OF AN ASTEROID (THEORETICAL MODELS)

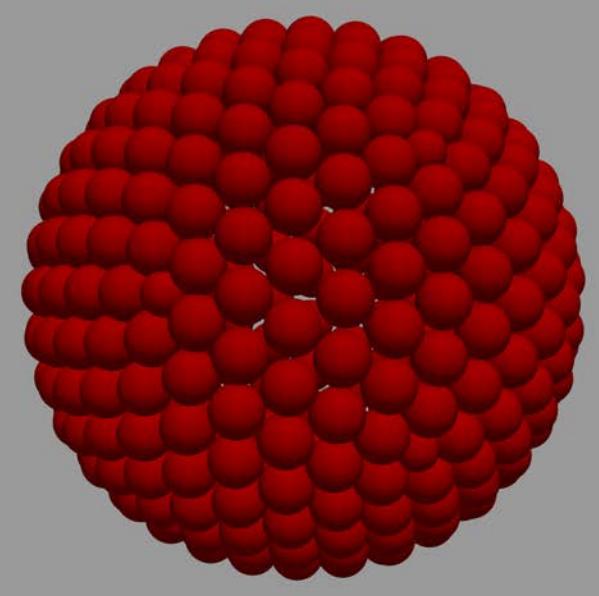
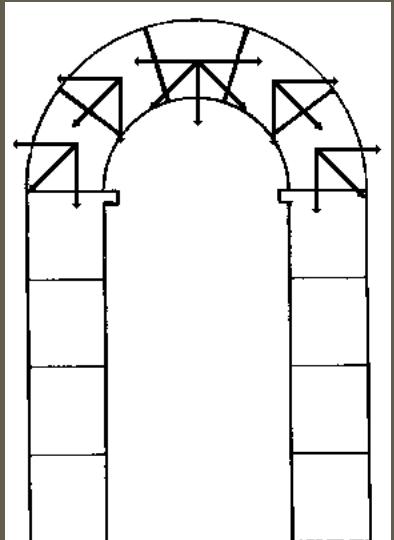
Variation of the pressure inside an agglomerated asteroid computed with three methods:

- A fluid in hydrostatic equilibrium
- A rigid perfectly plastic material, according to eqs. from Sharma (2013)
- An asteroid with vessels in the interior filled with granular material (Cheng 2004)



PRESSURE IN THE INTERIOR OF AN ASTEROID (RUBBLE PILE MODELS)

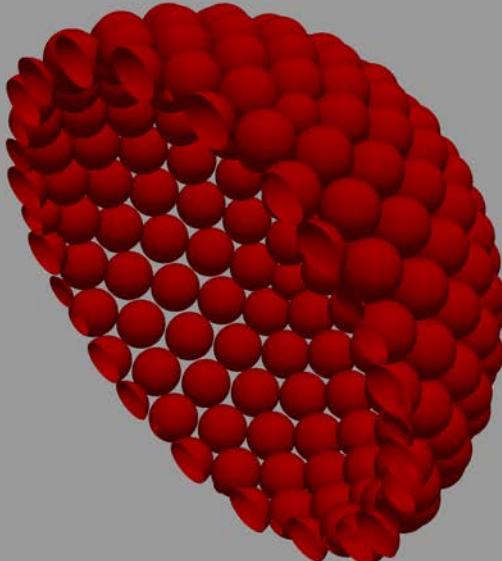
An agglomerated asteroid could have chain forces among the particles that hold the weight of the overlaying material, like an architectural arc or dome.



Hypothetical extreme object, with one layer of particles, maintained by self-gravity

The pressure in the interior will be 0.

Cut of the interior



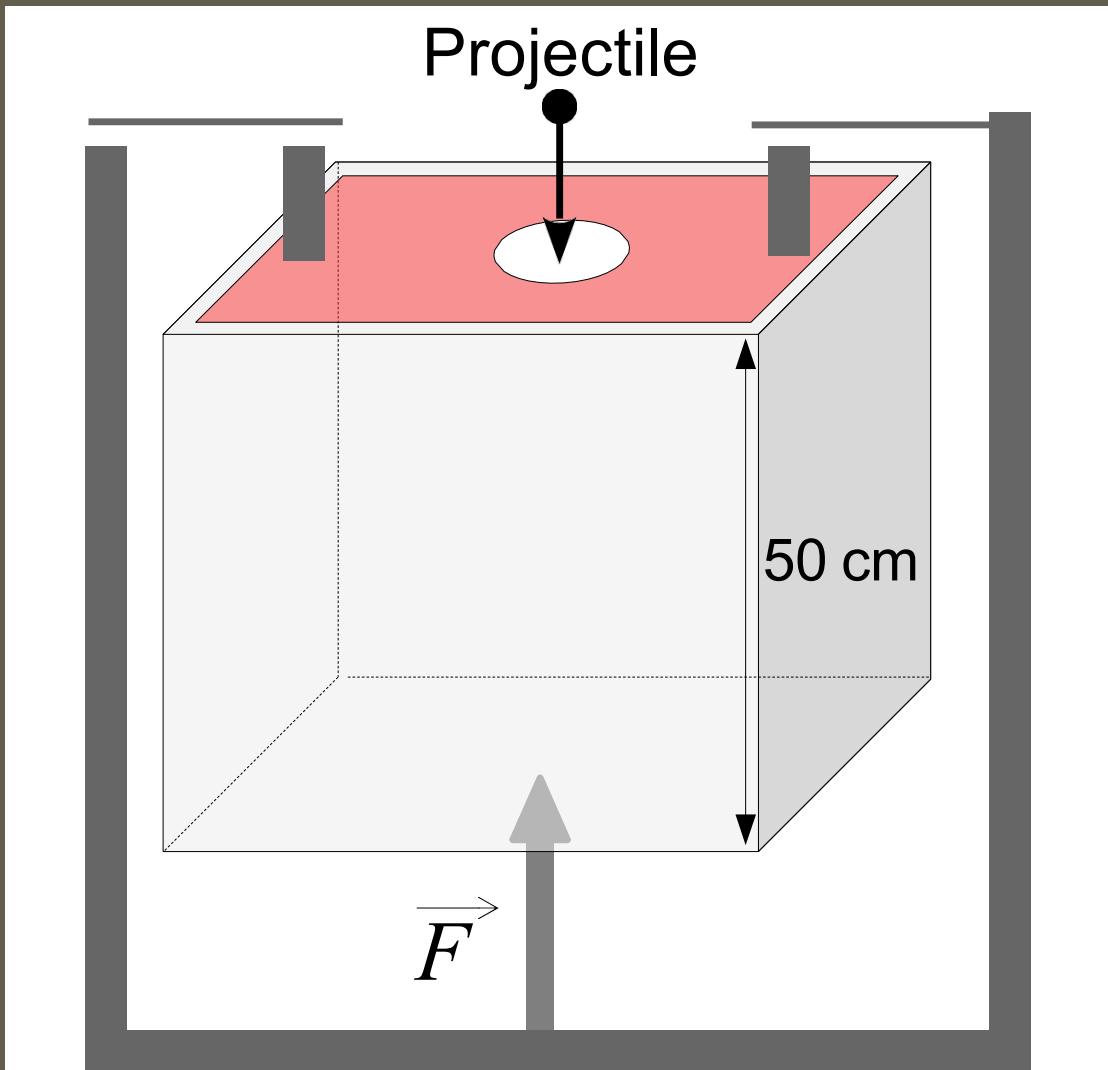
HOW MIGHT THIS EFFECT AFFECT THE PROPAGATION OF IMPACT-INDUCED WAVES INTO THE INTERIOR?

TWO APPROACHES

Laboratory experiments in Earth-gravity with different granular materials and a wide range of velocities.

Numerical simulations with a DEM code, with different elastic material properties, velocities up to the sound speed of the solid material and a wide range of gravity regimes.

EXPERIMENTAL SETUP

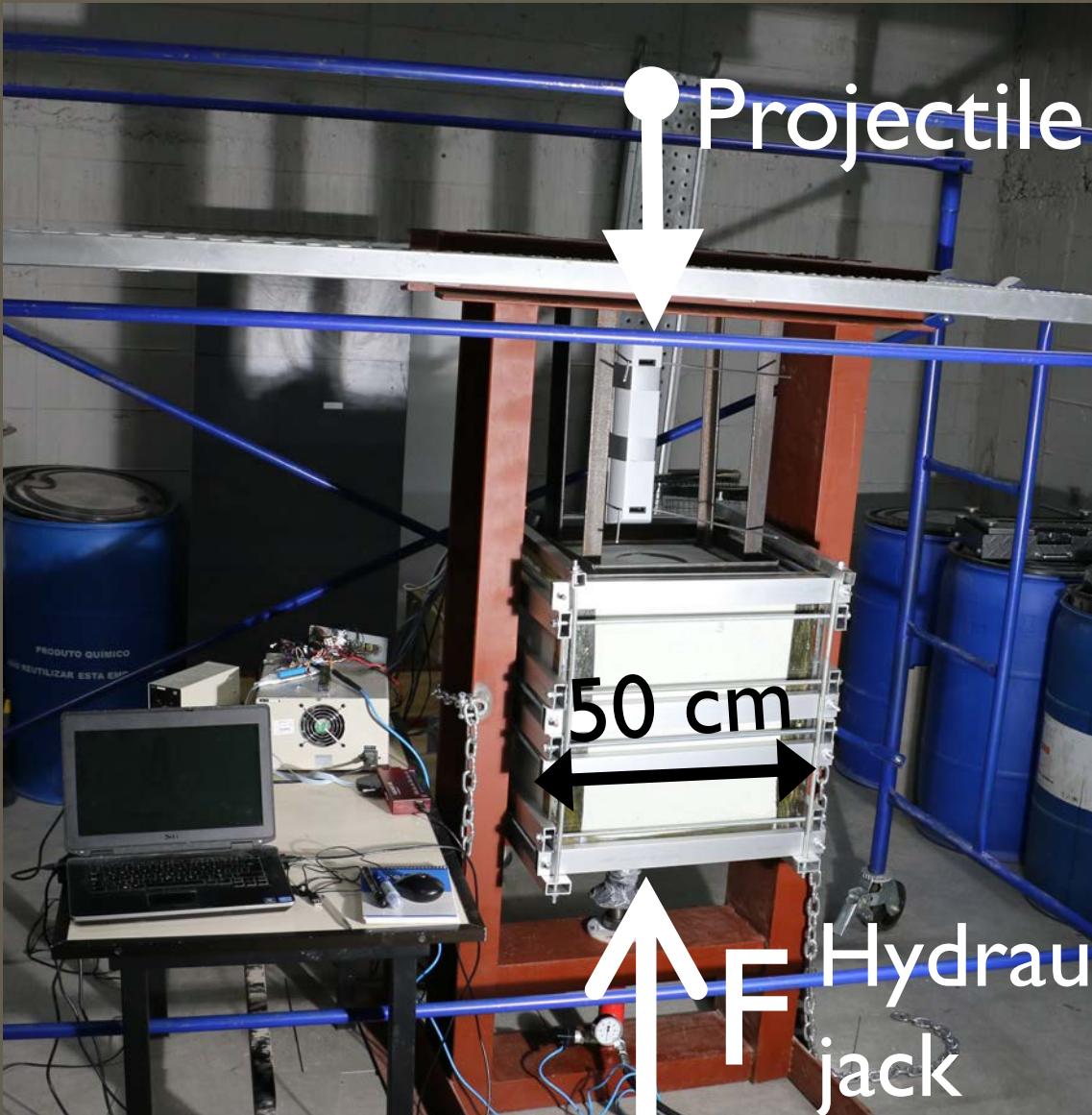


- Granular media in a movable cubic box with a hydraulic jack
- Top cover cannot move
- Small aperture on top for impact

Previous similar experiments:

- Yasui et al. 2015
- Van den Wildenberg et al. 2013
- Delage et al. 2017

EXPERIMENTAL SETUP



Selfgravity is mimicked
by static loading

Top view

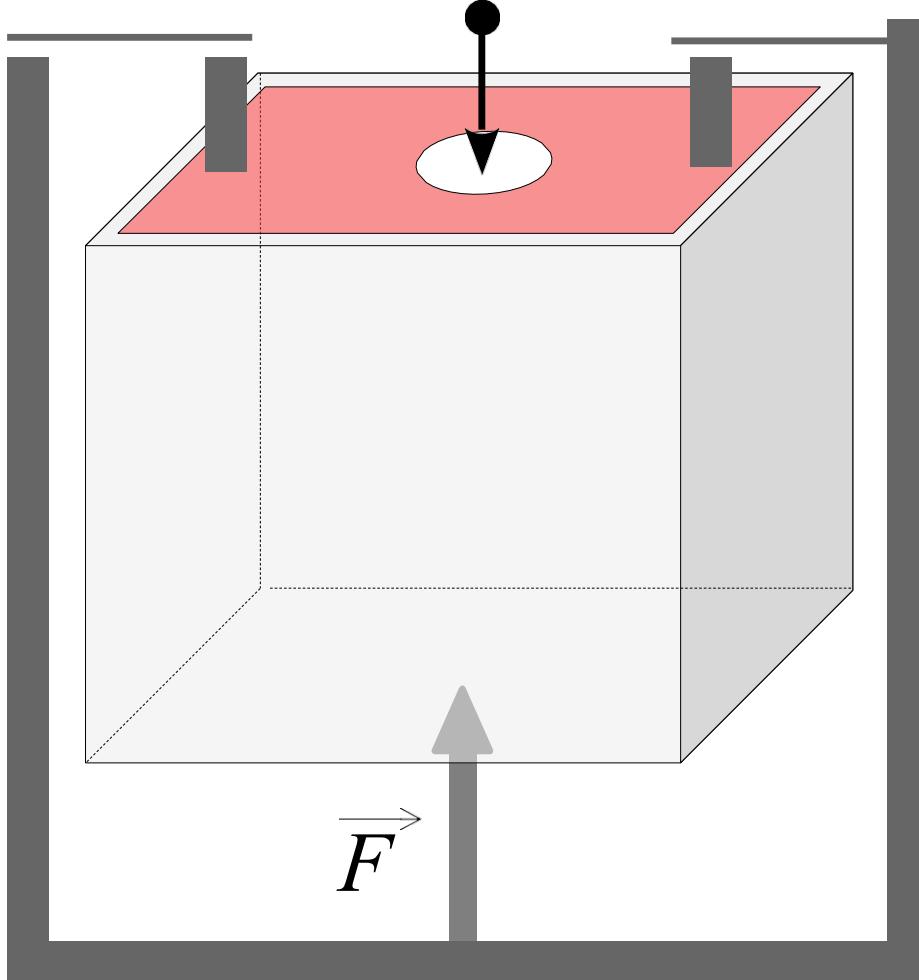


EXPERIMENTAL LIMITATION AND QUESTIONS

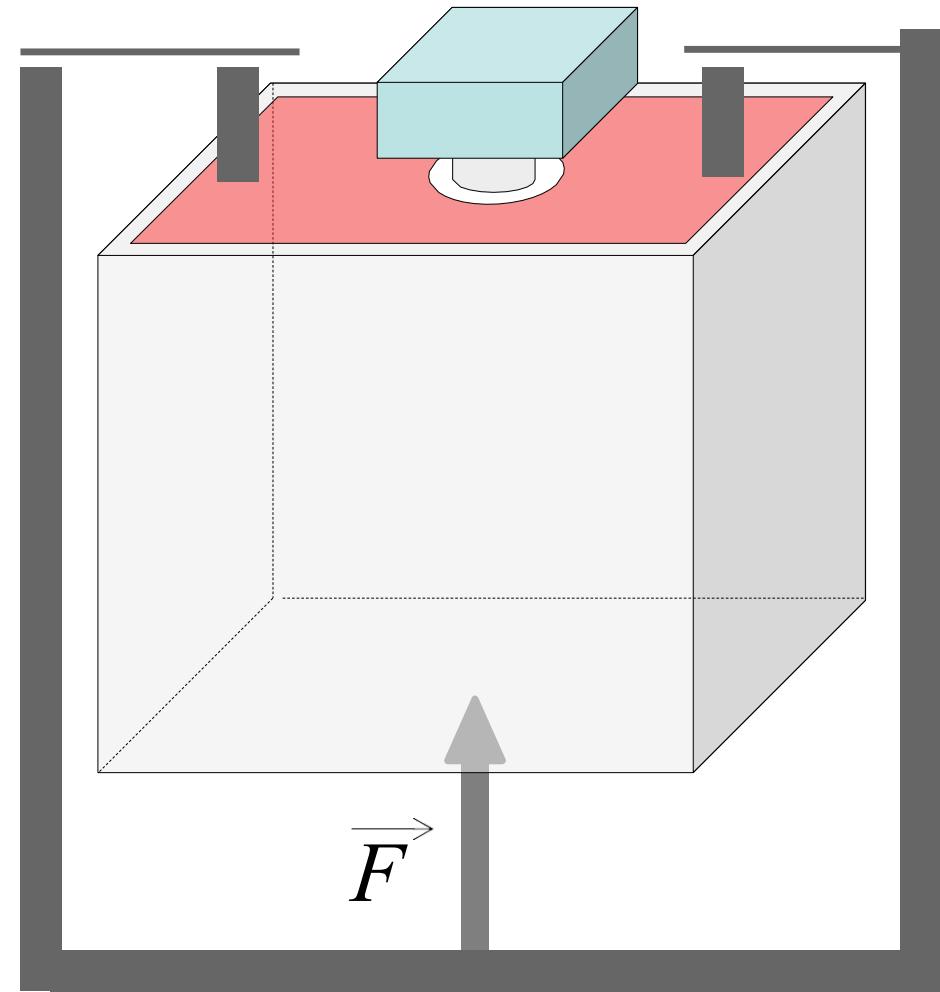
- Does confining pressure mimic selfgravity? (min= *atm.*)
- How can we extrapolate our results to micro-g?
- Are non-impact induced waves equivalent? e.g. waves produced by vibrations (relevant for a microgravity experiment in orbit)

TWO TYPES OF GENERATED WAVES IMPACT AND SHAKER

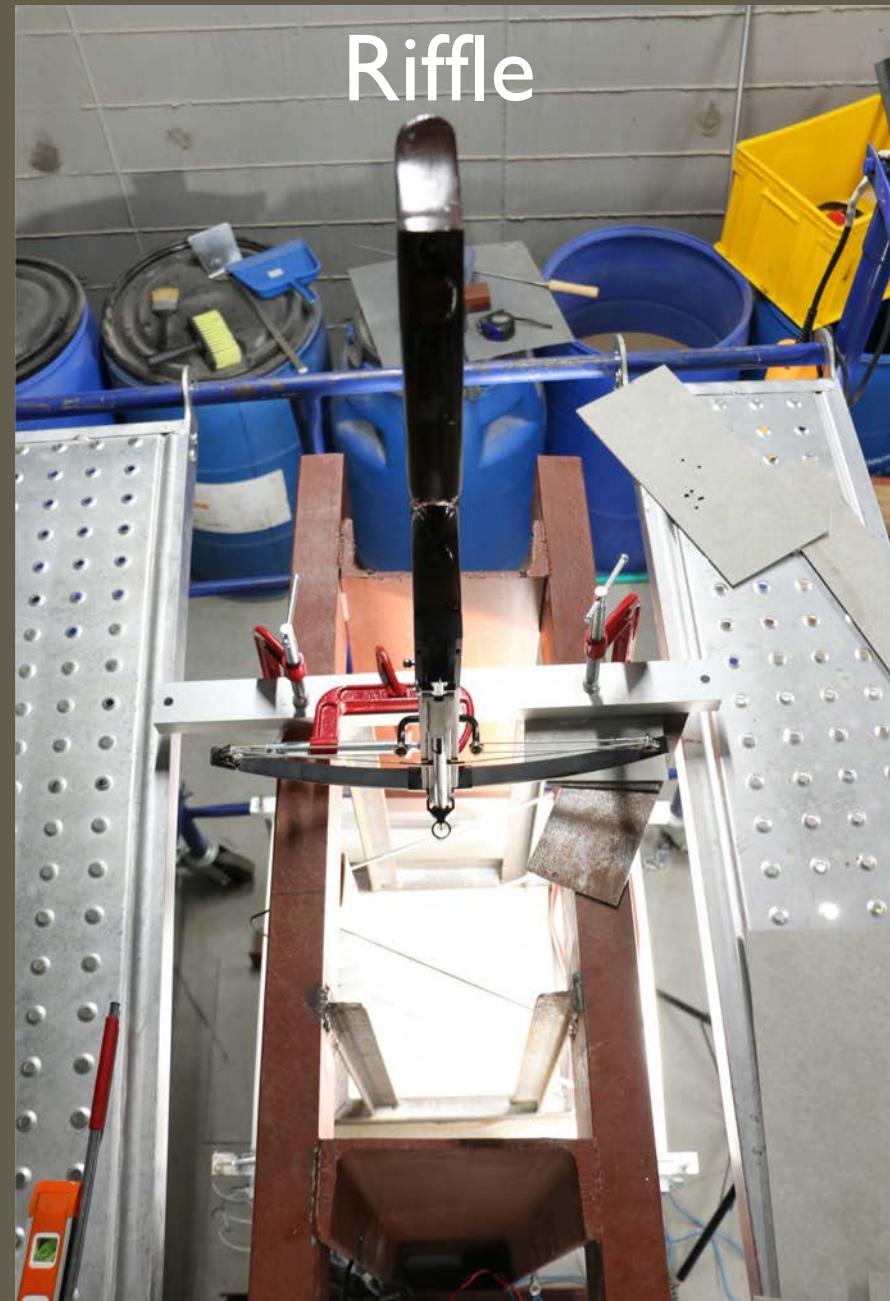
Projectile



Shaker

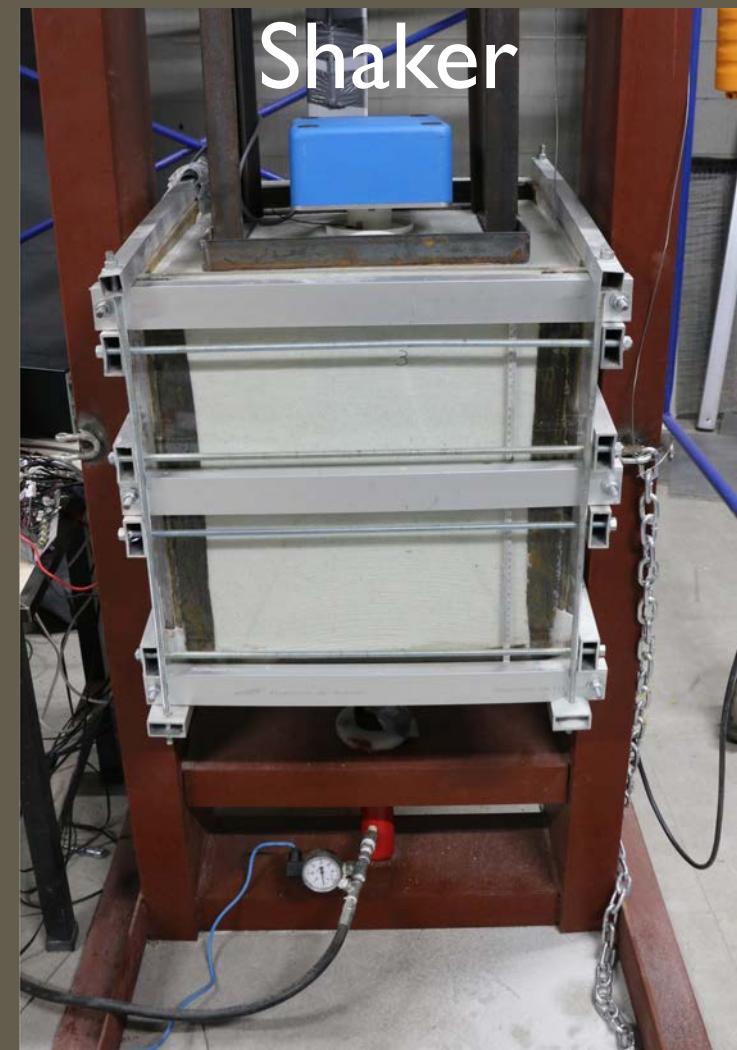


Riffle



IMPACT vs. SHAKER

Shaker



GRANULAR MEDIA

Natural: granite gravel



Irregular shapes

Artificial: Glass beads



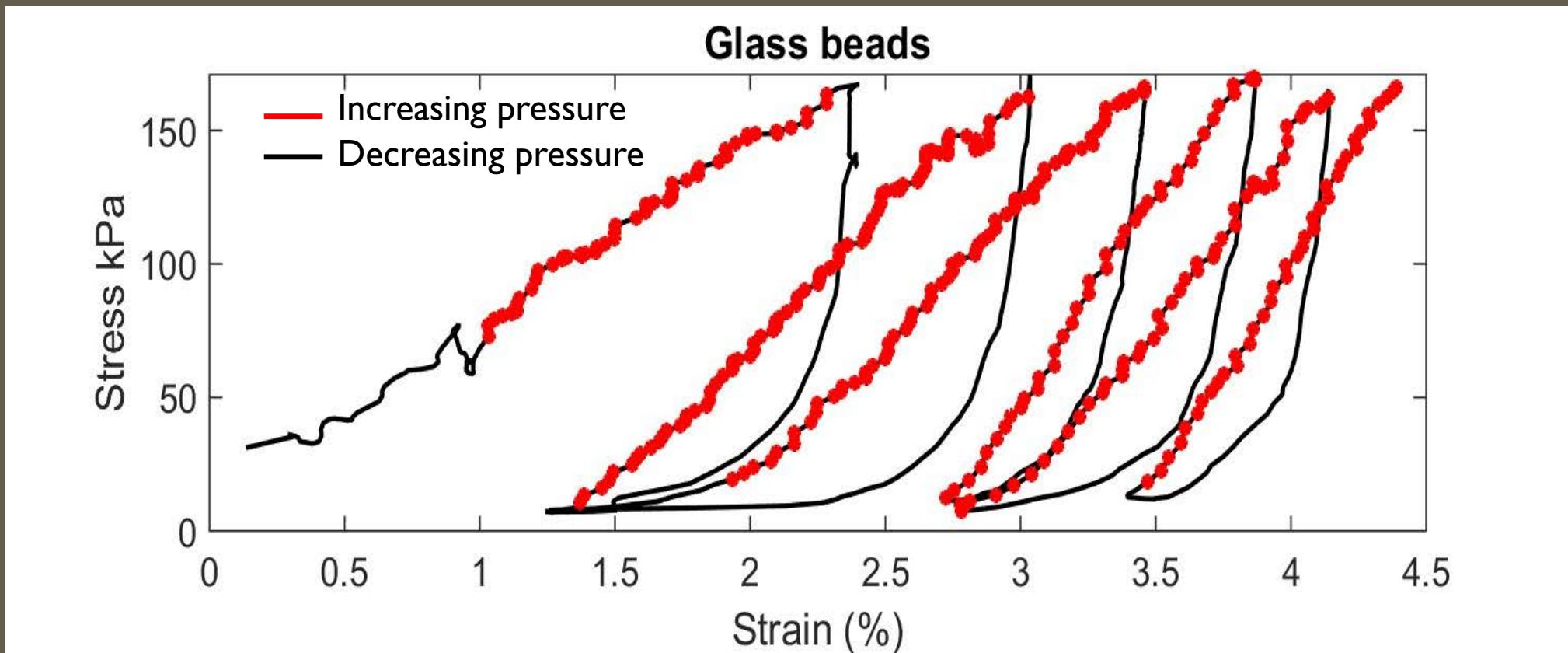
Spherical shapes

| Type | mm | Porosity (%) |
|--------|----------|--------------|
| Gravel | 1 - 4 | 35 |
| Sand | 0.25 - 2 | 38 |

| Type | mm | Porosity (%) |
|-------|-----------|--------------|
| Glass | 0.125 - 1 | 15 |

STRESS-STRAIN QUASI-STATIC RELATIONSHIP

After loading the material into the box, we perform a set of increase and release of pressure with the hydraulic jack. We study the hysteresis of the granular material.



- Strong hysteresis (non-reversible motions of grains)
- Several loading to “stabilize the system”

Spherical bullets

PROJECTILES

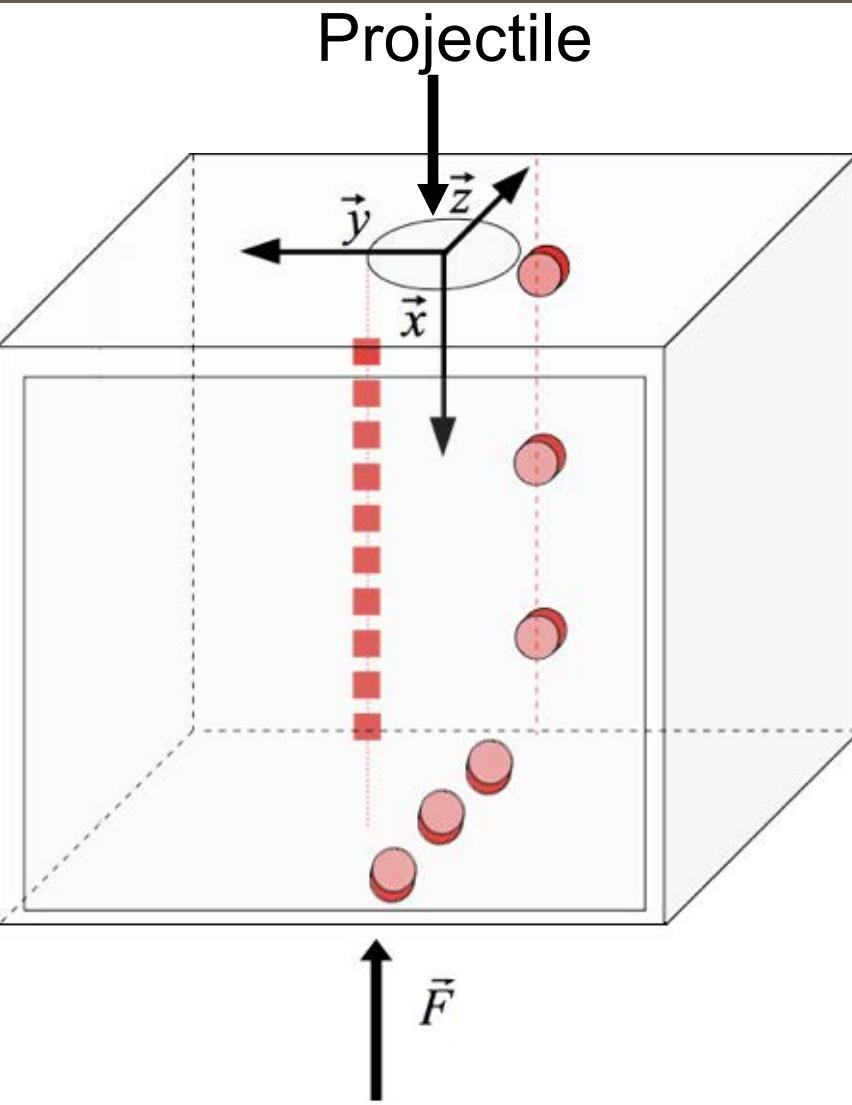


GUNS

Rifle ~ 300m/s



MEASUREMENTS INSIDE THE BOX

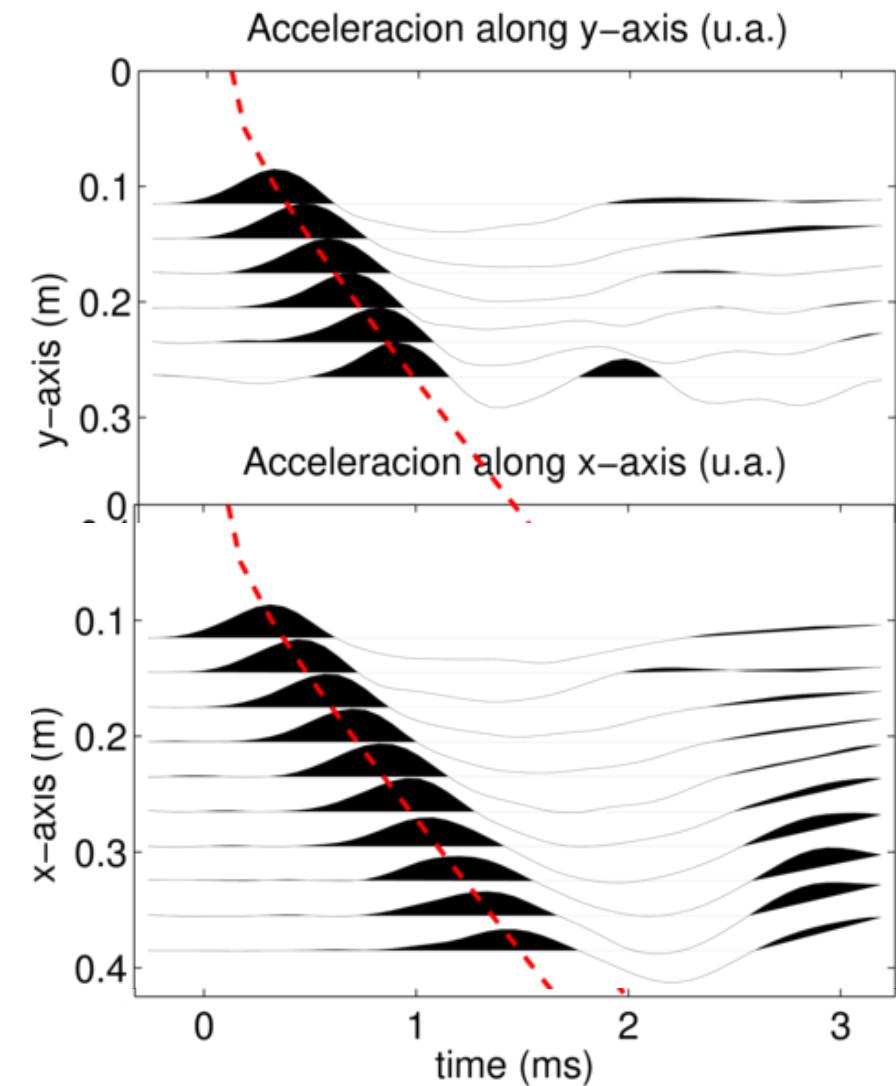


From the analysis of the polarization

→ P-Wave

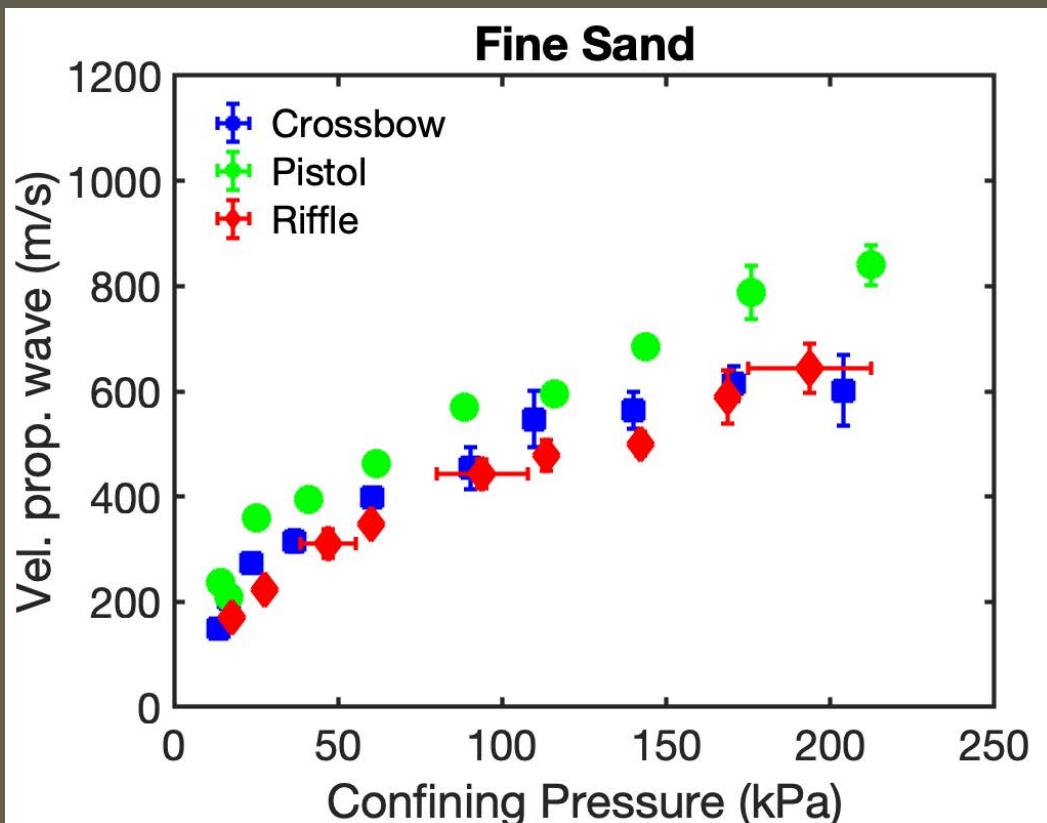
$$f \approx 500 \, Hz$$

$$\lambda \approx 0.4 \, m$$

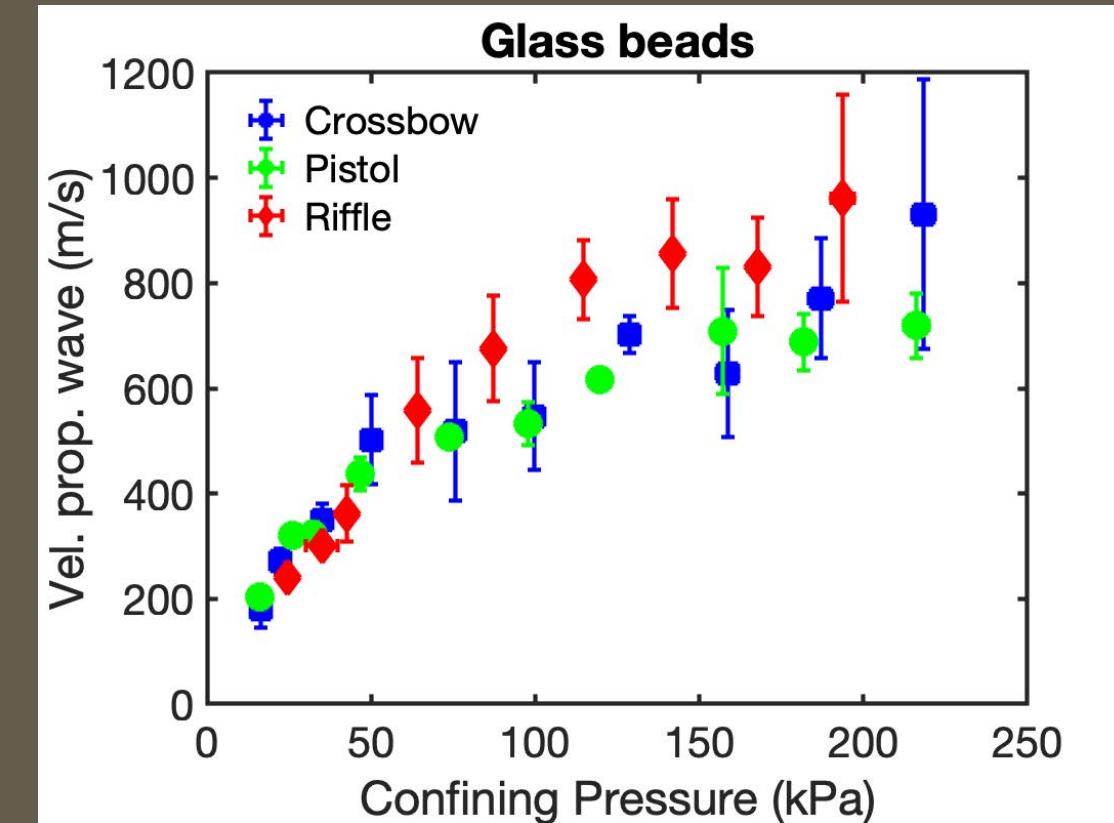


VELOCITY OF THE IMPACT INDUCED WAVE vs CONFINING PRESSURE

Fine Sand 0.5-1 mm



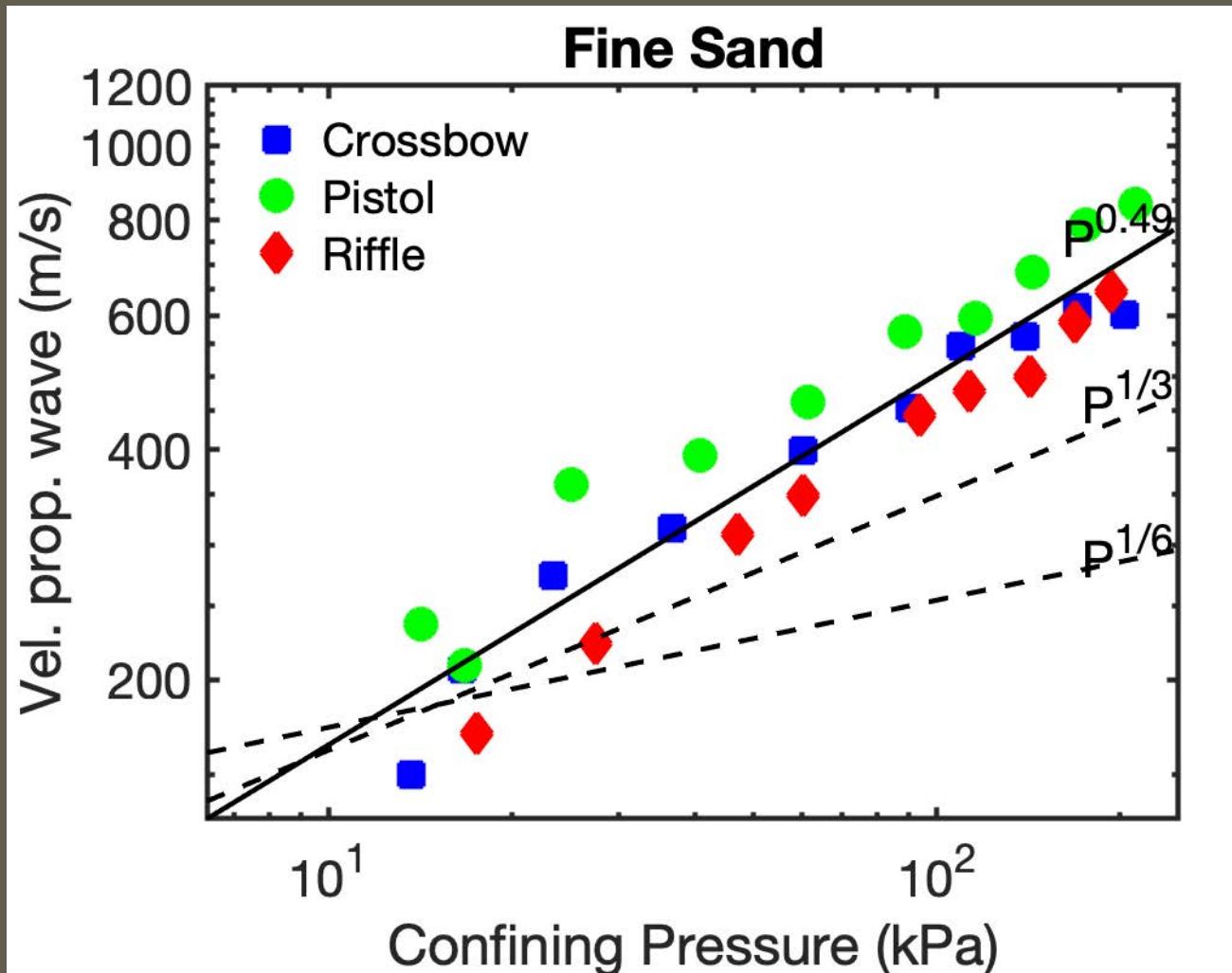
Glass beads 0.25-1 mm



→ No clear dependency on kinetic energy

→ bulk material more significant than grain size

VELOCITY OF THE IMPACT INDUCED WAVE vs. CONFINING PRESSURE OBS. vs. THEORY

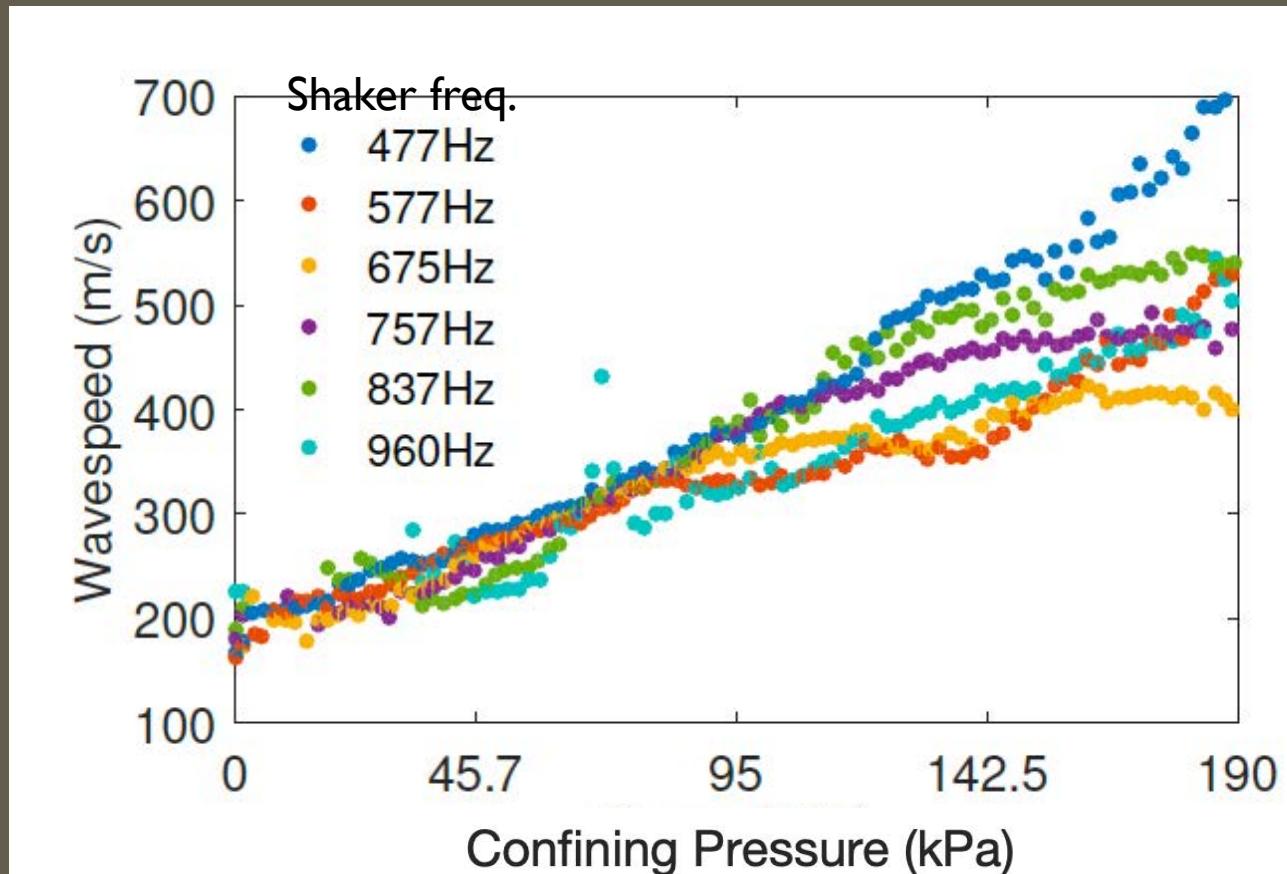
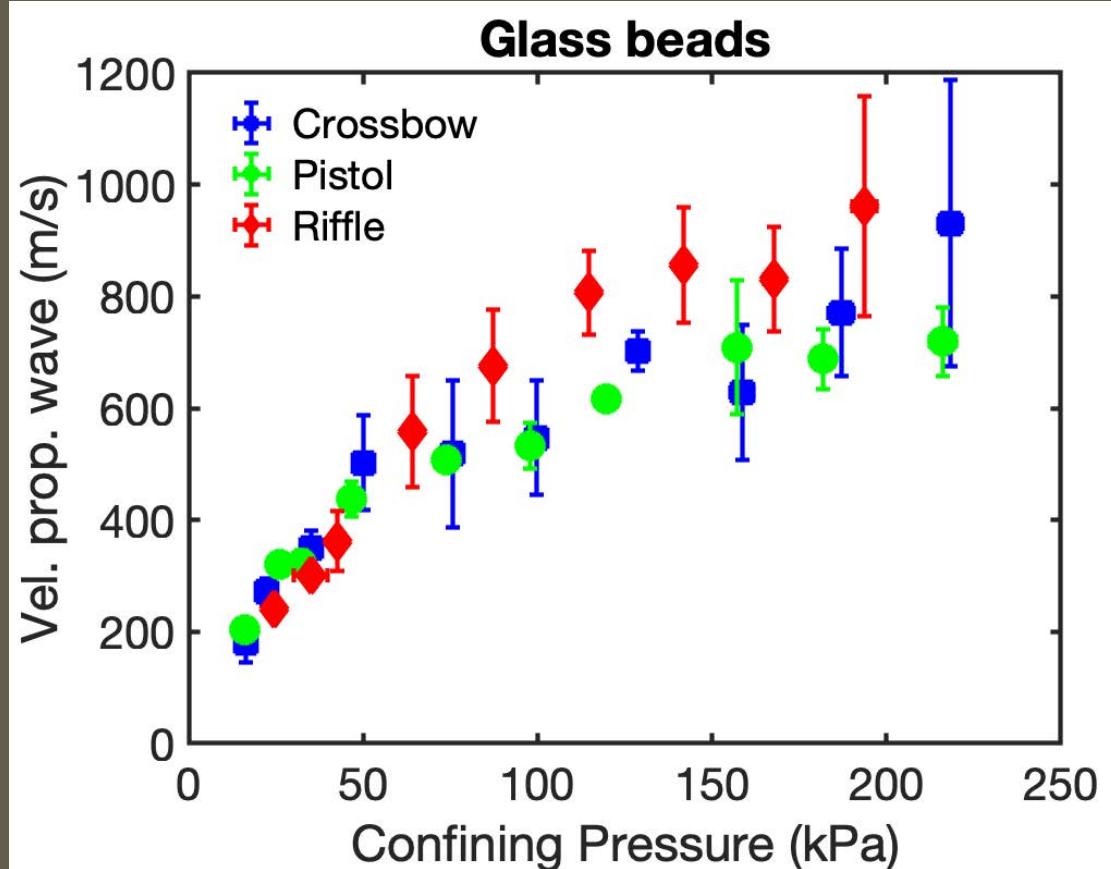


→ close to linear-like relationship

→ \neq Hertz-Mindlin theory

$$V \propto P^{1/3-1/6}$$

IMPACT VS SHAKER - LABORATORY



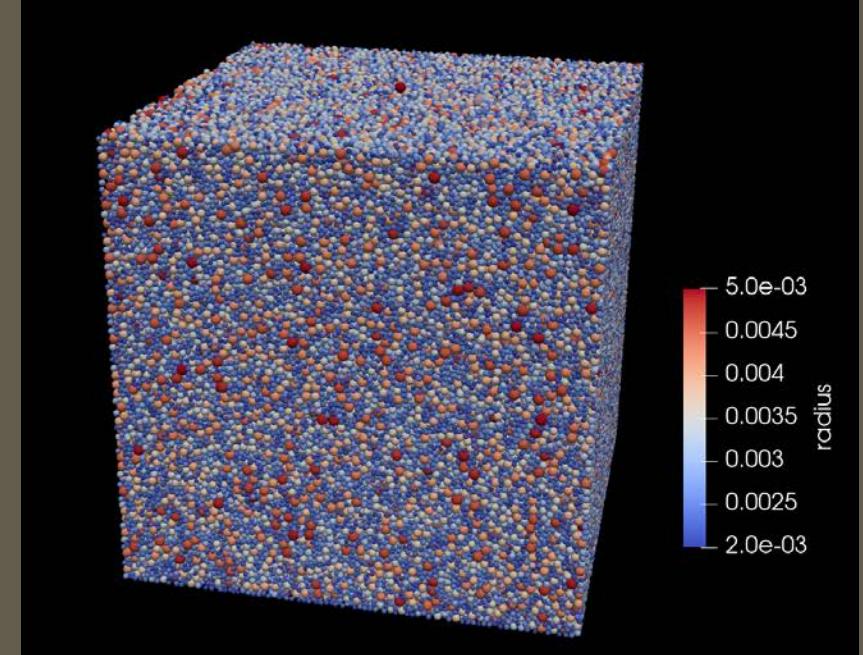
IMPACT / SHAKER COMPARISON

| | Impact | Shaker |
|--------------|----------------------------------|--------------------------|
| Acceleration | $> 3,5 \text{ m/s}^2$ | $\sim 0,2 \text{ m/s}^2$ |
| Frequency | $\sim 500 \text{ Hz}$ | $\sim 500 \text{ Hz}$ |
| Polarization | P-Wave | P-Wave |
| Wavespeed | Similar dependence with pressure | |

Implications: Possibility to conduct safe experiments in orbit (micro-g) with granular media & shaker to study the wave propagation

NUMERICAL SIMULATIONS

- Code: ESyS-Particle
- Create initial conditions:
 - Generate block of particles
 - Cube 0.4x0.4x0.4 m
 - Particles: sizes between 2-5 mm
 - Particle density: 3000 kg/m^3
 - ~ 300.000 particles
- Several settling steps under different gravity conditions.

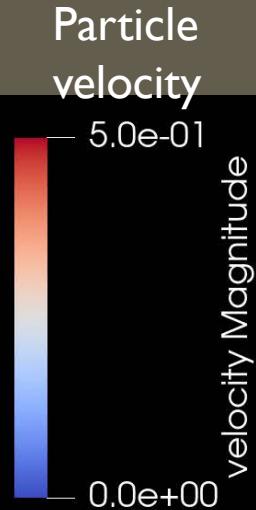
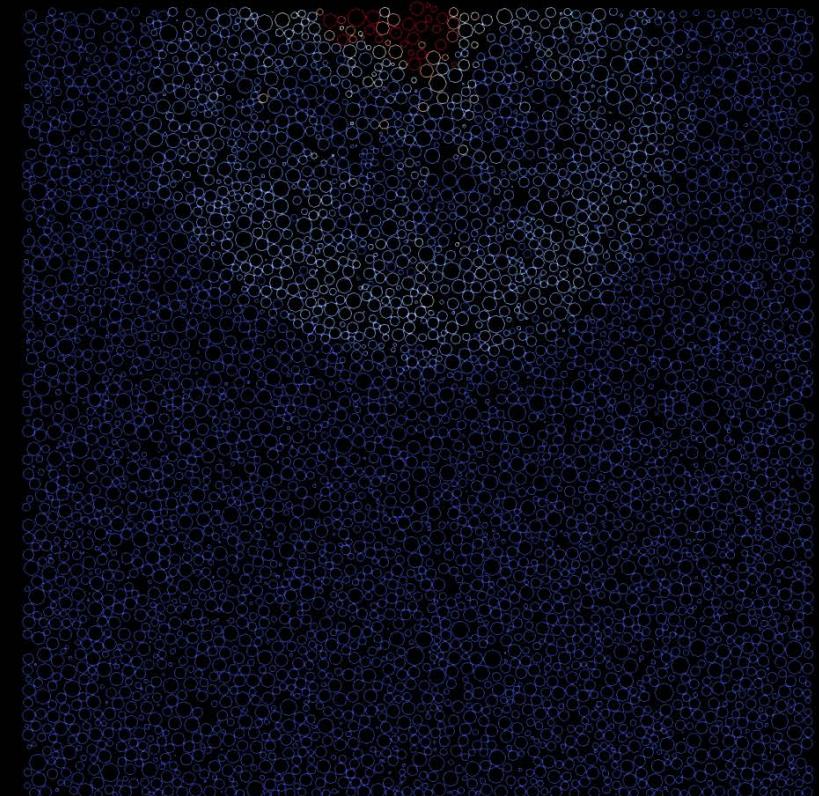
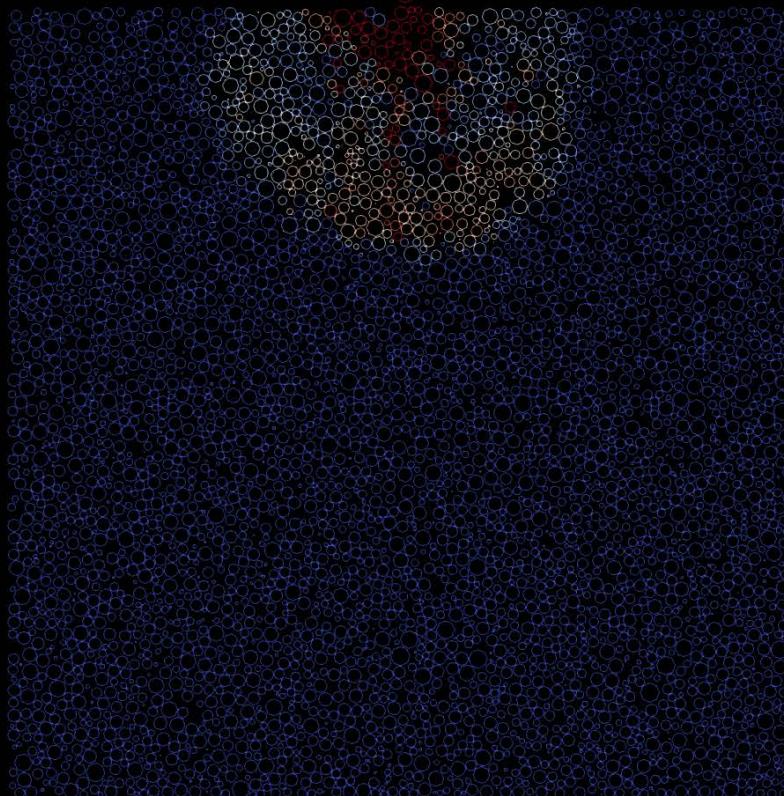
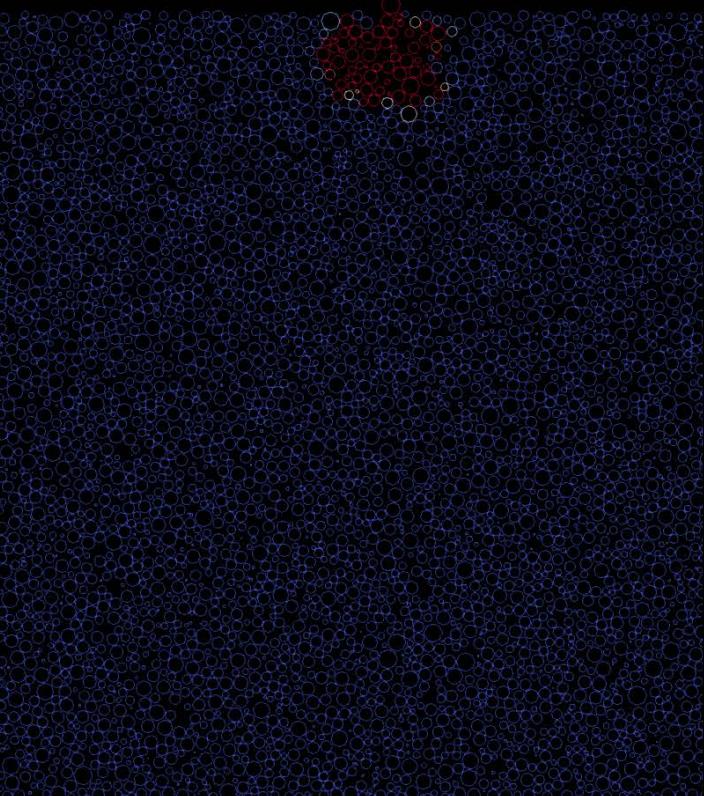


PROPAGATION OF IMPACT INDUCED WAVES

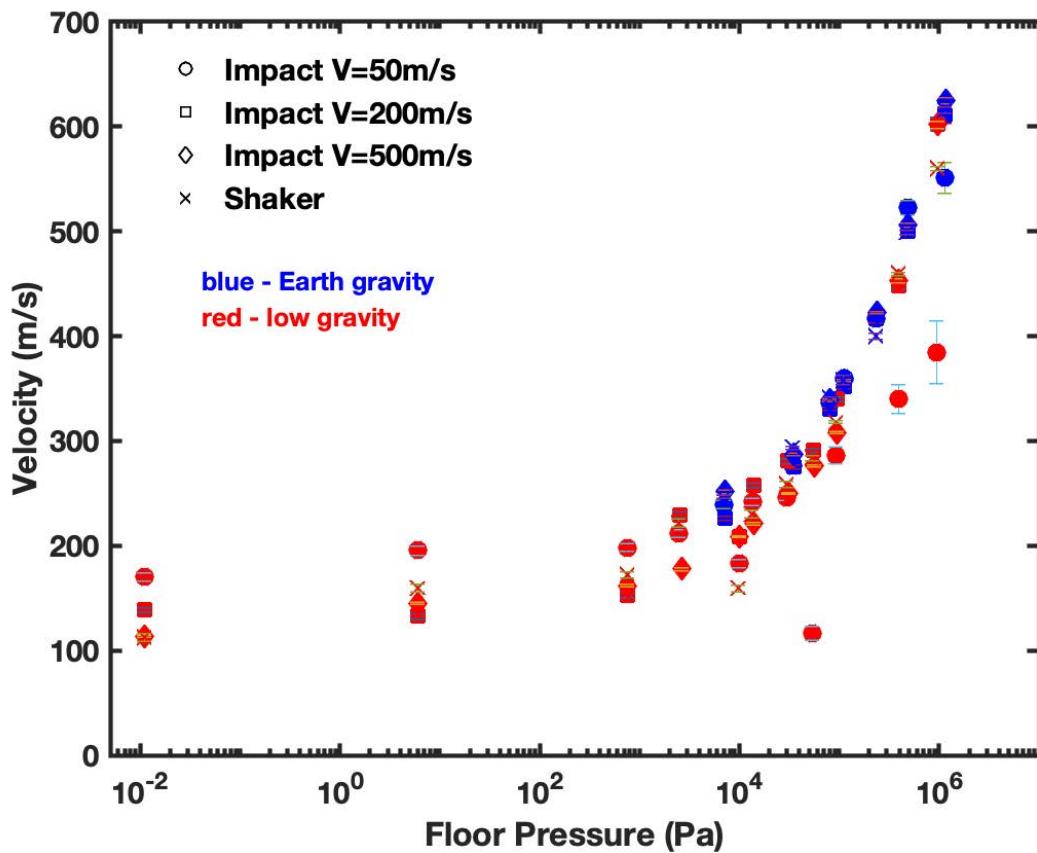
Impact of a 5mm projectile at $v_{imp}=50,200,500$ m/s.

We also perform similar experiments with a simulated shaker.

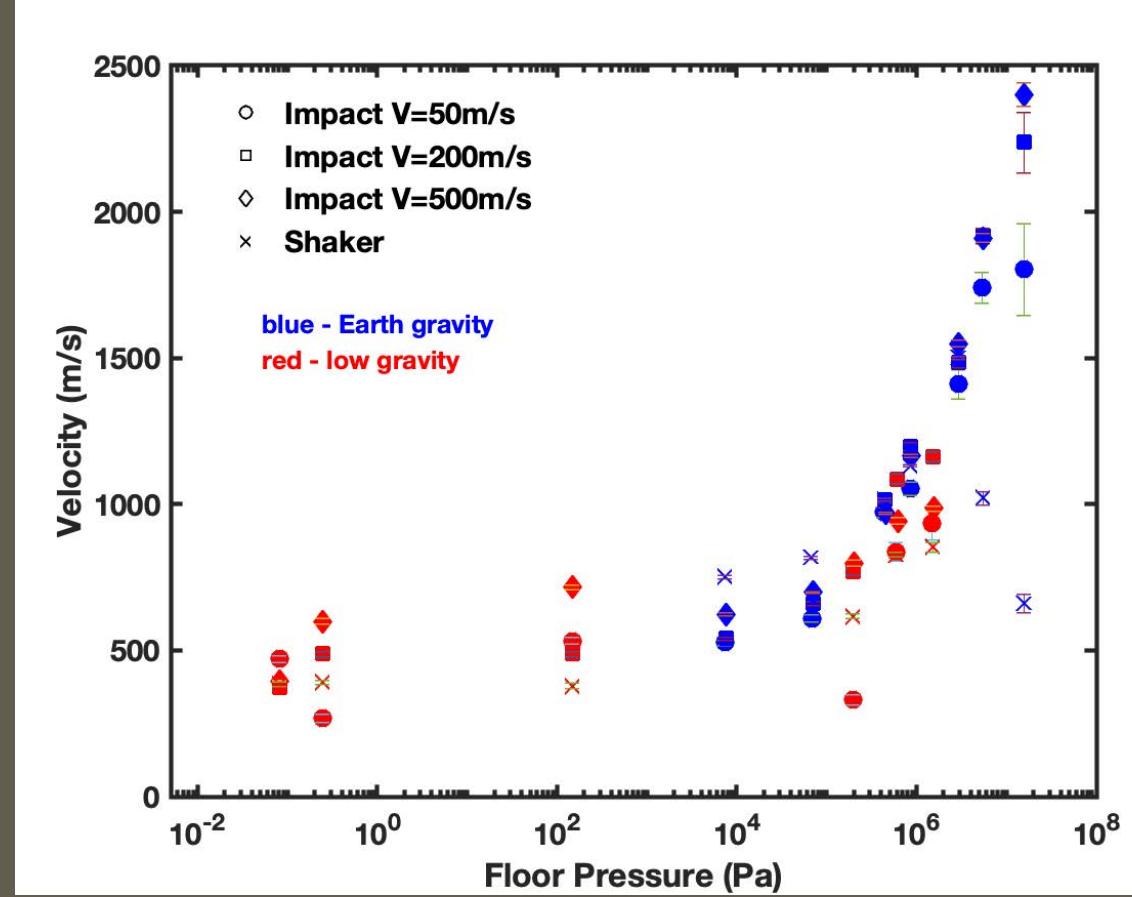
Snapshots of a slice in the interior below the impact point at 3 different times separated by 10^{-5} s ($v_{imp}=200$).



WAVE PROPAGATION OVER 7 ORDERS IN PRESSURE

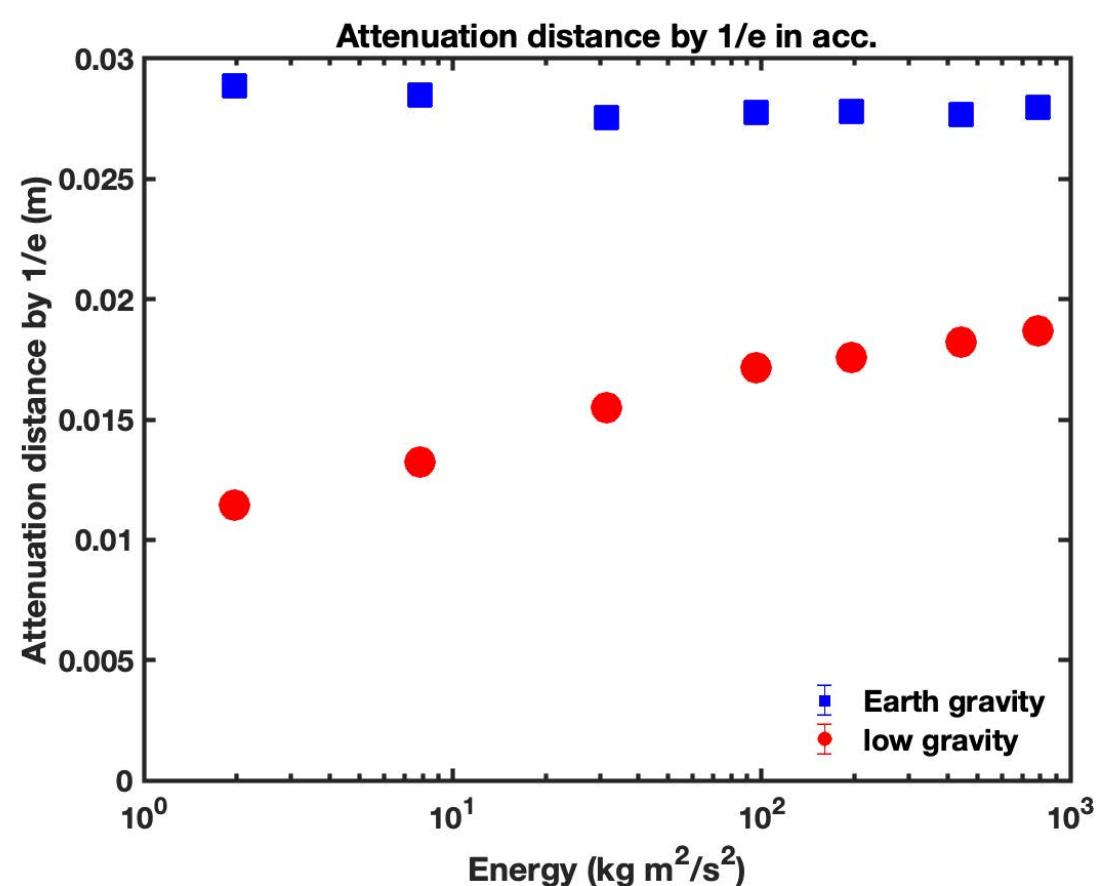


Material type I ($Y=10^{10}$ Pa)

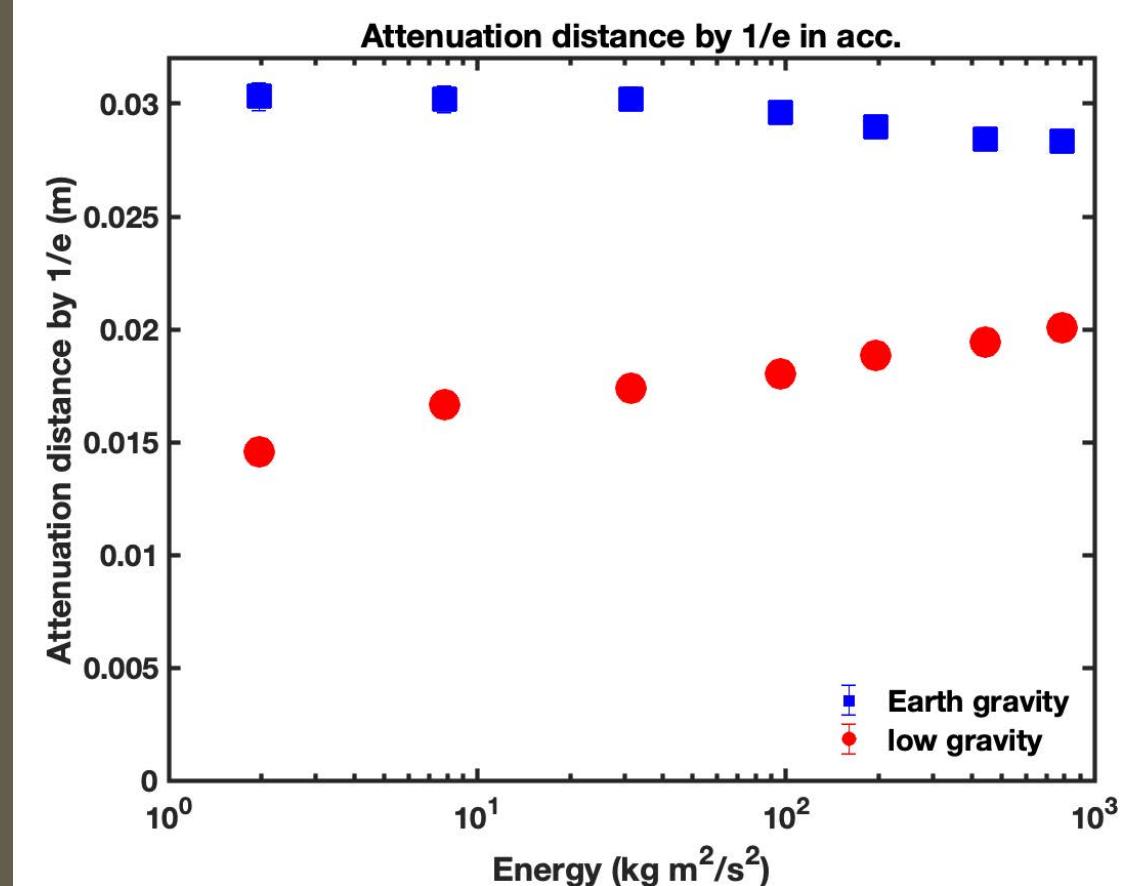


Material type II ($Y=10^{11}$ Pa)

ATTENUATION OF THE WAVE



Material type I ($\Upsilon=10^{10} \text{ Pa}$)



Material type II ($\Upsilon=10^{11} \text{ Pa}$)

SIMULATION RESULTS

- The propagation speed does not depend on the speed of the projectile or the generation mechanism (impact vs shaker).
- There is exponential dependence of propagation speed (v) with the confining pressure (P) with a similar factor b for materials with different strengths.

$$v = a 10^{bP} + v_0$$

| | a | b | v_0 (m/s) |
|------------------|------|------|-------------|
| $Y = 10^{10}$ Pa | 3.15 | 0.36 | 141 |
| $Y = 10^{11}$ Pa | 4.2 | 0.36 | 447 |

- Asymptotic speed at $P \rightarrow 0$: for low strength material ~ 140 m/s
for high strength material ~ 450 m/s

CONCLUSIONS

- Impacts induce a P-compression wave
- Equivalence between impact and shaker
- Increase of wavespeed with confining pressure

IMPLICATIONS FOR DART

- For a 160m granular asteroid (like Didymos B), pressures at the interior $\lesssim 10$ Pa. Very low P-wavespeed.
- The seismic wave induced by the DART impact will take ~ 1 sec. to travel across the body.
- Very high attenuation. Could very low-speed ejecta be produced far from the impact point?

FUTURE WORK

- Extend lab. experiments with hypervelocity projectiles
Electrothermal accelerometer is under construction.
Impact speeds of 2-4 km/s.
- Lab. experiments with a shaker in low-g are desirable
(Hermes facility in ISS)