

Alloy Scattering and Field-Dependent Electron Transport in Direct-Gap $\text{Ge}_{1-x}\text{Sn}_x$ Alloys

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Incorporation of Sn in Ge to form $\text{Ge}_{1-x}\text{Sn}_x$ alloys has been theoretically predicted and experimentally confirmed to drive an indirect- to direct-gap transition. This signals significant potential for applications in optoelectronic devices suitable for monolithic integration on Si, stimulating ongoing efforts to develop direct-gap group-IV optoelectronic devices compatible with complementary metal-oxide-semiconductor (CMOS) fabrication [1]. Proposed device applications of $(\text{Si})\text{Ge}_{1-x}\text{Sn}_x$ alloys – including mid-infrared lasers for Si photonics, 1 eV absorber layers for multi-junction solar cells, and tunneling field-effect transistors for post-CMOS electronics [3] – mandate detailed understanding of carrier transport in the alloy, particularly in the presence of an applied electric field.

The indirect- to direct-gap transition in $\text{Ge}_{1-x}\text{Sn}_x$, which occurs for Sn composition $x \approx 8\%$, reorders the Γ - and L-point valleys in the lowest energy conduction band (CB), with the former being lower in energy for $x > 8\%$. This has long been predicted to drive strong enhancement of the electron mobility μ at low field, due to the low Γ -valley effective mass [2]. However, there has to date been limited analysis of the impact of Sn incorporation on the low-field μ , and no explicit analysis of field-dependent electron transport in the alloy. The direct-gap $\text{Ge}_{1-x}\text{Sn}_x$ CB structure – characterized by a low effective mass zone-center Γ -valley minimum flanked by higher energy, high effective mass zone-edge L- and X-point satellite valleys – can also be expected to give rise to negative differential resistance (NDR) in the presence of an applied electric field. Achieving NDR – the so-called Gunn effect, which is present in several direct-gap III-V semiconductors and is exploited to provide efficient microwave power generation for sensing applications – represents potentially novel electrical functionality in a group-IV semiconductor.

We present the first explicit calculations of field-dependent electron transport in $\text{Ge}_{1-x}\text{Sn}_x$ alloys, informed by recent developments in our understanding of the details of the CB structure [4]. We firstly analyze the evolution of the low-field electron mobility with x , via direct evaluation of the Sn-induced intra- and intervalley alloy scattering rates based on atomistic alloy supercell calculations. Our calculations demonstrate strong enhancement of the low-field μ in the direct-gap regime which, in the absence of defects, can exceed that of GaAs for Sn compositions $x > 11\%$. We then consider field-dependent transport, in which an electric field drives the electron population out of thermal equilibrium. We solve the Boltzmann transport equation in the relaxation time approximation, including inter- and intra-valley scattering of electrons by acoustic and optical phonons, and by the alloy potential. Our calculations reveal strong dependence of the electron mobility and drift velocity on the field strength F , characterized by prompt acceleration of Γ -valley electrons and rapid intervalley scattering to L valleys. We verify the presence of NDR in the direct-gap regime, but within a limited range of F vs. in III-V semiconductors, due to the absence of polar-optical phonon scattering in group-IV materials.

References

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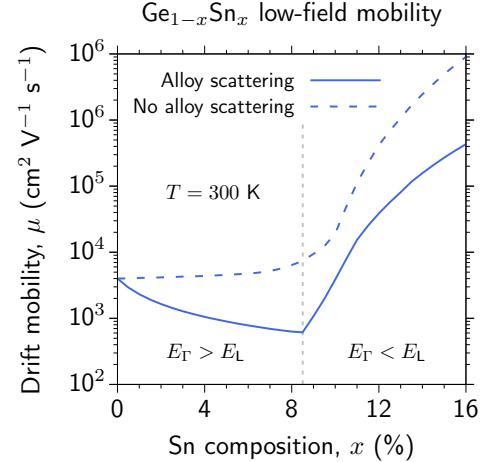


Fig. 1. Evolution of the low-field electron mobility μ with x in $\text{Ge}_{1-x}\text{Sn}_x$, calculated with (solid blue) and without (dashed blue) alloy scattering. The alloy is direct-gap for $x > 8\%$ (dotted gray), beyond which composition μ increases strongly as electrons occupy the low effective mass Γ -valley.